

Lecture 17 CH102 A2 (MWF 11:15 am) Spring 2019 Copyright © 2019 Dan Dill dan@bu.edu

[TP] At 25 °C the  $pK_a = -\log(K_a)$  of a certain acid is 4.17. A solution is made by combining 0.314 mol of HA and 0.314 mol of NaA in a total volume of 716 mL. What is the pH of the resulting solution?

14% 1. 1.78  
 14% 2. 2.19  
 14% 3. 3.14  
 14% 4. 4.17  
 14% 5. 5.78  
 14% 6. 7.00  
 14% 7. Something else

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 Monday, March 4, 2019

- $pK_a = -\log(K_a)$
- Titration: What happens when some  $OH^-$  is added to an acid

Next:  $[H_3O^+]$  when “too little” base added;  $[H_3O^+]$  when “too much” base added; Practice: Too little, just enough, too much?;  $[H_3O^+]$  when different amounts of “not enough” base added

Review: Logarithm Tutorial, <https://goo.gl/RtLg9X>

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$pK_a = -\log(K_a)$

Since  $K_a = [H_3O^+][A^-] / [HA]$ , we can express the hydronium ion concentration as  $[H_3O^+] = K_a [HA] / [A^-]$

From this we can express pH as

$$pH = -\log(K_a) + \log([A^-] / [HA])$$

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$pK_a = -\log(K_a)$

Since  $K_a = [H_3O^+][A^-] / [HA]$ , we can express the hydronium ion concentration as  $[H_3O^+] = K_a [HA] / [A^-]$

From this we can express pH as

$$pH = -\log(K_a) + \log([A^-] / [HA])$$

$$= pK_a + \log([A^-] / [HA])$$

where  $pK_a$  is defined as  $pK_a = -\log(K_a)$

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$$\text{p}K_a = -\log(K_a)$$

An important application of

$$\text{pH} = \text{p}K_a + \log\left(\frac{[\text{A}^-]}{[\text{HA}]}\right)$$

is that ...

if **equal amounts** of weak acid and its conjugate base are combined, then

$$\text{pH} = \text{p}K_a + \log(1) = \text{p}K_a$$

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**[TP]** At 25 °C the  $\text{p}K_a = -\log(K_a)$  of a certain acid is 4.17. A solution is made by combining 0.314 mol of HA and 0.314 mol of NaA in a total volume of 716 mL. What is the pH of the resulting solution?

0% 1. 1.78  
 0% 2. 2.19  
 0% 3. 3.14  
 0% 4. 4.17  
 0% 5. 5.78  
 0% 6. 7.00  
 0% 7. Something else

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$$\text{p}K_a = -\log(K_a)$$

Since  $\text{pH} = \text{p}K_a + \log\left(\frac{[\text{A}^-]}{[\text{HA}]}\right)$ , when **equal amounts** of acid and its conjugate base are combined in solution (an **equimolar solution**), the pH will be  $\text{p}K_a$ .

This means that a way to measure  $K_a$  is to make an **equimolar solution** and measure its pH, for then

$$K_a = 10^{-\text{pH}}$$

Very useful to remember!

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Titration: What happens when **some**  $\text{OH}^-$  is added to an acid?

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**[Quiz]** An acid has  $K_a = 1.0 \times 10^{-7}$  at 25 °C. The hydronium concentration of a  $c_a = 0.40$  M solution of this acid solution is  $[H_3O^+] = 2.0 \times 10^{-4}$ . After adding **some** 0.20 M  $OH^-$ ,  $[H_3O^+]$  **must be** ...

0% 1. smaller than  $2.0 \times 10^{-4}$   
 0% 2. less than  $1.0 \times 10^{-7}$  (basic)  
 0% 3. equal to  $1.0 \times 10^{-7}$  (neutral)  
 0% 4. greater than  $1.0 \times 10^{-7}$  (acidic)  
 0% 5. More information needed

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### Add "some" $OH^-$ to an acid

When **some**  $OH^-$  solution is added to an HA solution, **some** HA will be converted to conjugate base,  $A^-$ .

Therefore,  $[HA]$  **will be less**, the equilibrium

$$HA(aq) + H_2O(l) \rightleftharpoons H_3O^+(aq) + A^-(aq)$$

will **shift toward reactants**, and so, by Le Chatelier,  $[H_3O^+]$  must **decrease**.

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### Add "some" $OH^-$ to an acid

When **some**  $OH^-$  solution is added to an HA solution, **some** HA will be converted to conjugate base  $A^-$ , and so  $[H_3O^+]$  must **decrease**.

There are **two steps** to find the new value of  $[H_3O^+]$ .

**Step 1:** Assume HA and the added  $OH^-$  react 100%, as a **limiting reagent** problem.

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### Add "some" $OH^-$ to an acid

When **some**  $OH^-$  solution is added to an HA solution, **some** HA will be converted to conjugate base  $A^-$ , and so  $[H_3O^+]$  must **decrease**.

There are **two steps** to find the new value of  $[H_3O^+]$ .

**Step 1:** Assume HA and the added  $OH^-$  react 100%, as a **limiting reagent** problem.

**Step 2:** Use the results of step 1 to re-solve the equilibrium.

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## Add “some” OH<sup>-</sup> to an acid

When **some** OH<sup>-</sup> solution is added to an HA solution, **some** HA will be converted to conjugate base A<sup>-</sup>, and so [H<sub>3</sub>O<sup>+</sup>] must **decrease**.

There are **two steps** to find the new value of [H<sub>3</sub>O<sup>+</sup>].

**Step 1:** Assume HA and the added OH<sup>-</sup> react 100%, as a **limiting reagent** problem.

**Step 2:** Use the results of step 1 to re-solve the equilibrium.

To begin, let's learn about the **results of step 1**.



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## Step 1: HA + OH<sup>-</sup> limiting reagent reaction

There are three possible results of **step 1**.

“**Too little**” base:

If fewer moles of OH<sup>-</sup> are added than the moles of acid present, then **only some** of the acid HA will be converted to conjugate base A<sup>-</sup>, consuming **all** of the added OH<sup>-</sup>.



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## Step 1: HA + OH<sup>-</sup> limiting reagent reaction

There are three possible results of **step 1**.

“**Just enough**” base:

If the moles of OH<sup>-</sup> added is the same as the moles of acid present, then **all** of the acid HA will be converted to conjugate base A<sup>-</sup>, consuming **all** of the added OH<sup>-</sup>.



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## Step 1: HA + OH<sup>-</sup> limiting reagent reaction

There are three possible results of **step 1**.

“**Too much**” base:

If the moles of OH<sup>-</sup> added is more than the moles of acid present, then **all** of the acid HA will be converted to conjugate base A<sup>-</sup> and **unused OH<sup>-</sup>** will be **left over**.



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### Step 1: HA + OH<sup>-</sup> limiting reagent reaction

There are three possible results of **step 1**.

	HA(aq)	OH <sup>-</sup> (aq)	A <sup>-</sup> (aq)
"Too little"			
"Just enough"			
"Too much"			

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### Step 1: HA + OH<sup>-</sup> limiting reagent reaction

There are three possible results of **step 1**.

	HA(aq)	OH <sup>-</sup> (aq)	A <sup>-</sup> (aq)
"Too little"	Some	None	Some
"Just enough"	None	None	Some
"Too much"	None	Some	Some

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[TP]  $V_b = 100. \text{ mL}$  of  $c_b = 0.40 \text{ M}$  of OH<sup>-</sup> is combined with  $V_a = 100. \text{ mL}$  of  $c_a = 0.40 \text{ M}$  of HA. The result is ...

0% 1. "too little" OH<sup>-</sup>  
 0% 2. "just enough" OH<sup>-</sup>  
 0% 3. "too much" OH<sup>-</sup>  
 0% 4. Further information needed

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[Quiz]  $V_b = 100. \text{ mL}$  of  $c_b = 0.20 \text{ M}$  of OH<sup>-</sup> is combined with  $V_a = 100. \text{ mL}$  of  $c_a = 0.40 \text{ M}$  of HA. The result is ...

0% 1. "too little" OH<sup>-</sup>  
 0% 2. "just enough" OH<sup>-</sup>  
 0% 3. "too much" OH<sup>-</sup>  
 0% 4. Further information needed

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## Add “some” OH<sup>-</sup> to an acid

There are two steps to find the new value of [H<sub>3</sub>O<sup>+</sup>].

Step 1: Assume the acid HA and the added OH<sup>-</sup> react 100%, as a **limiting reagent problem** (ignoring equilibrium!).

Step 2: Based on whether we have added “too little”, “just enough”, or “too much” OH<sup>-</sup>, we use the results of step 1 to **re-calculate the equilibrium** concentration of [H<sub>3</sub>O<sup>+</sup>].



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