

- 1 Here is a representation of four quanta of energy,  $q$ , distributed among three molecules:  $q|q|qq$ . How many ways can the four units of energy end up with one in first molecule, one in the second molecule, and two in the third molecule?

A 1  
 B  $q = 4$   
 C  $q! = 4! = 4 \cdot 3 \cdot 2 \cdot 1 = 24$

- 2 Here is a representation of four units of energy,  $q$ , distributed among  $m = 3$  molecules:  $q|q|qq$ . How many different ways can the two partitions,  $|$ , be assigned to achieve the arrangement  $q|q|qq$ ?

A 1  
 B  $(m - 1)! = (3 - 1)! = 2 \cdot 1 = 2$   
 C  $m! = 3! = 3 \cdot 2 \cdot 1 = 6$

- 3 Here is a representation of four units of energy,  $q$ , distributed among  $m = 3$  molecules:  $q|q|qq$ . How many different arrangements of the six objects in the diagram are there, ignoring that  $q$  and  $|$  are different?

A  $m + q = 7$   
 B  $(m - 1) \cdot q = 6$   
 C  $(q + m - 1)! = 6! = 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 720$

- 4 How many ways (distinct or not) can the arrangement  $q|q|qq$  of four quanta among three molecules be made?

A  $q! \cdot m! = 2! \cdot 2! = 4$   
 B  $q! \cdot (m - 1)! = 4! \cdot (3 - 1)! = 24 \cdot 2 = 48$   
 C  $(q + m)! = (4 + 3)! = 7! = 5040$

- 5 Two arrangements of  $q = 4$  quanta among  $m = 3$  molecules are  $q|q|qq$  and  $qqq||q$ . Which relation is true about the number of \*unique\* ways,  $We(q, m)$ , that  $q$  quanta can be distributed among  $m$  molecules?

A  $We(q, m) = q! \cdot m!$   
 B  $We(q, m) = (q + m - 1)!$   
 C  $We(q, m) \cdot q! \cdot (m - 1)! = (q + m - 1)!$

- 6  $We(q, m) = (q + m - 1)! / (q! \cdot (m - 1)!)$  is the number of unique ways that  $q$  quanta can be distributed among  $m$  molecules. How many ways can two quanta be distributed among three molecules?

A 3  
 B 6  
 C 9

- 7 We( $q, m$ ) =  $(q + m - 1)! / (q! * (m - 1)!)$  is the number of unique ways that  $q$  quanta can be distributed among  $m$  molecules. How many ways can three quanta be distributed among three molecules?

- A 10
- B 16
- C 20