

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

[TP] The wavelength of the electron wave in the ground state of H atom is about the size of the atom. In what region of the spectrum is light of similar wavelength?

- 0% 1. Radio
- 0% 2. Microwave
- 0% 3. Infrared
- 0% 4. Visible
- 0% 5. Ultraviolet
- 0% 6. X-ray
- 0% 7. Gamma ray

1

BOSTON UNIVERSITY

Lecture 28 CH101 A1 (MWF 9:05 am)

Monday, November 12, 2018

For today ...

- Electron waves and quantization (de Broglie)
- Hydrogen atom electron clouds

Next lecture: Energy of hydrogen atom electron clouds ; Revisit: How light and matter exchange energy ; H atom energy diagrams: Balmer's formula ; H atom energy diagrams: Beyond Balmer's formula

Prepare: Hydrogen atom family album, <https://goo.gl/XPkcxv>

BOSTON UNIVERSITY

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Electron waves and quantization (de Broglie)

4

BOSTON UNIVERSITY

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Electron waves and quantization (de Broglie)

Only certain colors = quantization

Hydrogen Absorption Spectra

Intensity ↑

Wavelength (nm) →

Figure 4.8b
© 2009 W. H. Freeman and Company

5

BOSTON UNIVERSITY

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

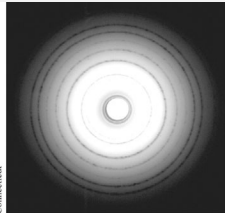
Electron clouds are built from waves

By analogy to the energy-frequency relation for light,

$$E_{\text{photon}} = h\nu_{\text{light}}$$

De Broglie **guessed** that electron clouds are **built from waves**.

This guess was confirmed by **diffraction of electrons** by the lattice of ions in a salt crystal.



R.K. Bohm, Department of Chemistry, University of Connecticut

BOSTON UNIVERSITY

8

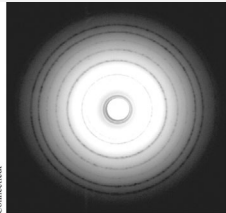
Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Electron clouds are built from waves

The electron wave wavelength

$$\lambda_{\text{electron}} = h/p_{\text{electron}}$$

is **inversely proportional** to electron **momentum**

$$p_{\text{electron}} = mu$$


R.K. Bohm, Department of Chemistry, University of Connecticut

BOSTON UNIVERSITY

9

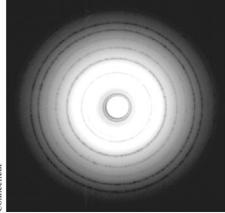
Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Electron clouds are built from waves

Show that the units of

$$\lambda_{\text{electron}} = \frac{h}{p} = \frac{h}{mu}$$

are correct.

$$\lambda_{\text{electron}} \propto \frac{\text{J s}}{\text{kg} \frac{\text{m}}{\text{s}}} = \frac{\text{kg} \frac{\text{m}^2}{\text{s}^2} \text{ s}}{\text{kg} \frac{\text{m}}{\text{s}}} = \text{m}$$


R.K. Bohm, Department of Chemistry, University of Connecticut

BOSTON UNIVERSITY

10

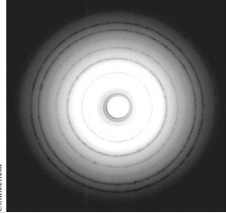
Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Electron clouds are built from waves

One crucial thing to understand:

Electron waves are **not anything physical** waving in space.

Rather, they are **abstract mathematical waves**.



R.K. Bohm, Department of Chemistry, University of Connecticut

BOSTON UNIVERSITY

11

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

[TP] The wavelength of the electron wave in the ground state of H atom is about the size of the atom. In what region of the spectrum is light of similar wavelength?

- 0% 1. Radio
- 0% 2. Microwave
- 0% 3. Infrared
- 0% 4. Visible
- 0% 5. Ultraviolet
- 0% 6. X-ray
- 0% 7. Gamma ray

12

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Electron “waves”

We can illustrate electron waves and their properties with wave on a spring.

14

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Electron “waves”

Big idea 1:

Integer number of loops, $\lambda/2$, must “fit” in the atom

15

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Integer number of loops fit in the atom

- 1 loop
- 2 loops
- 3 loops

16

Electron "waves"

Big idea 2:
More loops, ...
more energy



17

Electron "waves"

We have illustrated electron waves and their properties with a spring.

What corresponds to the spring?

Space is permeated by what is called the **quantum field**.

The **spring** represents the **quantum field**.

Excitations of the quantum field (one loop, two loops, etc.) are **electron waves**.



19

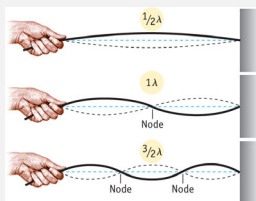
Hydrogen atom electron clouds

1D electron cloud:

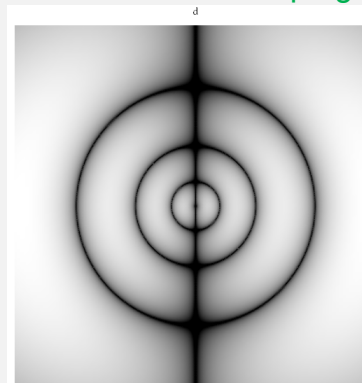
1D example of a standing wave

Major Lesson: lowest energy has 1 loop (0 nodes)

Major Lesson: more loops, more energy



26

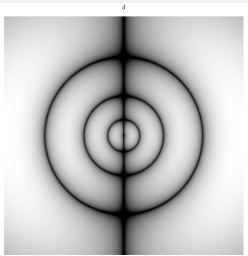
Extend to 3D electron cloud: <http://goo.gl/XPkcxv>

27

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Hydrogen atom family album: <http://goo.gl/XPkcxv>

1D electron cloud:
 1D example of a standing wave
 Major Lesson: lowest energy has 1 loop (0 nodes)
 Major Lesson: more loops, more energy



Extend to 3D electron cloud:
 Atoms are spheres!! (not wires)
 Two types of loops:
 radial
 angular (nodal planes)

BOSTON UNIVERSITY 28

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Clouds and probability

The density of an electron cloud is a measure of the **fraction of the electron** in that region.

For this reason, clouds are sometimes referred to in terms of **probability density**.

It is crucial to understand that **the cloud is the electron**, and **not a time exposure** of a point particle.

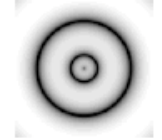
Probability density is due to **spatial extent** rather than **motion**.

BOSTON UNIVERSITY 29

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Radial loops

Concentric rings around nucleus
 (distance from the nucleus)



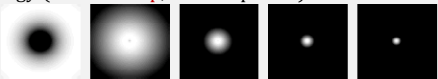
$j = \# \text{ radial loops}$

BOSTON UNIVERSITY 31

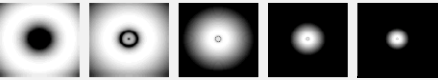
Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Radial loops only (known as "s")

Lowest Energy (1 radial loop, 0 nodal planes):



2nd Lowest Energy (2 radial loops, 0 nodal planes):



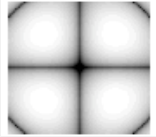
Etc.

BOSTON UNIVERSITY 32

Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Nodal planes

- Will look like planes (lines) of **zero probability**



$l = \#$ of nodal planes


BOSTON UNIVERSITY

33

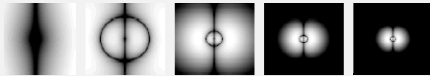
Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Radial + 1 nodal plane (known as "p")

Lowest Energy (1 radial loop, 1 nodal plane):



2nd Lowest Energy (2 radial loops, 1 nodal plane):



Etc.

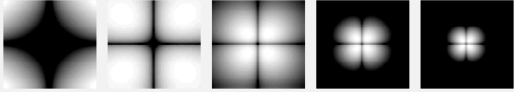
BOSTON UNIVERSITY

34

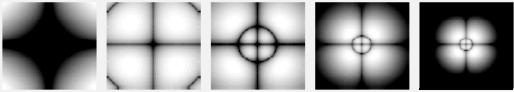
Lecture 28 CH101 A1 (MWF 9:05 am) Fall 2018 Copyright © 2018 Dan Dill dan@bu.edu

Radial + 2 nodal planes (known as "d")

Lowest Energy (1 radial loop, 2 nodal planes):



2nd Lowest Energy (2 radial loops, 2 nodal planes):



Etc.

BOSTON UNIVERSITY

35