

## Lecture 8 CH131 Summer 1

Tuesday, June 4, 2019

- Relative boiling points

### Ch11: Solutions

- Vapor pressure lowering,  $P_1 = x_1 P^{\circ}_1$
- Boiling point elevation,  $T_b - T^{\circ}_b = K_b m_c$
- Freezing point depression,  $T^{\circ}_f - T_f = K_f m_c$
- Osmotic pressure,  $\Pi = RTM_c$

**Next lecture:** Begin ch12: Thermodynamic processes and thermochemistry



3

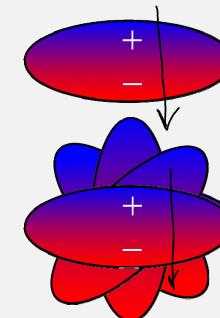
## Relative boiling points

Effects of

- Dispersion — always, but weak
- Dipole-dipole interaction — polar molecules, moderate
- Hydrogen bonding — N-H, O-H, F-H, strongest

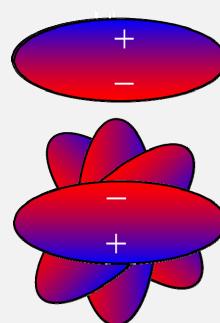
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## Dispersion always attractive

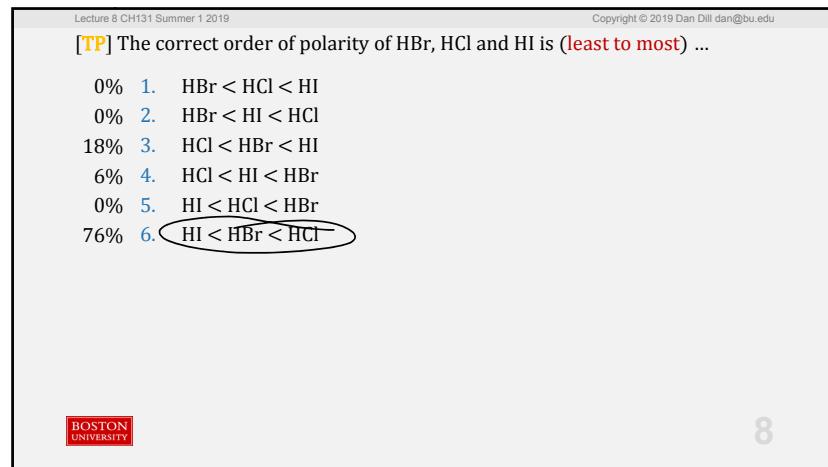
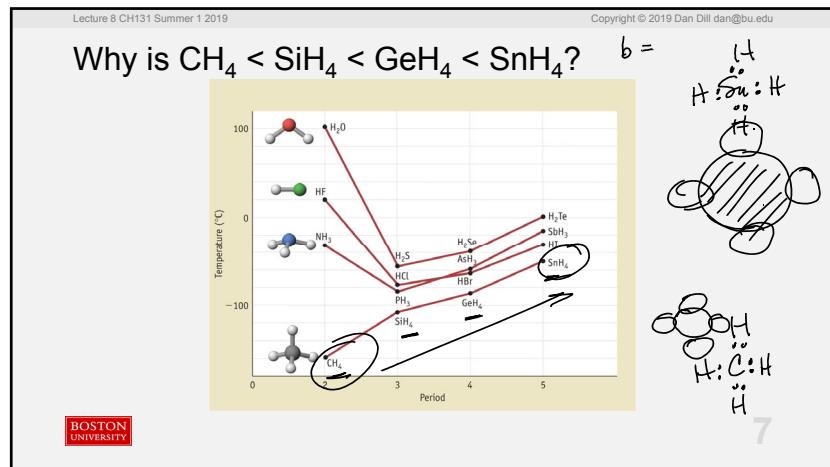
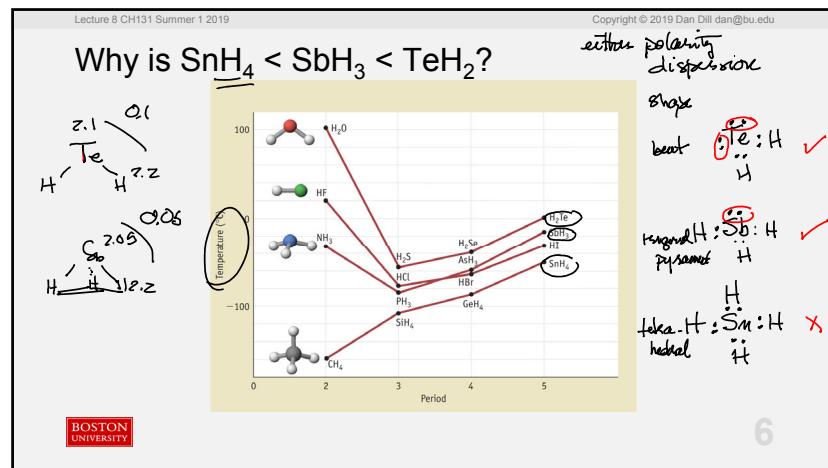
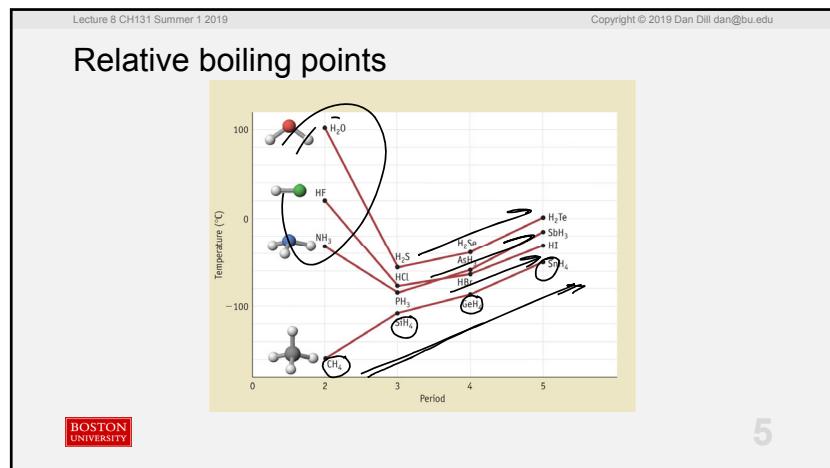


4

## Dipole can be attractive or repulsive



3



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[TP] The correct order of **boiling point** of HBr, HCl and HI is (lowest to highest) ...

0% 1. HBr < HCl < HI  
 0% 2. HBr < HI < HCl  
 31% 3. HCl < HBr < HI ✓ observed  
 6% 4. HCl < HI < HBr  
 13% 5. HI < HCl < HBr  
 50% 6. HI < HBr < HCl expect

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### Why is HCl < HBr < HI?

A graph showing boiling points of various hydrides across five periods. The y-axis is Temperature (°C) from -100 to 100. The x-axis is Period from 0 to 5. Key points include H<sub>2</sub>O at ~65°C (Period 2), HF at ~-18°C (Period 2), NH<sub>3</sub> at ~-78°C (Period 2), CH<sub>4</sub> at ~-160°C (Period 2), H<sub>2</sub>S at ~-60°C (Period 3), HCl at ~-85°C (Period 3), HBr at ~-90°C (Period 3), HI at ~-100°C (Period 3), H<sub>2</sub>Se at ~-80°C (Period 4), AsH<sub>3</sub> at ~-70°C (Period 4), GeH<sub>4</sub> at ~-60°C (Period 4), H<sub>2</sub>Te at ~-50°C (Period 5), SbH<sub>3</sub> at ~-40°C (Period 5), and SnH<sub>4</sub> at ~-30°C (Period 5). Handwritten notes show partial Lewis structures for HCl (H<sub>2</sub>Cl<sup>-</sup>) and HBr (H<sub>2</sub>Br<sup>-</sup>). A red arrow points from HCl to HI.

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### Why is NH<sub>3</sub> > PH<sub>3</sub> < AsH<sub>3</sub> < SbH<sub>3</sub>?

A graph showing boiling points of various hydrides across five periods. The y-axis is Temperature (°C) from -100 to 100. The x-axis is Period from 0 to 5. Key points include H<sub>2</sub>O at ~65°C (Period 2), HF at ~-18°C (Period 2), NH<sub>3</sub> at ~-78°C (Period 2), CH<sub>4</sub> at ~-160°C (Period 2), H<sub>2</sub>S at ~-60°C (Period 3), HCl at ~-85°C (Period 3), HBr at ~-90°C (Period 3), HI at ~-100°C (Period 3), H<sub>2</sub>Se at ~-80°C (Period 4), AsH<sub>3</sub> at ~-70°C (Period 4), GeH<sub>4</sub> at ~-60°C (Period 4), H<sub>2</sub>Te at ~-50°C (Period 5), SbH<sub>3</sub> at ~-40°C (Period 5), and SnH<sub>4</sub> at ~-30°C (Period 5). Handwritten notes show partial Lewis structures for NH<sub>3</sub>, PH<sub>3</sub>, AsH<sub>3</sub>, and SbH<sub>3</sub>. A red arrow points from NH<sub>3</sub> to SbH<sub>3</sub>.

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### Why is OH<sub>2</sub> > FH > NH<sub>3</sub>?

A graph showing boiling points of various hydrides across five periods. The y-axis is Temperature (°C) from -100 to 100. The x-axis is Period from 0 to 5. Key points include H<sub>2</sub>O at ~65°C (Period 2), HF at ~-18°C (Period 2), NH<sub>3</sub> at ~-78°C (Period 2), CH<sub>4</sub> at ~-160°C (Period 2), H<sub>2</sub>S at ~-60°C (Period 3), HCl at ~-85°C (Period 3), HBr at ~-90°C (Period 3), HI at ~-100°C (Period 3), H<sub>2</sub>Se at ~-80°C (Period 4), AsH<sub>3</sub> at ~-70°C (Period 4), GeH<sub>4</sub> at ~-60°C (Period 4), H<sub>2</sub>Te at ~-50°C (Period 5), SbH<sub>3</sub> at ~-40°C (Period 5), and SnH<sub>4</sub> at ~-30°C (Period 5). Handwritten notes show partial Lewis structures for OH<sub>2</sub>, FH, and NH<sub>3</sub>. A red arrow points from OH<sub>2</sub> to SbH<sub>3</sub>.

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## Colligative properties

Non-volatile solute (negligible vapor pressure) ...

- lowers vapor pressure of solvent:  $P_1 = x_1 P^{\circ}_1, \Delta P = P^{\circ}_1 - P_1 = x_2 P^{\circ}_1$

$$x_1 = \frac{\text{mol of solvent}}{\text{mol of solvent} + \text{mol of solute}}$$

$$\text{NaCl(s)} \rightarrow \text{Na}^+(\text{aq}) + \text{Cl}^-(\text{aq})$$

$$1 \text{ mol} \rightarrow 1 \text{ mol} \quad 1 \text{ mol}$$

$$x_1 = \frac{55 \text{ mol}}{55 + 2} = 0.96$$

$$2.8 \text{ kPa} \quad 0.96 \times 3 \text{ kPa}$$

$$\text{NaCl(s)} \quad \text{P}^{\circ}_1 = 3 \text{ kPa}$$

$$25^\circ \text{C}$$

$$1 \text{ L of H}_2\text{O} = 1000 \text{ g} \times \frac{1 \text{ mol}}{18 \text{ g}}$$

$$= 55 \text{ mol}$$

$$1 \text{ mol of NaCl in 1 L of water}$$

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## Colligative properties

Non-volatile solute (negligible vapor pressure) ...

- lowers vapor pressure of solvent:  $P_1 = x_1 P^{\circ}_1, \Delta P = P^{\circ}_1 - P_1 = x_2 P^{\circ}_1$
- raises boiling point of solvent:  $T_b - T_b^{\circ} = i m_{\text{solute}} K_b = m_c K_b$

$$i = \frac{\text{# of mol of solute particles in solution}}{\text{mol of solute}}$$

$$\text{NaCl: } i = 2$$

$$\text{Sugar: } i = 1$$

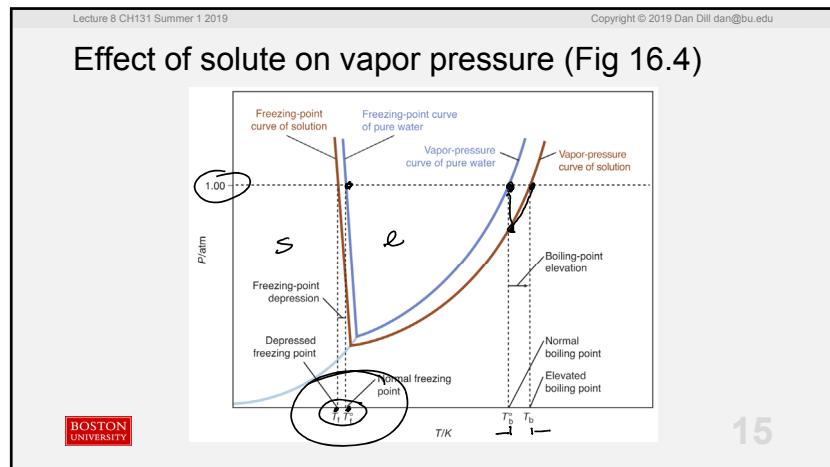
$$\text{CaCl}_2: i = 3$$

$$m = \text{molality} = \frac{\text{mol of solute}}{\text{kg of solvent}}$$

$$K_b = \text{boiling point elevation constant}$$

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## The more particles, the greater the effect

Sugar in water, 1 mol of particles per mol of sugar, so  $i = 1$

NaCl in water, 2 mol of particles per mol of NaCl, so  $i = 2$

Na<sub>2</sub>SO<sub>4</sub> in water, 3 mol of particles per mol of Na<sub>2</sub>SO<sub>4</sub>, so  $i = 3$

$$\text{Na}_2\text{SO}_4(\text{s}) \rightarrow 2 \text{Na}^+(\text{aq}) + \text{SO}_4^{2-}(\text{aq})$$

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16

## Colligative properties

Non-volatile solute (negligible vapor pressure) ...

- lowers vapor pressure of solvent:  $P_1 = x_1 P^\circ_1$ ,  $\Delta P = P^\circ_1 - P_1 = x_2 P^\circ_1$
- raises boiling point of solvent:  $T_b - T^\circ_b = i m_{\text{solute}} K_b = m_c K_b$
- lowers freezing point of solvent:  $T^\circ_f - T_f = i m_{\text{solute}} (K_f \cancel{+} m_c K_f)$

$$i m_{\text{solute}} = m_c$$

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17

## Freezing point example

Calculate the freezing point of 3.00 kg of water to which has been added 525 g of **ethylene glycol**,  $\text{OHC}_2\text{H}_4\text{OH}$ ,  $K_f = 1.86 \text{ K kg/mol}$

$$\frac{T_f - T_f^\circ}{T_f^\circ} = m_c K_f$$



$$m_c = \frac{525 \text{ g}}{62.1 \text{ g/mol}}$$

$$T_f^\circ - T_f = \frac{(525/62.1) \text{ mol}}{3.00 \text{ kg}} \cdot 1.86 \text{ K } \cancel{\frac{\text{kg}}{\text{mol}}} \quad \left. \begin{array}{l} \\ \end{array} \right.$$

$$= 5.25 \text{ K}, \quad T_f = -5.25^\circ \text{C} \quad \left. \begin{array}{l} \\ T_f^\circ = 0^\circ \text{C} \end{array} \right\}$$

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## Freezing point example again

Calculate the freezing point of 3.00 kg of water to which has been added 525 g of **sodium chloride**, NaCl,  $K_f = 1.86 \text{ K kg/mol}$

$$\text{Answer: } -11.1^\circ \text{C} \quad \text{NaCl(s)} \rightarrow \text{Na}^+(\text{aq}) + \text{Cl}^-(\text{aq})$$

$$\text{NaCl} = 58.4 \text{ g/mol}$$

$$T_f^\circ - T_f = \frac{2 \times 525 \text{ g}}{58.4 \text{ g/mol}} \cdot 1.86 \text{ K } \cancel{\frac{\text{g}}{\text{mol}}} \quad \left. \begin{array}{l} \\ \end{array} \right.$$

$$= 11.1$$

$$T_f = -11.1^\circ \text{C}$$

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[TP] A non-volatile solute lowers the vapor pressure of the solvent. This in turn means the boiling point of the solvent **must** increase. Why? Because ...

- 0% 1. higher temperature is necessary to evaporate the solute
- 35% 2. the solute particles stick to the solvent particles, analogous to van der Waals  $a$
- 65% 3. at the normal boiling point the vapor pressure of the solvent will be too low
- 0% 4. the solute vapor pressure is so low
- 0% 5. Some other reason

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[TP] The vapor pressure of water at 32 °C is 4.76 kPa. A glass of water is sealed in a 1.00 L container filled with air at 32 °C. After the water comes to equilibrium with the air in the container, the total pressure is 1 bar and there is 500. g of liquid water in the glass, and the partial pressure of water vapor in the container is ...

- 12% 1. less than 4.76 kPa  
 88% 2. 4.76 kPa  
 0% 3. more than 4.76 kPa  
 0% 4. Further information required

[Quiz] Then, 35.0 g of ethylene glycol is dissolved in the liquid water. After the water returns to equilibrium, the mass of the liquid water ...

- 35% 1. will have decreased  
 0% 2. will be unchanged  
 65% 3. will have increased  
 0% 4. Further information required

## Effect of solute on vapor pressure

The vapor pressure of water at 32 °C is 4.76 kPa. A glass of water is sealed in a container filled with air at 32 °C. After the water comes to equilibrium with the air in the container, the total pressure is 1.00 bar, there is 500. g of liquid water in the glass, and the volume of the container in addition to the glass and liquid water is 1.00 L

Then 35.0 g of ethylene glycol is dissolved in the water.

Calculate change in the mass of the liquid water after it has returned to equilibrium.

**Answer:** The mass of liquid water will increase by **0.000673 g**

## Colligative properties

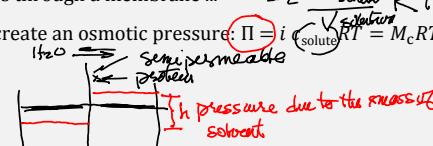
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- lowers freezing point of solvent:  $T_f^\circ - T_f = i m_{\text{solute}} K_f = m_c K_f$

$$i C_{\text{solute}} = M_c$$

If solute cannot pass through a membrane ...

- the solvent will create an osmotic pressure:  $\Pi = i \frac{M_{\text{solute}}}{V_{\text{solution}}} RT = M_c RT$



### Roadmap of osmotic pressure calculations

Osmotic pressure  $\Pi = i c R T$ .

$$C = \frac{\text{mol solute}}{\text{L solution}} = \text{molarity}$$

1. Use measured osmotic pressure,  $\Pi$ , and temperature,  $T$ , to evaluate concentration  $C = \Pi/(i R T)$ , in mol/L.
2. Use cell volume to express concentration in terms of moles,  $n = c V$ .
3. Use solute mass to calculate molar mass,  $M = \text{mass}/n$ .

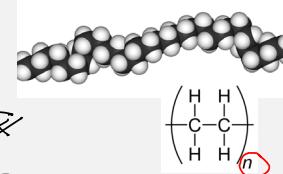
### Osmotic pressure $\Pi = i c R T$

1.40 g of polyethylene ( $i = 1$ ) dissolved in 100. mL of benzene generates an osmotic pressure of 0.248 kPa at 25 °C. Calculate the molar mass of the polyethylene.

1. Calculate the concentration...

$$\begin{aligned} C &= \frac{\Pi}{R T} = \frac{0.248 \text{ Pa}}{8.314 \text{ Pa} \cdot 10^3 \text{ L} \cdot 298 \text{ K}} \\ &\approx 1.00 \times 10^{-4} \text{ mol/L} \end{aligned}$$

$\frac{\Pi}{R T}$   
Knots

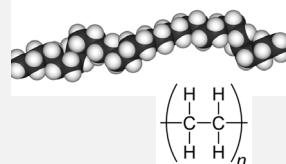


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$$1.00 \times 10^{-4} \text{ mol/L}$$



### Osmotic pressure $\Pi = i c R T$

1.40 g of polyethylene ( $i = 1$ ) dissolved in 100. mL of benzene generates an osmotic pressure of 0.248 kPa at 25 °C. Calculate the molar mass of the polyethylene.

1. Calculate the concentration...

$$1.00 \times 10^{-4} \text{ mol/L}$$

2. Calculate the moles...

$$\begin{aligned} &\frac{1.00 \times 10^{-4} \text{ mol}}{\text{L}} * \frac{100 \text{ mL} * 1 \text{ L}}{1000 \text{ mL}} \\ &= 1.00 \times 10^{-5} \text{ mol} \end{aligned}$$

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**Osmotic pressure  $\Pi = i c R T$** 

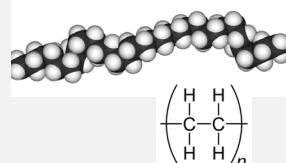
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1. Calculate the concentration...

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2. Calculate the moles...

$$1.00 \times 10^{-5} \text{ mol}$$

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**Osmotic pressure  $\Pi = i c R T$** 

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1. Calculate the concentration...

$$1.00 \times 10^{-4} \text{ mol/L}$$

2. Calculate the moles...

$$10^{-5} \text{ mol}$$

3. Calculate the molar mass...

$$\frac{1.40 \text{ g}}{1.00 \times 10^{-5} \text{ mol}} = 1.40 \times 10^5 \text{ g/mol}$$

How many  $M$ ?

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**Osmotic pressure  $\Pi = i c R T$** 

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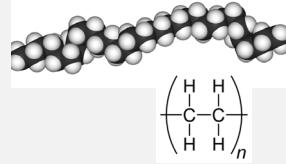
$$1.00 \times 10^{-4} \text{ mol/L}$$

2. Calculate the moles...

$$10^{-5} \text{ mol}$$

3. Calculate the molar mass...

$$1.40 \times 10^{+5} \text{ g/mol}$$

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31