

Lecture 22 CH102 A2 (MWF 11:15 am) Spring 2019 Copyright © 2019 Dan Dill dan@bu.edu

[TP] At 25 °C, 0.10 mol each of a weak acid HA, its conjugate base A⁻, and OH⁻ are combined in 1.0 L of water. The pH of the solution is ...

25% 1. < 7
 25% 2. = 7
 25% 3. > 7
 25% 4. Further information needed

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0 of 0

1

Lecture 22 CH102 A2 (MWF 11:15 am)
 Friday, March 22, 2019

- Postscript on titration of strong acid with strong base
- Buffers: [H₃O⁺] when different amounts of “not enough” base added
- Practice: Too little, just enough, too much?

Next lecture: Ch15: Five kinds of solubility equilibria problems; Practice with solubility equilibria.

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Strong acid titration: “not enough” base

Add 0.006 mol of OH⁻ to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.004 mol HA and 0.006 mol A⁻.

Step 2

	[HA]	[H ₃ O ⁺]	[A ⁻]	Q
Initial	0.004/V	1×10^{-7}	0.006/V	$\ll K_a$
Change				
Equilibrium				

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7

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Strong acid titration: “not enough” base

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Step 1 results in 0.004 mol HA and 0.006 mol A⁻.

Step 2

	[HA]	[H ₃ O ⁺]	[A ⁻]	Q
Initial	0.004/V	1×10^{-7}	0.006/V	$\ll K_a$
Change	$\approx -0.004/V$	$\approx +0.004/V$	$\approx +0.004/V$	
Equilibrium				

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8

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Strong acid titration: “not enough” base

Add 0.006 mol of OH^- to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.004 mol HA and 0.006 mol A^- .

Step 2

	[HA]	$[\text{H}_3\text{O}^+]$	$[\text{A}^-]$	Q
Initial	0.004/V	1×10^{-7}	0.006/V	$\ll K_a$
Change	$\approx -0.004/V$	$\approx +0.004/V$	$\approx +0.004/V$	
Equilibrium	≈ 0	$\approx 0.004/V$	$\approx 0.010/V$	$\approx K_a$

$[\text{H}_3\text{O}^+] = 4.0 \times 10^{-3}$ and pH = 2.4



9

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Strong acid titration: “just enough” base

Add 0.010 mol of OH^- to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.000 mol HA and 0.010 mol A^- .

Step 2, since $K_b = K_w/K_a \ll K_w$...

	$[\text{A}^-]$	[HA]	$[\text{OH}^-]$	Q
Initial	0.010/V	0	1×10^{-7}	$0 \ll K_b$
Change				
Equilibrium				



10

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Strong acid titration: “just enough” base

Add 0.010 mol of OH^- to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.000 mol HA and 0.010 mol A^- .

Step 2, since $K_b = K_w/K_a \ll K_w$...

	$[\text{A}^-]$	[HA]	$[\text{OH}^-]$	Q
Initial	0.010/V	0	1×10^{-7}	$0 \ll K_b$
Change	$-x$	$+x$	$+x$	
Equilibrium				



11

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Strong acid titration: “just enough” base

Add 0.010 mol of OH^- to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.000 mol HA and 0.010 mol A^- .

Step 2, since $K_b = K_w/K_a \ll K_w$...

	$[\text{A}^-]$	[HA]	$[\text{OH}^-]$	Q
Initial	0.010/V	0	1×10^{-7}	$0 \ll K_b$
Change	$-x$	$+x$	$+x$	
Equilibrium	$\approx 0.010/V$	x	$\approx 1 \times 10^{-7}$	$\approx K_b$

$[\text{H}_3\text{O}^+] = [\text{OH}^-] = 1.0 \times 10^{-7}$ and pH = 7.0



12

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Strong acid titration: “too much” base

Add 0.011 mol of OH^- to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.000 mol HA, 0.001 mol OH^- , and 0.010 mol A^- .

Step 2, since $K_b = K_w/K_a \ll K_w$...

	$[\text{A}^-]$	$[\text{HA}]$	$[\text{OH}^-]$	Q
Initial	0.010/V	0	0.001/V	$0 \ll K_b$
Change				
Equilibrium				

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13

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Strong acid titration: “too much” base

Add 0.011 mol of OH^- to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.000 mol HA, 0.001 mol OH^- , and 0.010 mol A^- .

Step 2, since $K_b = K_w/K_a \ll K_w$...

	$[\text{A}^-]$	$[\text{HA}]$	$[\text{OH}^-]$	Q
Initial	0.010/V	0	0.001/V	$0 \ll K_b$
Change	-x	+x	+x	
Equilibrium				

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14

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Strong acid titration: “too much” base

Add 0.011 mol of OH^- to 1.0 L of 0.01 M HA, $K_a = 1.0 \times 10^{+5}$, at 25 °C, assuming no volume change.

Step 1 results in 0.000 mol HA, 0.001 mol OH^- , and 0.010 mol A^- .

Step 2, since $K_b = K_w/K_a \ll K_w$...

	$[\text{A}^-]$	$[\text{HA}]$	$[\text{OH}^-]$	Q
Initial	0.010/V	0	0.001/V	$0 \ll K_b$
Change	-x	+x	+x	
Equilibrium	$\approx 0.010/V$	x	$\approx 0.001/V$	$\approx K_b$

$[\text{H}_3\text{O}^+] = \frac{K_w}{0.001/V} = 1.0 \times 10^{-11}$ and pH = 11.0 (excess base)

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15

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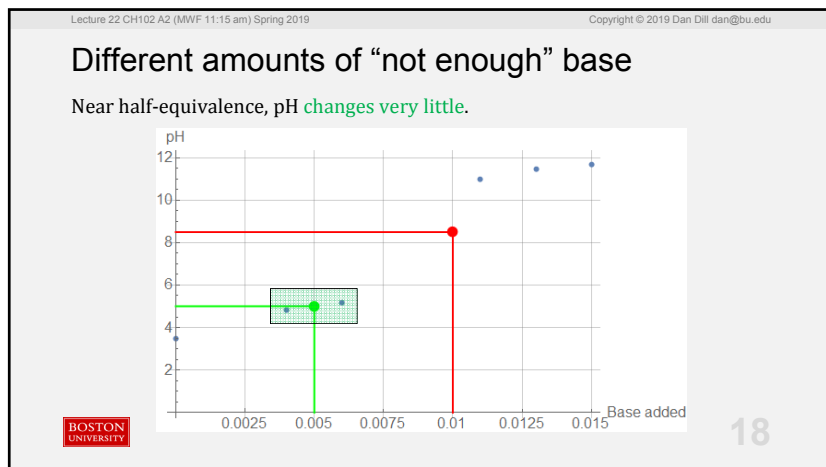
[Quiz] At 25 °C, titration of 1.0 L of 0.010 M weak acid with OH^- has pH = 8.5 at the equivalence point, whereas titration of 1.0 L of 0.010 M strong acid with OH^- has pH = 7.0 at the equivalence point. This means that, compared to the moles of OH^- needed to reach equivalence in the weak acid titration, the moles of OH^- needed in the strong acid titration must be ...

25% 1. less
 25% 2. the same
 25% 3. more
 25% 4. Further information needed

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0 of 0

16



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Different amounts of “not enough” base

At 25 °C, the pH of a 1.0 L solution of $c_a = c_b = 1.00 \text{ M}$, $K_a = 1 \times 10^{-5}$ is ...
 $\text{pH} = 5.00$

Add 100. mL of 0.100 M NaOH ...
 $\text{HA} \rightarrow 1.00 \text{ mol} - 0.010 \text{ mol} = 0.99 \text{ mol}$
 $\text{A}^- \rightarrow 1.00 \text{ mol} + 0.010 \text{ mol} = 1.01 \text{ mol}$
 $\downarrow \text{HA}(aq) + \text{OH}^-(aq) \rightarrow \text{H}_2\text{O}(l) + \uparrow \text{A}^-(aq)$

The pH of a 1.0 L solution of $c_a = 0.99 \text{ mol}/1.10 \text{ L}$, $c_b = 1.01 \text{ mol}/1.10 \text{ L}$ is ...
 $c_a/c_b = 1.00 \rightarrow 0.99/1.01$, $\text{pH} \rightarrow 5.01$ (tiny change!)

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19

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Different amounts of “not enough” base

At 25 °C, the pH of a 1.0 L solution **pure water**, $K_a = 1 \times 10^{-14}$ is ...
 $\text{pH} = 7.00$

Add 100. mL of 0.100 M NaOH ...
 $[\text{OH}^-] = 0.010 \text{ mol}/1.10 \text{ L} = 0.0091$
 $\text{pOH} = 2.04$, $\text{pH} = 11.96$ (huge change!)

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20

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Different amounts of “not enough” base

At 25 °C, the pH of a 1.0 L solution of $c_a = c_b = 1.00 \text{ M}$, $K_a = 1 \times 10^{-5}$ is ...
 $\text{pH} = 5.00$

Add 100. mL of 0.100 M HCl ...
 $\text{HA} \rightarrow 1.00 \text{ mol} + 0.010 \text{ mol} = 1.01 \text{ mol}$
 $\text{A}^- \rightarrow 1.00 \text{ mol} - 0.010 \text{ mol} = 0.99 \text{ mol}$
 $\text{HCl}(aq) + \downarrow \text{A}^-(aq) \rightarrow \uparrow \text{HA}(aq) + \text{Cl}^-(aq)$

The pH of a 1.0 L solution of $c_a = 1.01 \text{ mol}/1.10 \text{ L}$, $c_b = 0.99 \text{ mol}/1.10 \text{ L}$...
 $c_a/c_b = 1.00 \rightarrow 1.01/0.99$, $\text{pH} \rightarrow 4.99$ (tiny change!)

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21

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Different amounts of “not enough” base

At 25 °C, the pH of a 1.0 L solution **pure water**, $K_a = 1 \times 10^{-14}$ is ...
pH = 7.00

Add 100. mL of 0.100 M HCl ...

$$[\text{H}_3\text{O}^+] = 0.010 \text{ mol}/1.10 \text{ L} = 0.0091$$

pH = 2.04 (huge change!)



22

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Buffers

Mixtures of a weak acid and its conjugate base (or weak base and its conjugate acid) exhibit the special property that they **resist changes to pH**.

For this reason such mixtures are known as **buffers**.



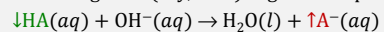
23

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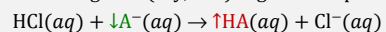
Buffers resist change in pH

Added strong base (say, OH^-) is gobbled up ...



c_a lowered, c_b raised, c_a/c_b lowered

Added strong acid (say, HCl) is gobbled up ...



c_b lowered, c_a raised, c_a/c_b raised

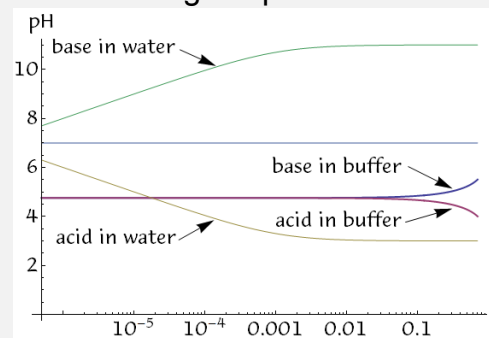


24

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Buffers resist change in pH



25

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Too little, just enough, too much?

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27

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[TP] At 25 °C, 0.10 mol each of a strong acid and OH⁻ are combined in 1.0 L of water. The pH of the solution is ...

0% 1. < 7
0% 2. = 7
0% 3. > 7
0% 4. Further information needed

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28

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[TP] At 25 °C, 0.10 mol each of a weak acid HA, its conjugate base A⁻, and OH⁻ are combined in 1.0 L of water. The pH of the solution is ...

1. < 7
2. = 7
3. > 7
4. Further information needed

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0 of 0

29

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[Quiz] At 25 °C, 0.10 mol each of a weak acid HA and a strong acid HB, and 0.20 mol of OH⁻ are combined in 1.0 L of water. The pH of the solution is ...

0% 1. < 7
0% 2. = 7
0% 3. > 7
0% 4. Further information needed

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30