

Lecture 6 CH102 A2 (MWF 11:15 am) Spring 2019 Copyright © 2019 Dan Dill dan@bu.edu

[TP] The rms speed, u_{rms} , of O_2 at 25 °C is about ...
("Use units, Luke!" $R = 8.314 \frac{\text{J}}{\text{K mol}} = 8.314 \frac{\text{kg m}^2/\text{s}^2}{\text{K mol}}$)

25% 1. 250 m/s
25% 2. 500 m/s
25% 3. 750 m/s
25% 4. 1000 m/s

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Response Counter 10 1

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Monday, February 4, 2019

- Molecular speeds and their distribution, CDF <https://goo.gl/VkRrsg>

Next: Real gases: Effect of molecular attraction; Real gases: Effect of molecular size; van der Waals equation; Phase diagrams

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Calculation of molecular speeds

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Response Counter 10 6

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Calculate rms speed of O₂ at 25 °C

$$u_{\text{avg}}^2 = \frac{3RT}{M}$$

$$u_{\text{rms}} = \sqrt{u_{\text{avg}}^2} = \sqrt{\frac{3RT}{M}}$$

$$R = 8.314 \frac{\text{J}}{\text{K mol}} = 8.314 \frac{\text{kg m}^2/\text{s}^2}{\text{K mol}}$$

Answer: 482 m/s $\approx$ 500 m/sBOSTON
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Distribution of molecular speeds

Distribution of speeds is a plot of the number of particles (y axis) at each speed (x axis).

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Distribution of molecular speeds

Say we 20,000 particles, all with the same speed $u = 500$ m/s.

Make a sketch of the corresponding distribution of speeds.

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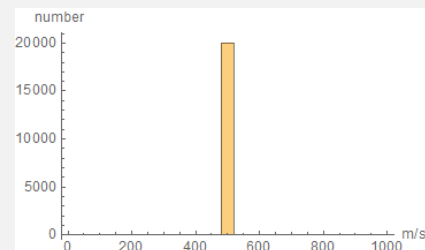
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Distribution of molecular speeds

We have said that collisions between gas particles results in the particles having **different speeds**.

Make a sketch of a possible distribution of just three speeds, 300, 500, and 700 m/s, of the 20,000 particles.



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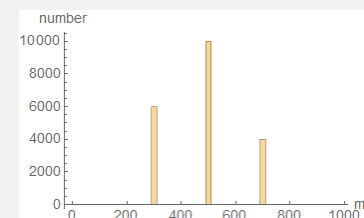
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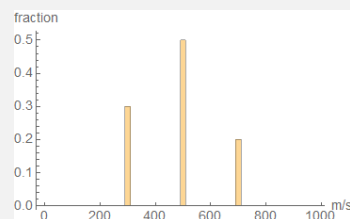
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Distribution of molecular speeds

We have said that collisions between gas particles results in the particles having **different speeds**.

It is convenient to express the distribution in terms of **fractional number of particles** rather than number of particles.



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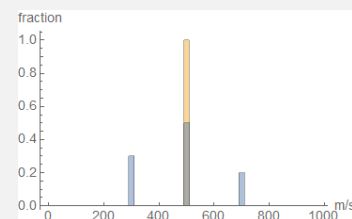
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15

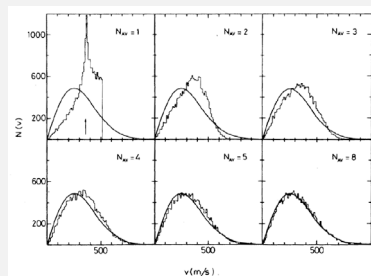
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Distribution of molecular speeds

Here is what happens to the speeds of 20,000 particles, all initially at the same speed, after they each have undergone successive numbers of collisions.

Bonomo & Riggi,
Am. J. Phys., Vol 52, p 54 (1984)
<http://dx.doi.org/10.1119/1.13809>

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Distribution of molecular speeds

At 300 K, the rms speed of O_2 is $u_{rms} = 500$ m/s.

Sketch the Maxwell-Boltzmann distribution of speeds of O_2 at 300 K, from 0 m/s to 4000 m/s, marking the position of u_{rms} on the x axis.

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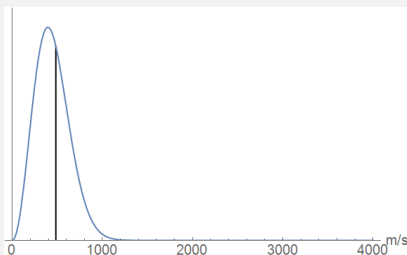
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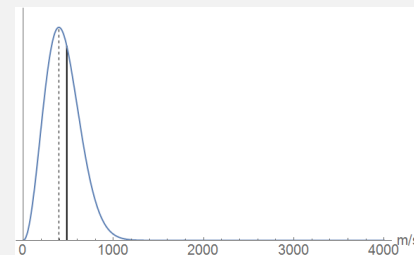
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Distribution of molecular speeds

The rms speed, u_{rms} , is slightly **higher** than the **most probable speed**, u_{mp} , because of the **exponential tail** extending to very high speeds.

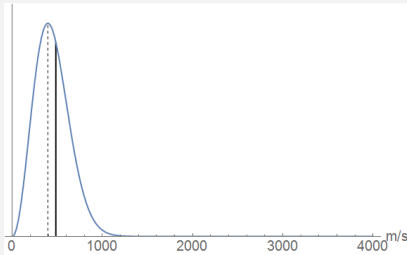
$$u_{mp} = \sqrt{2/3} u_{rms} \approx 0.82 u_{rms}$$

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u_{rms} versus temperature

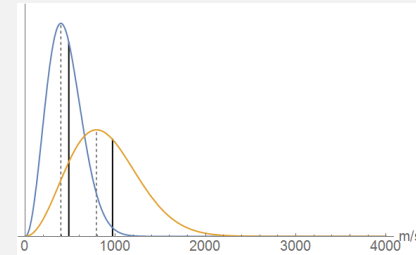
The rms speed of O_2 at 300 K is 500 m/s and the rms speed of O_2 at 1200 K is 1000 m/s. Sketch the distribution of speeds for O_2 at these two temperatures on the same axes, marking the position of the two rms speeds on the x axis.



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 u_{rms} versus temperature

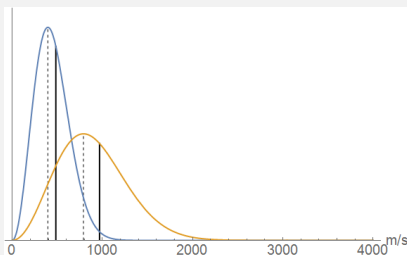
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 u_{rms} versus temperature

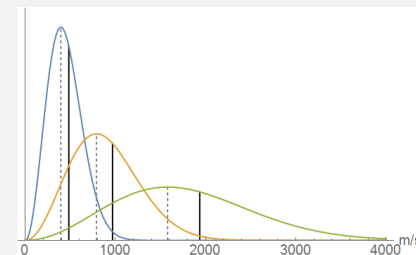
Add to your sketch the distribution of speeds of H_2 at 300 K.



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 u_{rms} versus temperature

Add to your sketch the distribution of speeds of H_2 at 300 K.



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