



# From Compressed Sensing to Deep Learning: Tasks, Structures, and Models

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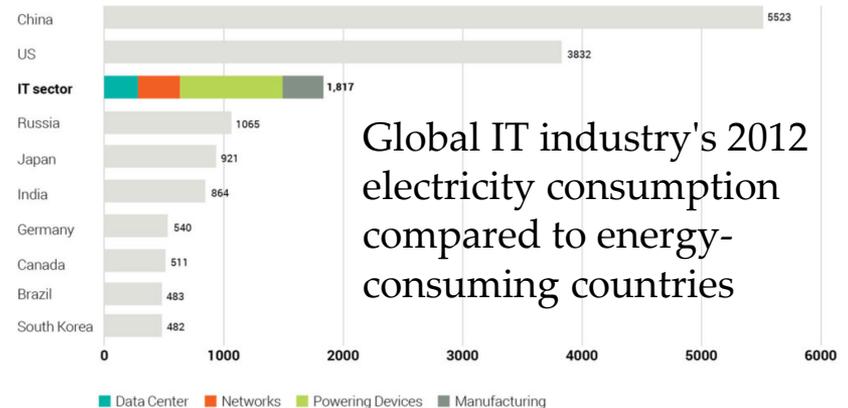
April 2021



# Data Abundance

Challenges of data proliferation in the digital era:

- > Power
- > Storage
- > Processing
- > Communicating



AI

$10^{21}$

Cisco: Mobile internet traffic will approach a zettabyte by 2022

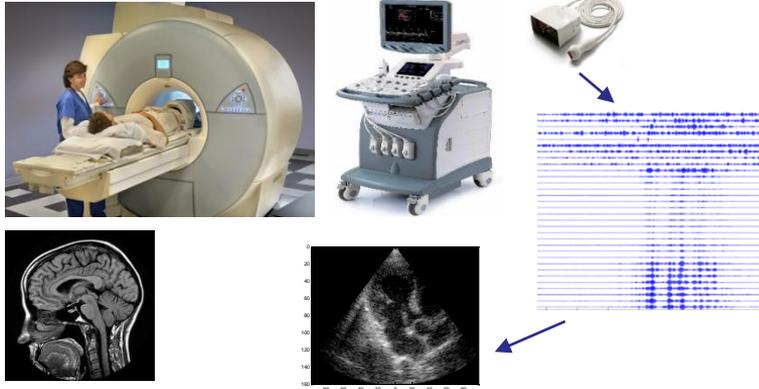
KYLE WIGGERS @KYLE\_L\_WIGGERS FEBRUARY 19, 2019 5:00 AM



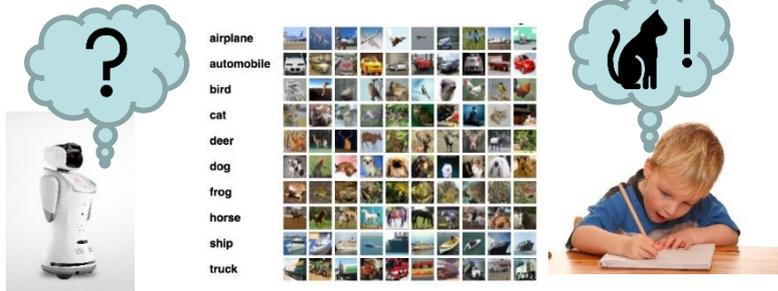
Do we really need so much data?

# Data Redundancy

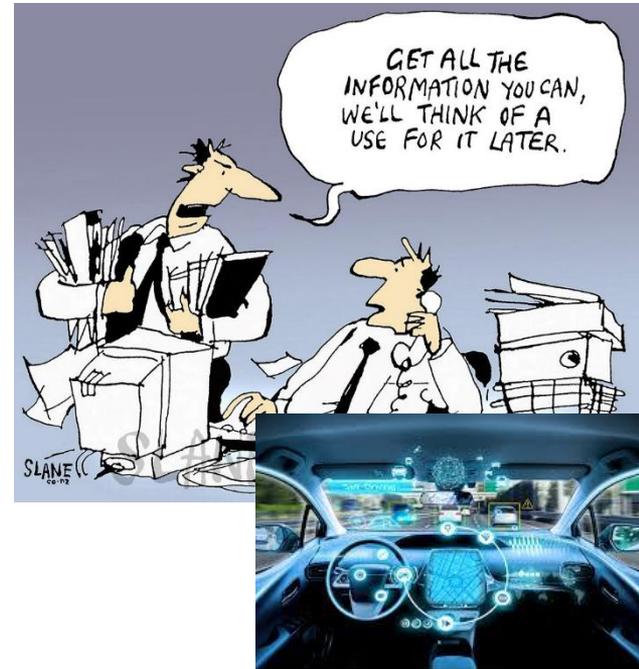
## Medical imaging



## Deep neural networks



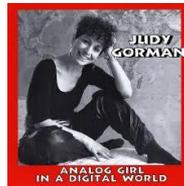
## Smart cities, autonomous cars



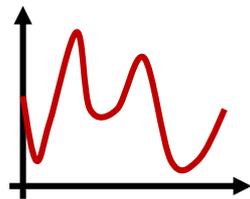
**Can we acquire only what we need?**

# “Analog Girl in a Digital World...”

Judy Gorman 99



## Analog world



$x(t)$

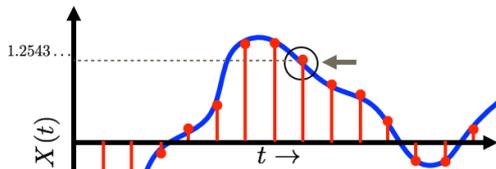
- > Music
- > Radar
- > Communication
- > Image...



## Sampling



Analog-to-Digital  
Convertor  
(ADC)



$$Y[n] = X(n/f_s)$$

$$f_s = \# \text{ samples/sec}$$

$$R = f_s \log_2(\# \text{ of levels}) \text{ (bit/sec)}$$

## Digital world



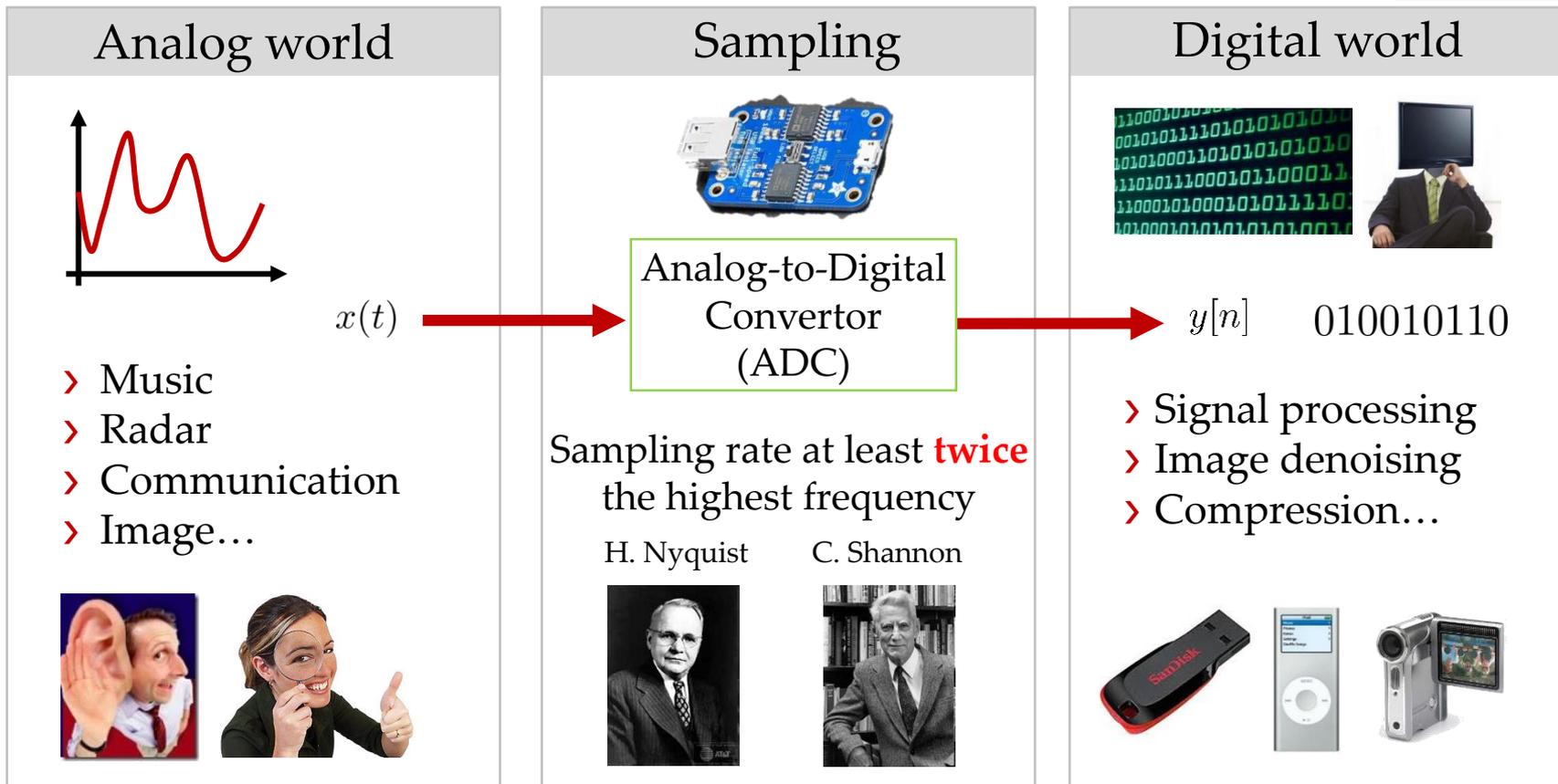
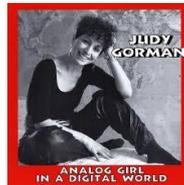
$y[n]$  010010110

- > Signal processing
- > Image denoising
- > Compression...

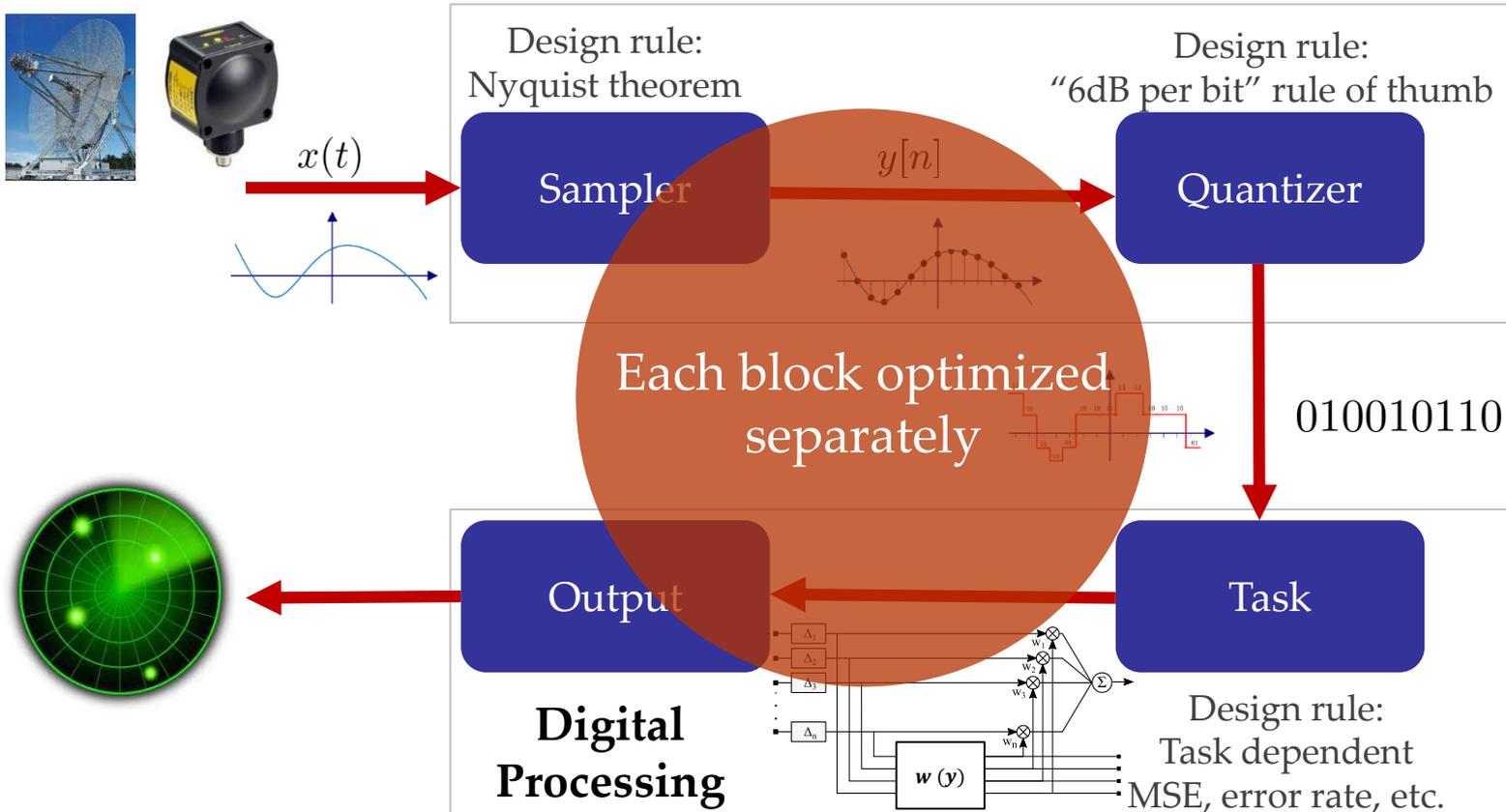


# “Analog Girl in a Digital World...”

Judy Gorman 99



# Standard Acquisition Systems



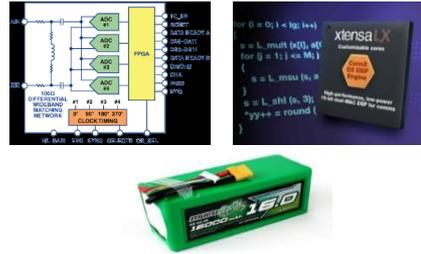
# Limitations of Standard Systems

Large Bandwidth

- High rate communications
- High resolution e.g. in radar and imaging

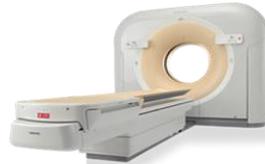


High rate samplers and quantizers



- Large and expensive hardware-intensive systems
- High-energy systems
- Large digital databases: difficult to process, store and transmit

In medical imaging, high rates often translate into long scanning times or **high radiation dosages**

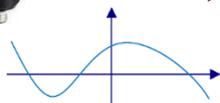


**ADCs, the front end of all digital devices, lead to hardware, data and power bottlenecks**

# Task-Based Structured Acquisition



$x(t)$



Sampler

$y[n]$

Quantizer

Joint Design:

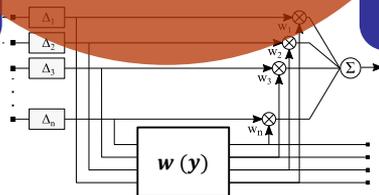
- Structure in input/system
- Output task

010010110

Output

Task

Digital  
Processing



Model based, efficient, and interpretable data driven methods!

# Advantages of Joint Design

Compact, portable devices with better imaging and detection quality

Joint radar and communication systems

Efficient wideband sensing

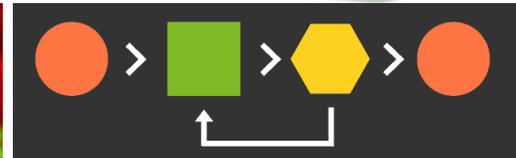
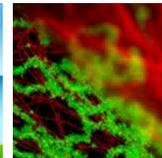
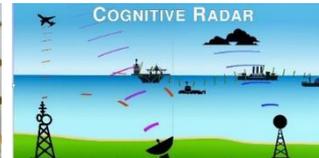
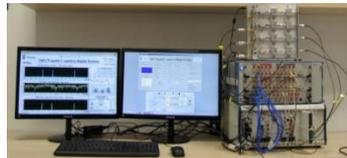
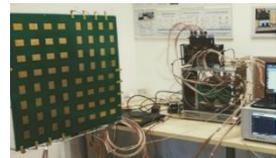
Compact, cheap and high resolution radar

Efficient massive MIMO systems

High performance  
Low-bit quantization

Super resolution microscopy and ultrasound

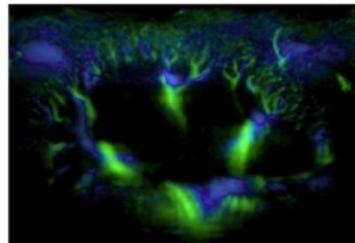
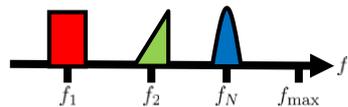
Interpretable, deep networks for communication, medical imaging, radar and more



# Talk Outline

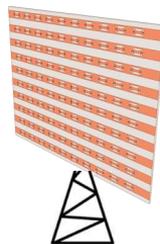
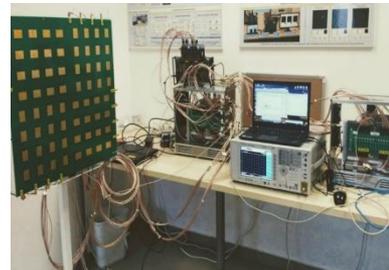
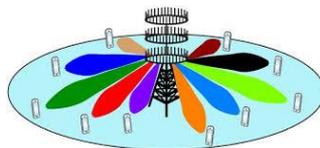
## ➤ Exploiting structure: From Sampling to Xampling

- Sub-Nyquist ultrasound and radar
- Wireless ultrasound

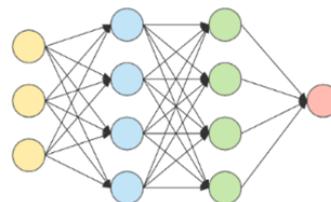


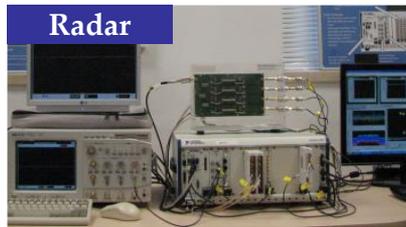
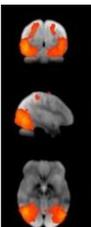
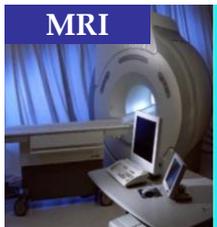
## ➤ Exploiting tasks: Task-based sampling

- Power spectrum estimation
  - Cognitive radio
  - Super-resolution microscopy and US
- Task-based quantization
  - Efficient massive MIMO systems
  - Federated learning
  - Metasurface multiantenna systems
  - Joint radar-communication systems



## ➤ Exploiting models: Model-based deep learning



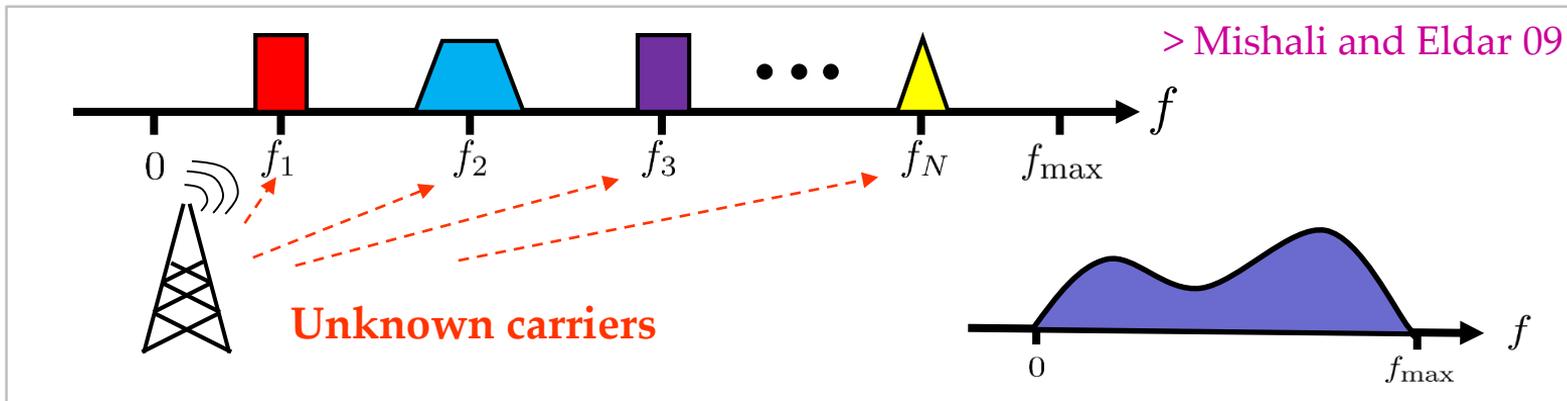


## Part 1:

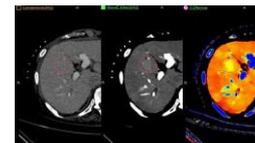
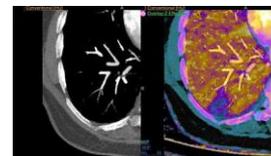
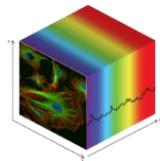
# From Sampling to Xampling

# Multiple Frequency Bands

## > Multiband Communication



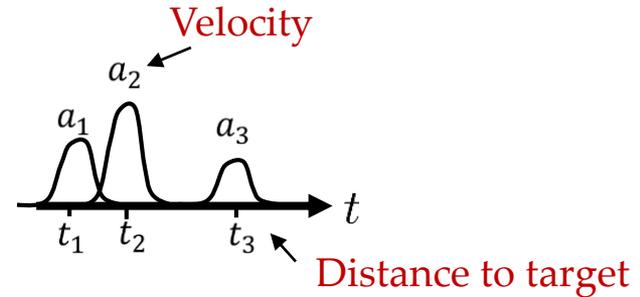
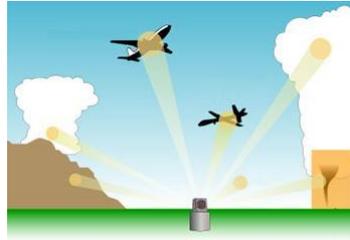
- Can be viewed as  $f_{\max}$  – bandlimited
  - But sampling at rate  $\geq 2f_{\max}$  is a waste of resources
  - For wideband applications Nyquist sampling may be infeasible
- > Multispectral imaging, multispectral CT



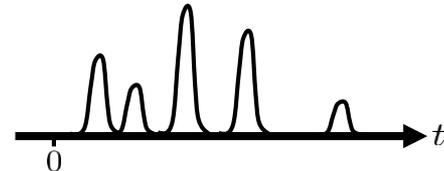
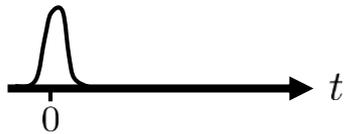
# Streams of Pulses

Radar:

> Vetterli et. al, 02



Ultrasound:

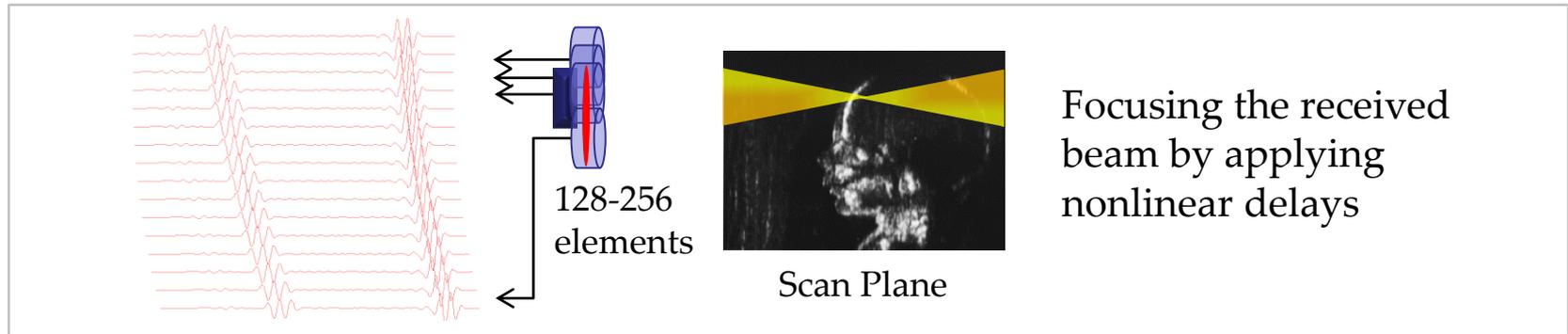


**A sampler that takes advantage of the pulses' structure can use fewer samples and lead to higher resolution**

# Compressed Beamforming

> Chernyakova and Eldar 13-15

- > SNR and resolution are increased by using an antenna array
- > Beamforming is performed by introducing appropriate time shifts to the received signals



$$\Phi(t; \theta) = \frac{1}{M} \sum_{m=1}^M \varphi_m \left( t - \frac{1}{2} \left( t - \sqrt{t^2 - 4(\delta_m/c)t \sin \theta + 4(\delta_m/c)^2} \right) \right)$$

**Requires high sampling and processing rates (lots of data...)**

One image trace needs 128 samplers @20M, beamforming to 150 points, total of  $6.3 \times 10^6$  sums/frame!

# Challenges

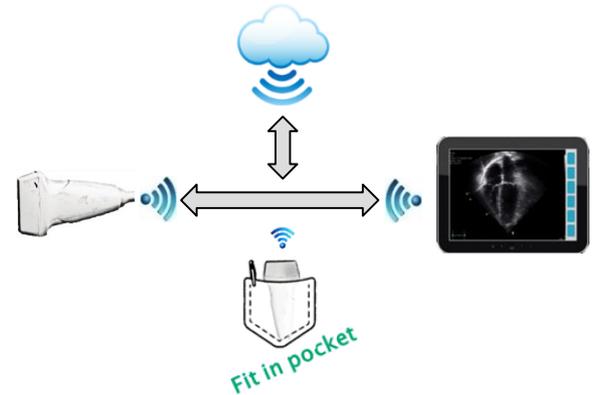
Can we...

- Reduce analog sampling rates of very noisy signals
- Perform nonlinear beamforming on sub-Nyquist samples, without interpolating to the high Nyquist-rate grid digitally



**Yes, use Compressed Beamforming!**

- Reduce US machine size at same resolution
- Increase frame rate
- Enable 3D imaging
- Enable remote wireless ultrasound

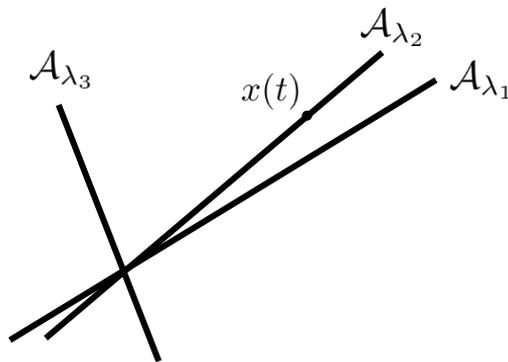
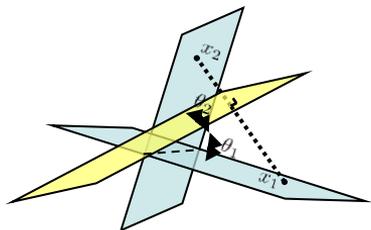


# Union of Subspaces

$$\mathcal{U} = \bigcup_{\lambda \in \Lambda} \mathcal{A}_\lambda$$

> Lu and Do 08, Mishali and Eldar 09

$x(t) \in \mathcal{A}_{\lambda^*} \rightarrow \lambda^*$  is unknown a-priori  
Each  $\mathcal{A}_\lambda$  has low dimension



- > Allows to keep low dimension in the problem model
- > Low dimension translates to low sampling rate

## Theorem

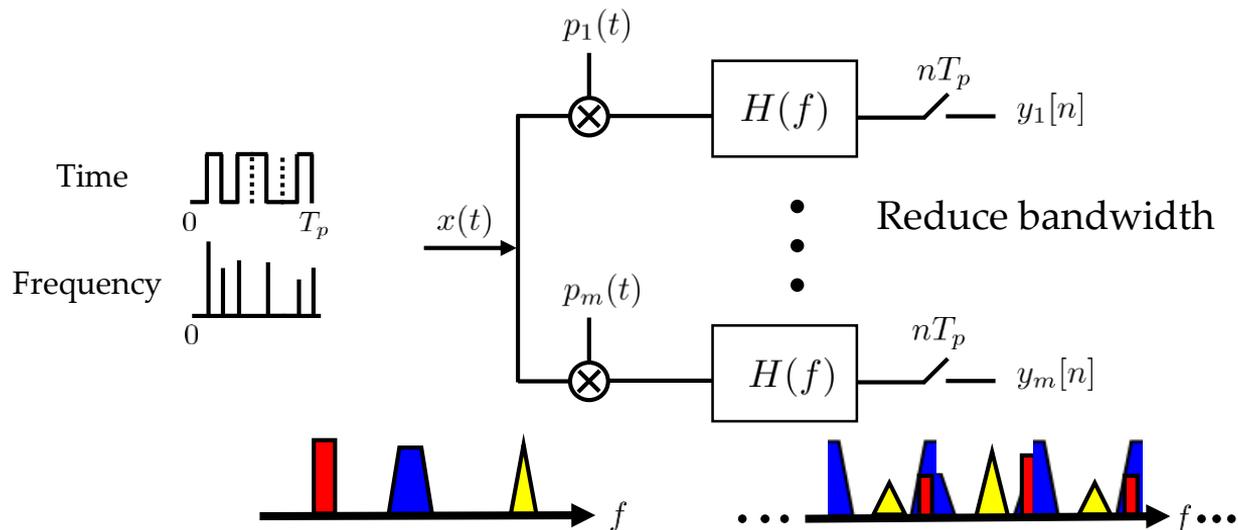
A sampling operator is invertible over a union of subspaces  $\mathcal{U}$  if and only if it is invertible for every

$$\mathcal{A}_{\lambda,\gamma} = \mathcal{A}_\lambda + \mathcal{A}_\gamma = \{x | x = x_1 + x_2, \text{ where } x_1 \in \mathcal{A}_\lambda, x_2 \in \mathcal{A}_\gamma\}$$

# Xampling Hardware

> Mishali and Eldar, 10-14

- > Alias the data onto low dimensional space by mixing with periodic functions



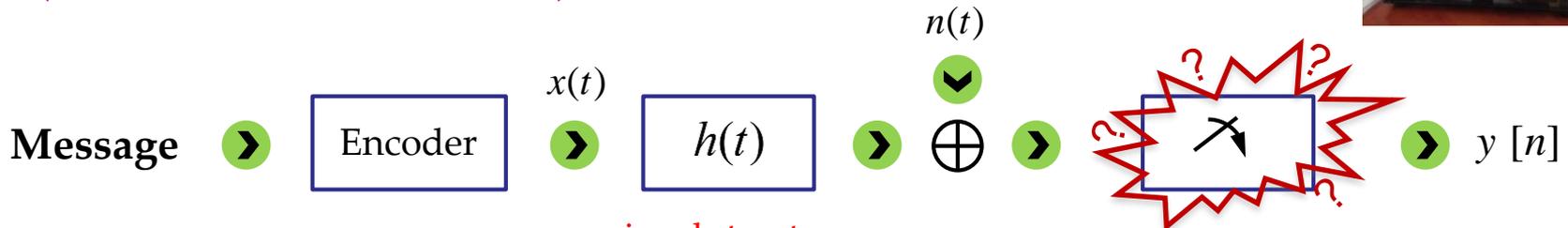
- > Functions designed so that in digital we have a CS problem



# Xampling Hardware

Sample at low rate using standard ADCs such that in digital we get a CS problem

- > Low rate, low bandwidth, simple hardware and low computational cost
- > Achieves the Cramer-Rao bound given a sub-Nyquist sampling rate (Ben-Haim, Michaeli, and Eldar 12)
- > Minimizes the worst-case capacity loss for a wide class of signal models (Chen, Eldar and Goldsmith 13)



signal structure,  
captured by channel

capacity-achieving  
sub-Nyquist sampler

$$\min_{\text{sampler states}} \max_{\text{states}} \text{CapLoss} \approx \frac{1}{2} \left\{ \mathcal{H}(\beta) - \alpha \mathcal{H} \left( \frac{\beta}{\alpha} \right) \right\}$$

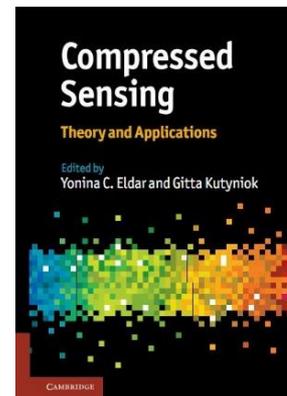
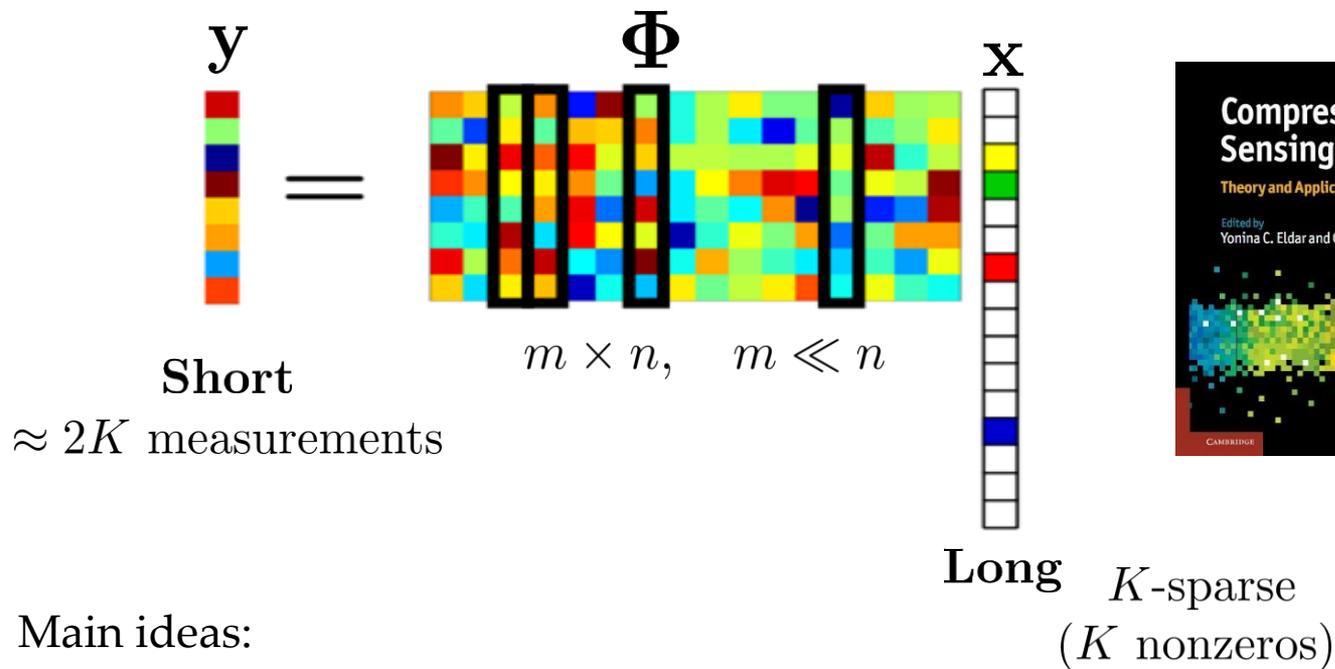
$$\mathcal{H}(\beta) = -\beta \log \beta - (1 - \beta) \log(1 - \beta)$$

binary entropy function

- >  $\alpha$ : undersampling factor
- >  $\beta$ : sparsity ratio

# Compressed Sensing

> Candes, Romberg, Tao 06, Donoho 06

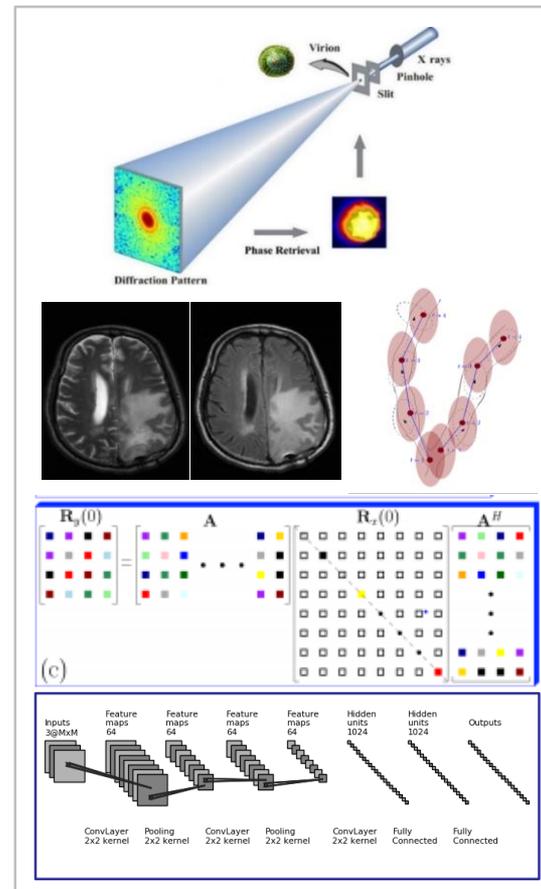


Main ideas:

- > Sparse input vector with unknown support
- > Sensing by sufficiently incoherent matrix (semi-random)
- > Polynomial-time recovery algorithms from  $K \log n$  measurements

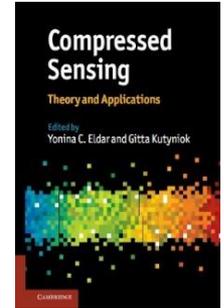
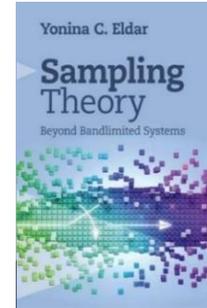
# Compressed Sensing Extensions

- Nonlinear sparse recovery (optics):
  - Phase retrieval  
(Shechtman et. al 11, 14, 15, Eldar and Mendelson 12, Ohlsson et. al 12)
  - Nonlinear compressed sensing  
(Beck and Eldar 12, Bahman et. al 11, Ohlsson et. al 13, Yang et. al 15)
- Reference based sparse recovery (MRI)  
(Weizman, Eldar and Ben Bashat 16)
- Sparsity with tracking (ultrasound) (Solomon et. al 18)
- Statistical sparsity  
(Pal and Vaidyanathan 14, Solomon et. al 18, Cohen and Eldar 18, Romero et. al 16)
- Deep learning (Gregor and LeCun 10, Mousavi and Baraniuk 17, Borgerding et. al 17, Aggarwal et. al 18, Bora et. al 17, Wu et. al 19)



# Xampling: Practical Compression + Sampling

- Xampling: practical sub-Nyquist sampling and processing
- Many examples in which we reduce sampling rate by exploiting structure
- Low rate translates to lower radiation dosage, faster scanning, processing wideband signals, smaller devices and improved resolution



DOA Estimation



Pulses



Ultrasound

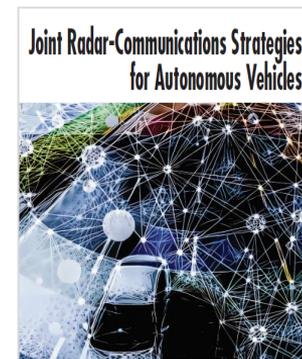
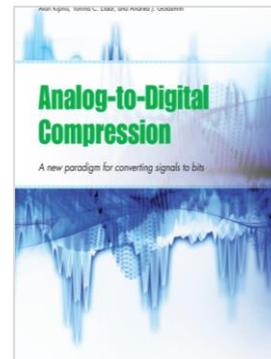
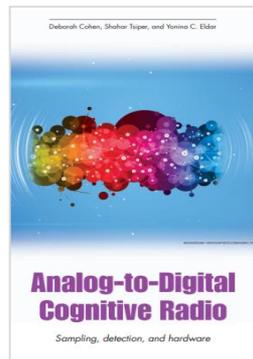
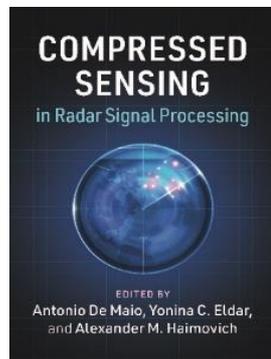


Radar

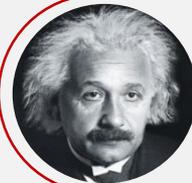


Cognitive Radio





# Applications

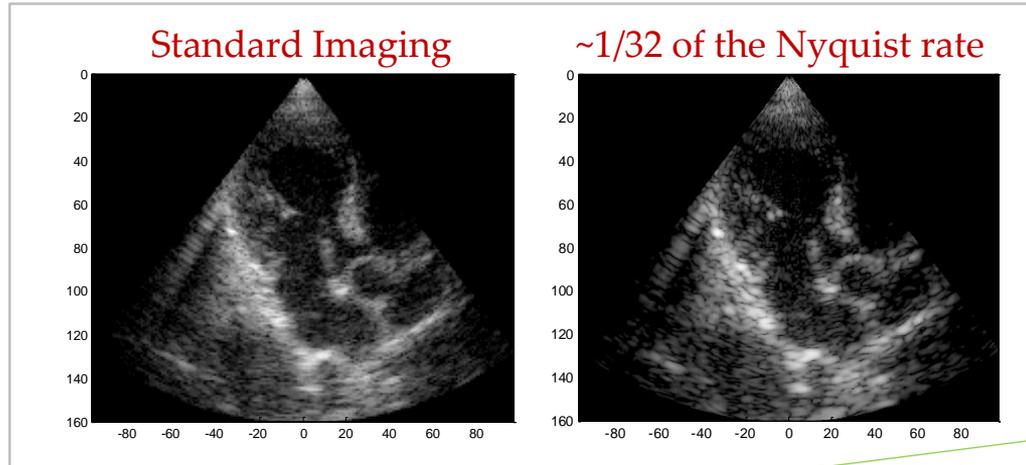


*“In theory, theory and practice are the same.  
In practice, they are not.”*

Albert Einstein

# Sub-Nyquist Ultrasound Imaging

> Chernyakova and Eldar 13-15



**4% Nyquist rate at every channel!**

Low rate sampling enables:

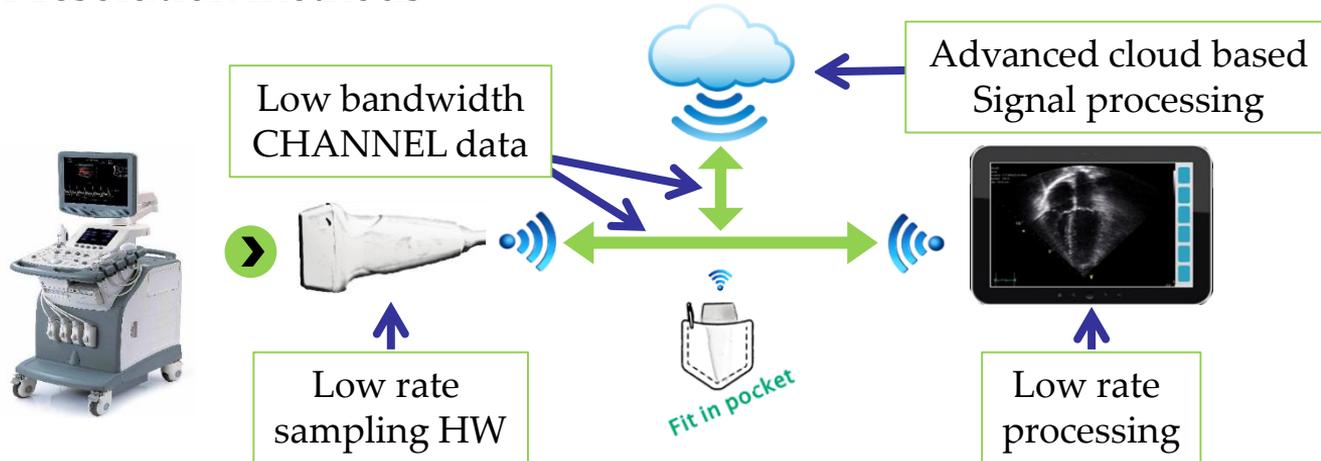
- > 3D imaging
- > High frame rate for cardiac imaging
- > Handheld wireless device: rural medicine, emergency imaging in the field/ambulance



# Bring the Digital Revolution to Ultrasound, Anywhere

**Xampling** technology samples and processes ultrasound signals without loss of information at very low rates!

- › Allows to integrate electronics into probe: wireless ultrasound
- › Enabling an “open imager” – advanced signal processing and AI methods **on channel data** that can run on any platform
- › Enabling remote health flexibility
- › Super resolution methods

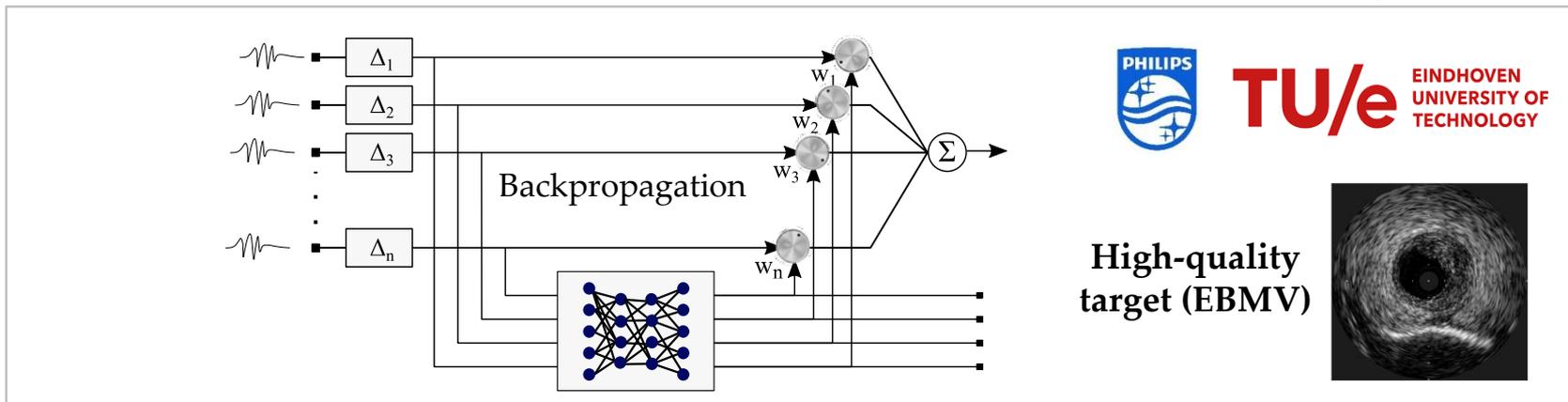


# Demo Movie



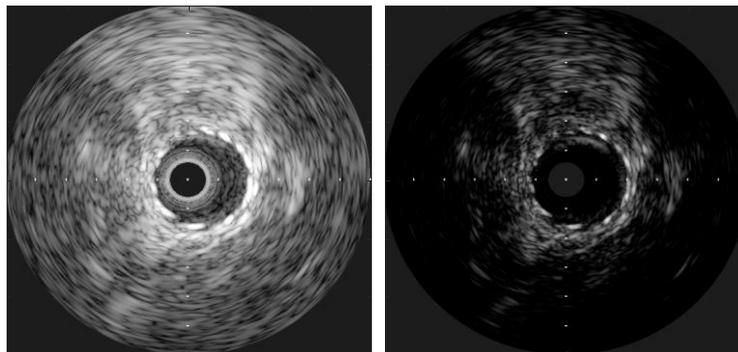
# Deep Adaptive Beamforming

> Luijten et. al 19



**Model based: Weights determined by deep learning!**

Delay-and-sum  
(standard)



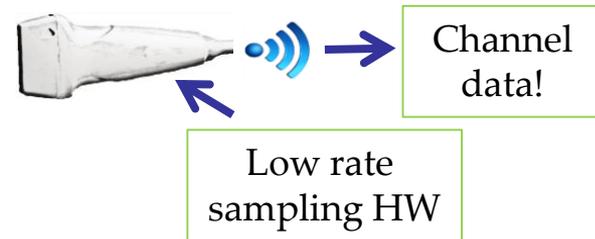
Deep learning

**Improved contrast  
and resolution**

# Channel Data Clinical Forum

## Improve diagnostics from channel data!

- › Ovarian cancer detection with MGH and MIT
- › Tumor classification with NYU medical and Siemens
- › Breast cancer detection with Beilinson
- › Children cardiology with Shiba
- › US for developing countries with Children's hospital and Brigham Women
- › Detection of pleural diseases with Haemek
- › Fetal anemia detection with Hillel Yaffe

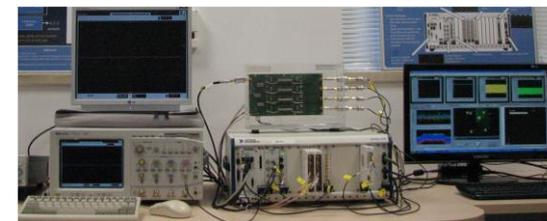
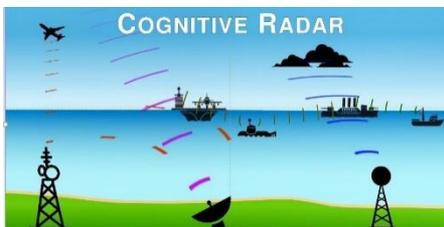
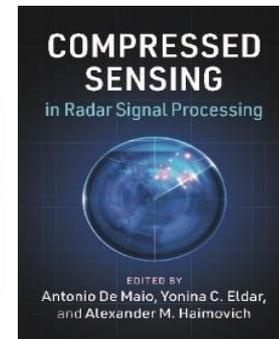
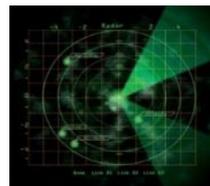


**New clinical applications enabled by new acquisition strategy**

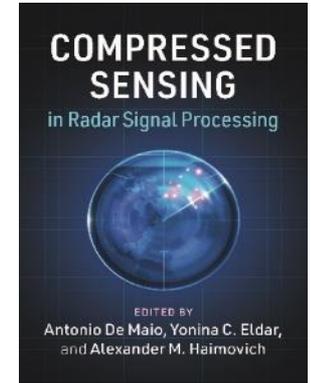
# Radar/Time of Flight Imaging

> Bar-Ilan and Eldar 14, Rossi et. al 14, Cohen and Eldar 18, Cohen et. al 18

- > Small, cheap radars with excellent resolution
- > We can also reduce physical parameters:
  - Create a radar map in less time
  - Use fewer antenna elements
- > Spectrum sharing between radar and communication over the same channel
- > Free congested spectrum
- > Fast frequency detection

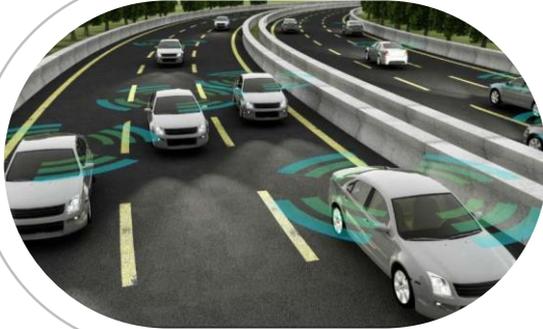


# Sub-Nyquist and Cognitive Radar



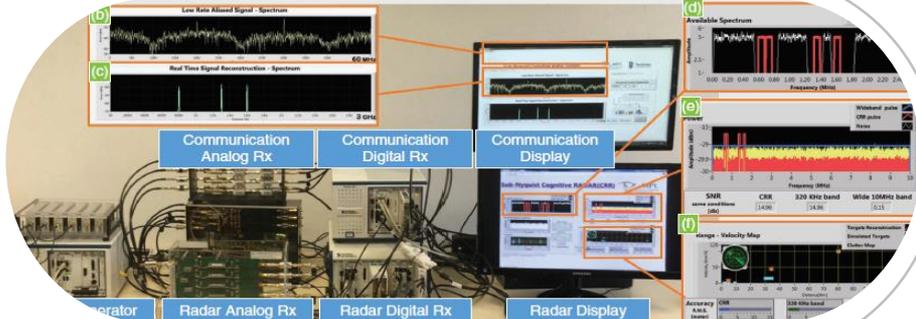
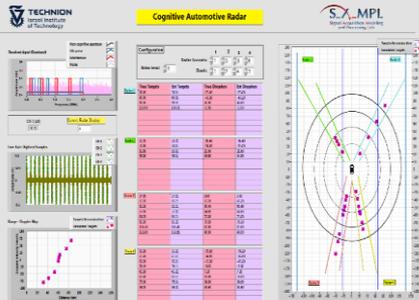
# Cognitive Automotive Radar

> Mulleti et. al 18-20



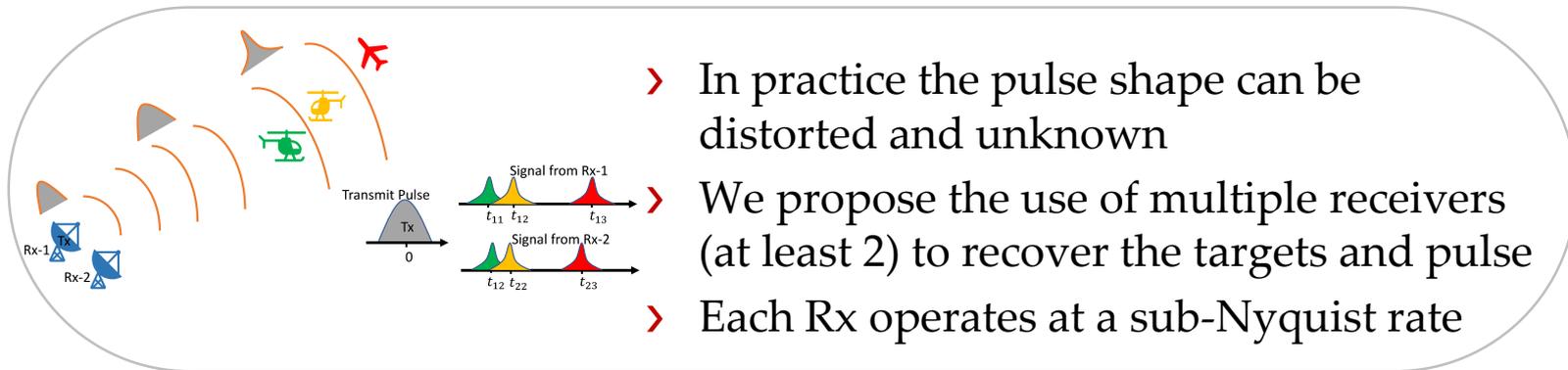
- > In autonomous systems the number of vehicles (radars) vary over time
- > Radars require to share bandwidth without interference
- > Our cognitive system divides the bandwidth into multiple narrow subbands adaptively
- > Based on desired no. of radars the subbands are assigned to each radar

**Sub-Nyquist sampling with robust reconstruction is achieved!**

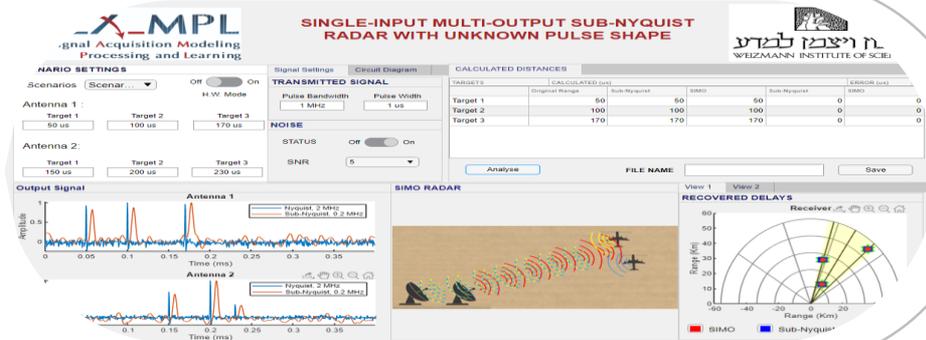
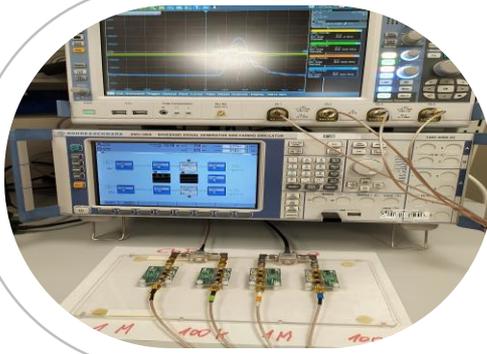


# Radar With Unknown Pulse Shape

> Mulleti et. al 20



Signal recovery from samples at 10 times lower than Nyquist



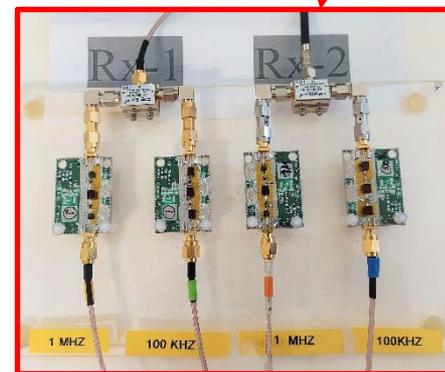
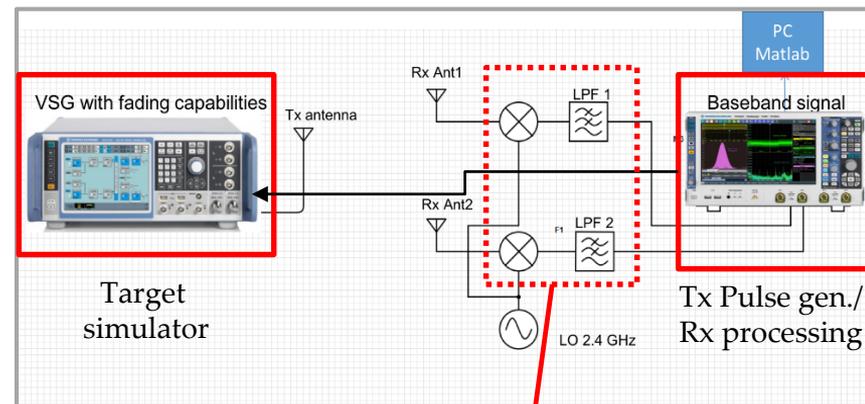
# Blind SIMO Sub-Nyquist Radar

Single-Input Multi-Output  
Sub-Nyquist Radar  
With Unknown Pulse Shape

S-X-MPL  
Signal Acquisition Modeling  
Processing and Learning Lab

מכון ויצמן למדע  
WEIZMANN INSTITUTE OF SCIENCE

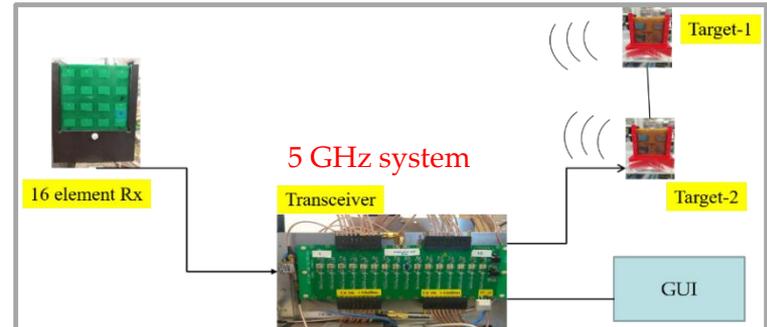
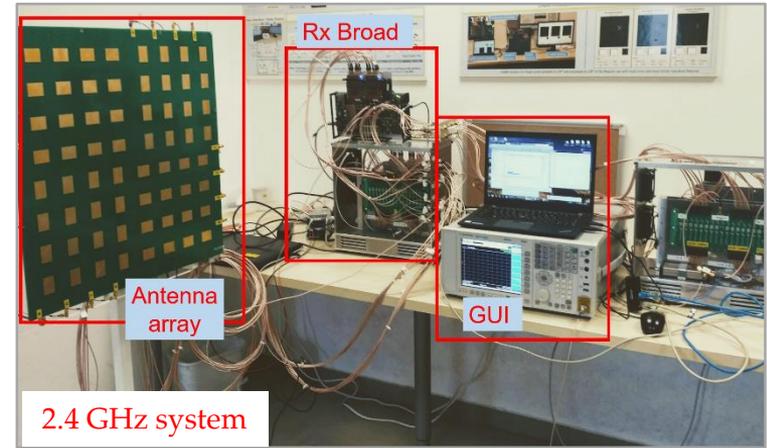
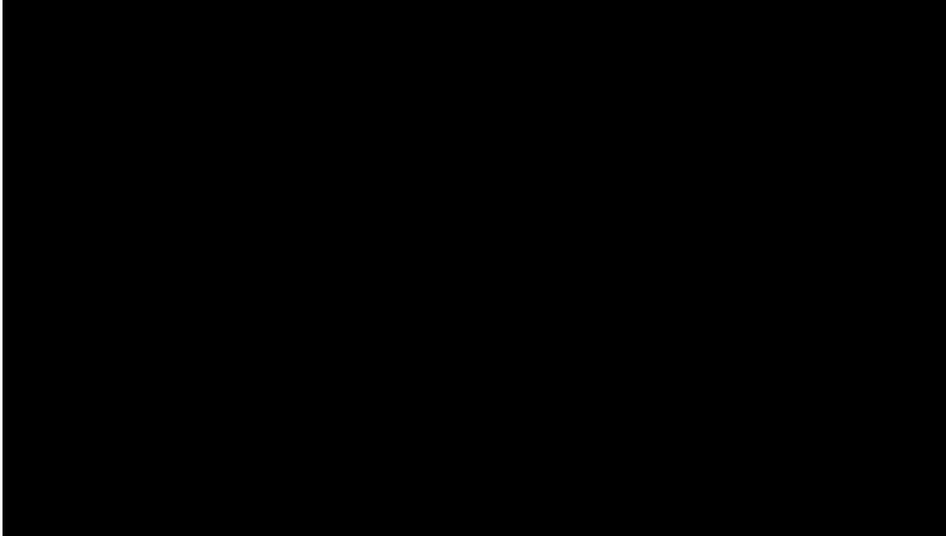
Allows for low power, low BW radar  
detection in complicated settings like  
automotive radar



Lowpass filters for Rx



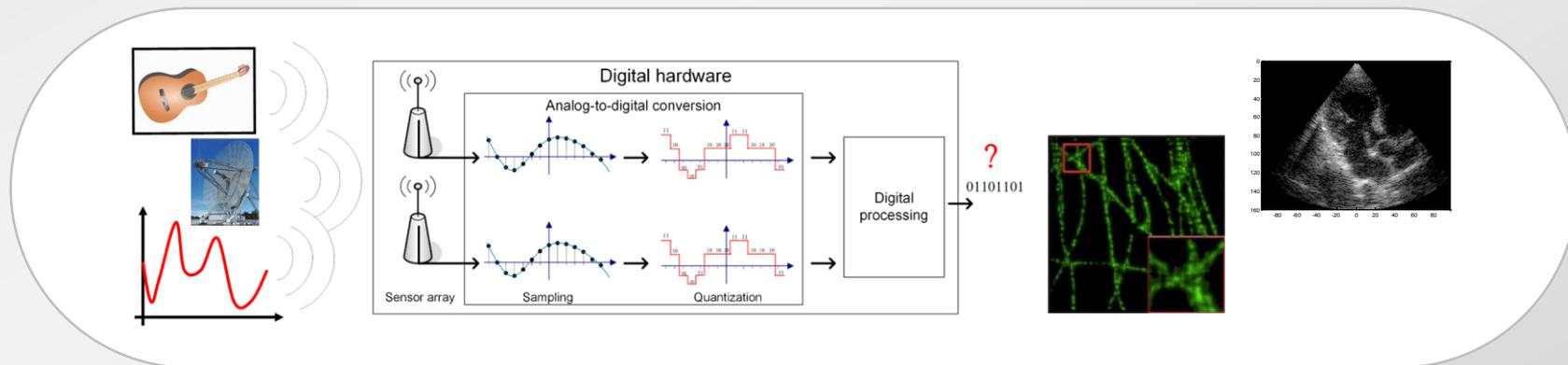
# Deep-Sparse Antenna Selection





## Part 2:

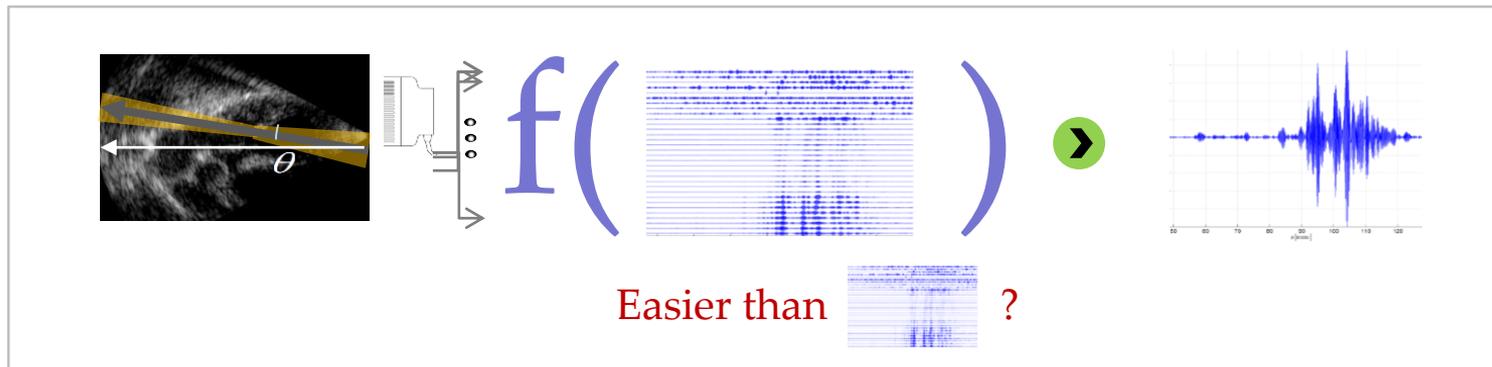
# Task-Based Sampling



# Task-Based Sub-Nyquist Sampling

**Can we reduce sampling rates for signals without structure?**

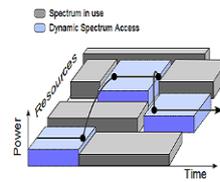
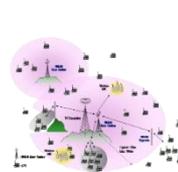
Consider the case where we don't actually need the signal, but rather some function of it



- > Signal statistics: Power spectrum estimation > with Geert Leus and Deborah Cohen
- > Quantized version of the signal > with Alon Kipnis, Andrea Goldsmith, and Tsachy Weissman
- > Task-based quantization in communication > with Nir Shlezinger and Miguel Rodrigues
- > Compressed beamforming > with Tanya Chernyakova and Regev Cohen

# Power Spectrum Reconstruction

- Often the required information can be extracted from the covariance rather than the signal itself:
  - Support detection
  - Statistical analysis
  - Array processing (e.g. DOA)
  - Brightness image



Cognitive Radios



Financial time series analysis

What is the minimal sampling rate to estimate the signal covariance of a wide-sense stationary ergodic signal?

- Previous work studied specific samplers in the asymptotic regime:
  - Vaidyanathan 11: coprime sparse samplers with arbitrarily low rate
  - Tarczynski 07, Davies 11, Leus 12: multicaset samples with arbitrarily low rate

For covariance estimation substantial rate reduction is possible!

# Covariance Estimation

> Cohen, Eldar and Leus 15

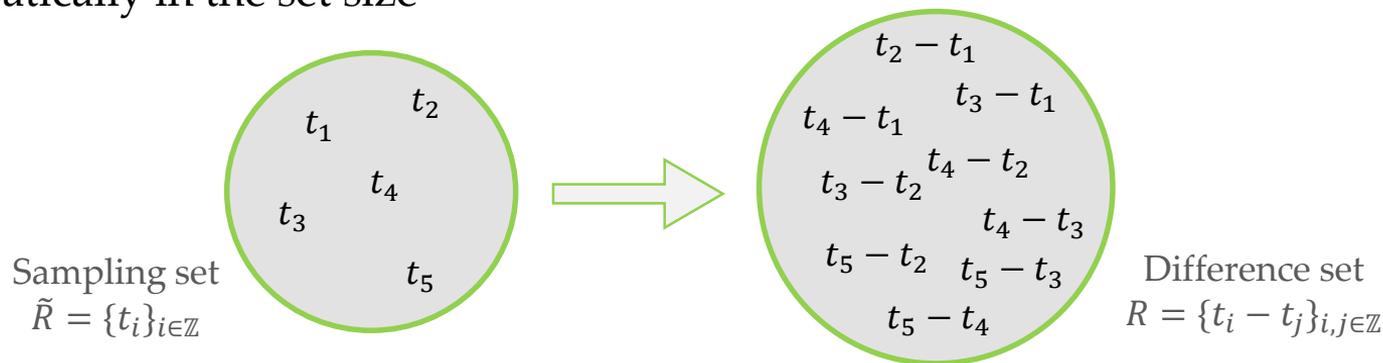
- > Let  $x(t)$  be a wide-sense stationary ergodic signal
- > We sample  $x(t)$  with a stable sampling set at times  $\tilde{R} = \{t_i\}_{i \in \mathbb{Z}}$
- > We want to estimate  $r_x(\tau) = \mathbb{E}[x(t)x(t - \tau)]$

What is the minimal sampling rate to recover  $r_x(\tau)$ ?

**Sub-Nyquist sampling is possible even for finite rates!**

**Intuition:**

- > The covariance  $r_x(\tau)$  is a function of the time lags  $\tau = t_i - t_j$
- > To recover  $r_x(\tau)$ , we only need the difference set which can grow quadratically in the set size



# Difference Set Density

**It is possible to create sampling sets with Beurling density 0 for which the difference set has Beurling density  $\infty$ !**

- › The density of the set should go to 0 slower than the square root
- › There should be enough distinct differences so that the size of the difference set grows like the square of the size of the sampling set
  - › The density of the square (difference set) goes to  $\infty$



## Theorem

Let  $\tilde{R} = \{t_i\}_{i \in \mathbb{Z}}$ , be a sampling set with lower Beurling density  $D^-(\tilde{R}) = 0$ , so that the set of differences between two sets of size  $p$  and  $q$  is of the order of  $pq$ . Let  $R = \{t_i - t_j\}, \forall t_i > t_j \in \tilde{R}$  be the associated difference set. If  $\lim_{r \rightarrow \infty} \frac{d_{\tilde{R}}(r)}{\sqrt{r}} = \infty$ , then,  $D^-(R) = \infty$

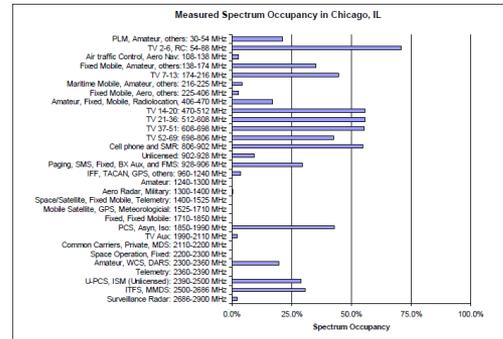
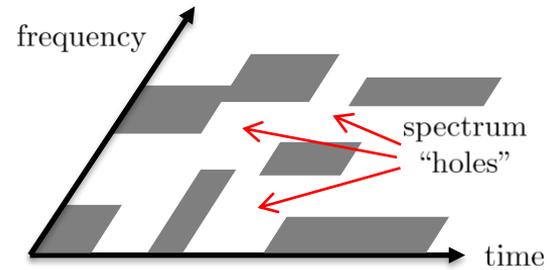
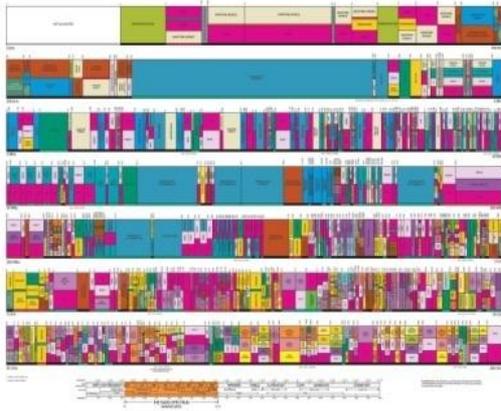
# Cognitive Radio

- Cognitive radio mobiles utilize unused spectrum “holes”
- Need to identify the signal support at low rates

## Federal Communications Commission (FCC) frequency allocation

### UNITED STATES FREQUENCY ALLOCATIONS

#### THE RADIO SPECTRUM



Shared Spectrum Company (SSC) – 16-18 Nov 2005

Licensed spectrum highly underused: E.g. TV white space, guard bands and more

# Sub-Nyquist Cognitive Radio

Deborah Cohen, Shahar Tsiper, and Yanina C. Eldar



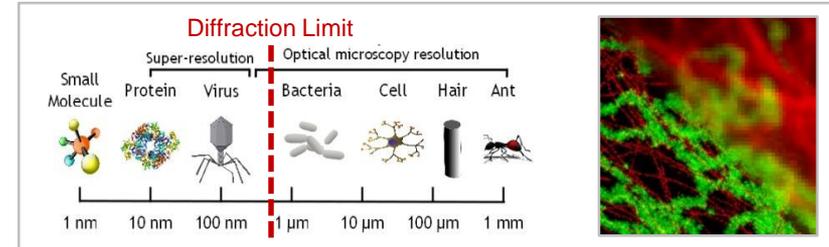
## Analog-to-Digital Cognitive Radio

*Sampling, detection, and hardware*

# Super Resolution Microscopy

- › Abbe's diffraction limit in optical imaging:

$$DL = \frac{\lambda}{2NA}$$



- › Noble prize 2014: super resolution using optical fluorescence microscopy (Betzig, Hell, Moerner)
- › New measurement process – control fluorescence of individual molecules
- › Image the same area multiple times – only a few point-emitters each time
- › Spatial resolution of ~20nm
- › **Limited temporal resolution!** > 10000 frames to collect all molecules



Photo: A. Mahmoud  
Eric Betzig



Photo: A. Mahmoud  
Stefan W. Hell

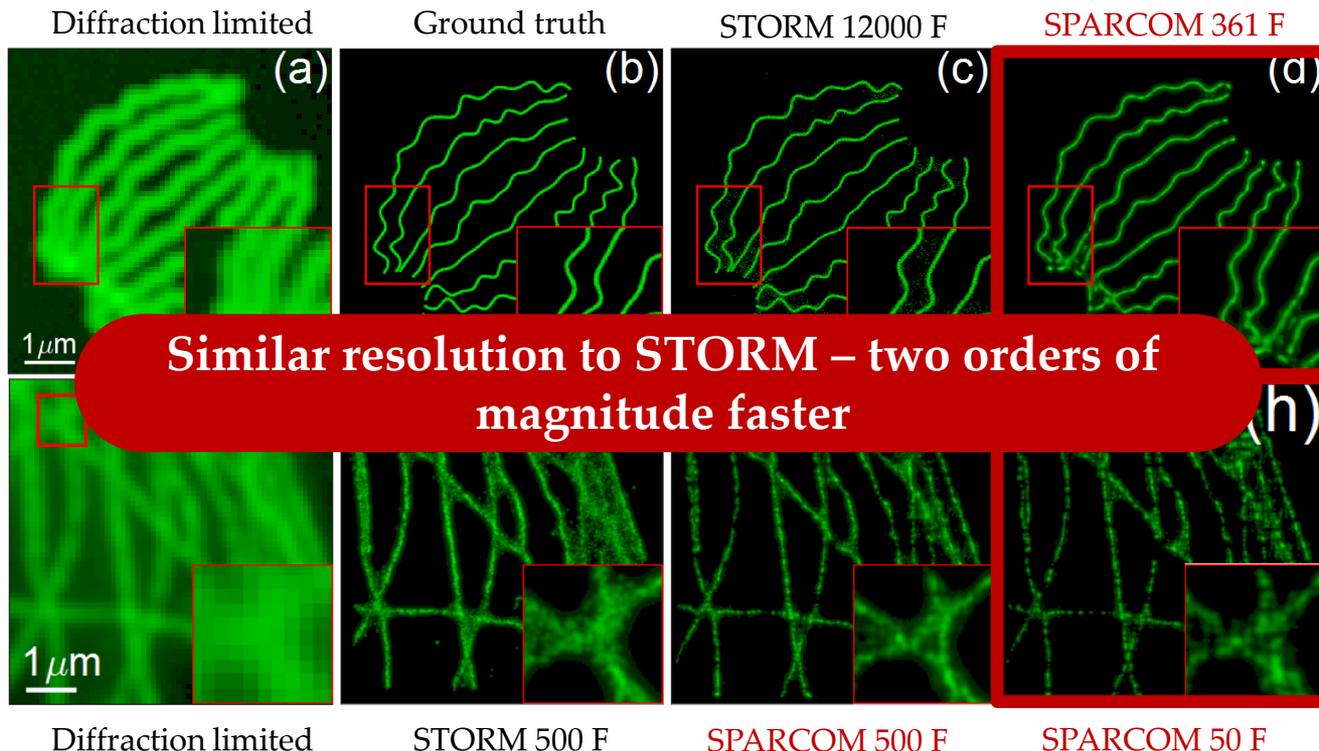


Photo: A. Mahmoud  
William E. Moerner

**Can we get both high temporal resolution and high spatial resolution?**

# SPARCOM: Super Resolution Correlation Microscopy

> Solomon et. al 18

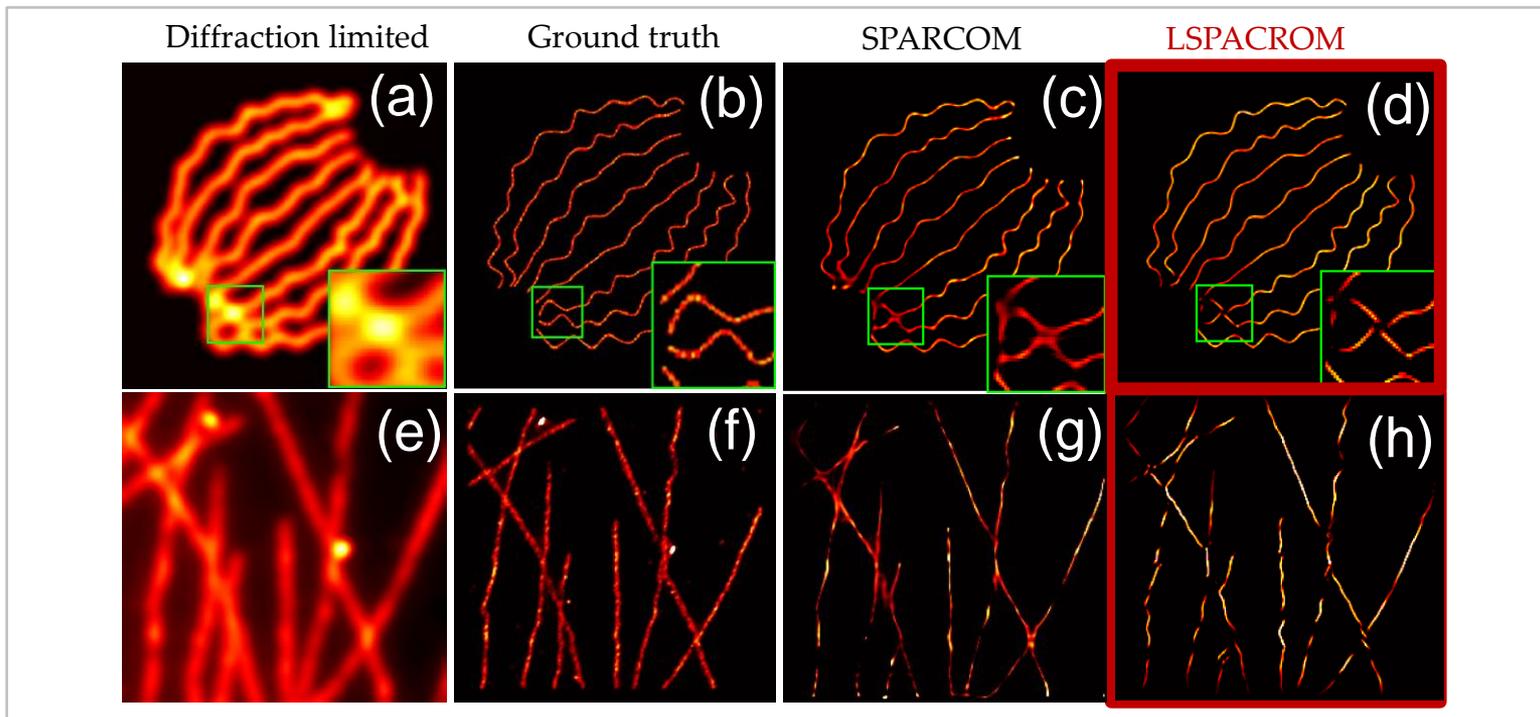


Data from: <http://bigwww.epfl.ch/smlm/>

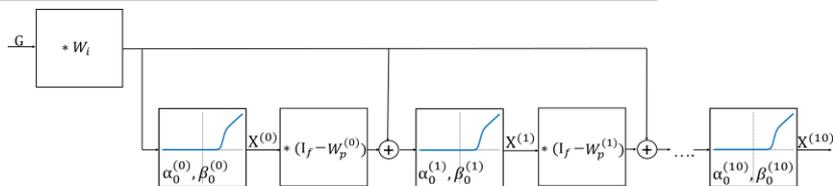
Super-resolution microscopy web site developed by Prof. Michael Unser's group at EPFL

# LSPARCOM: Learned SPARCOM

> Dardikman-Yoffe and Eldar, 20



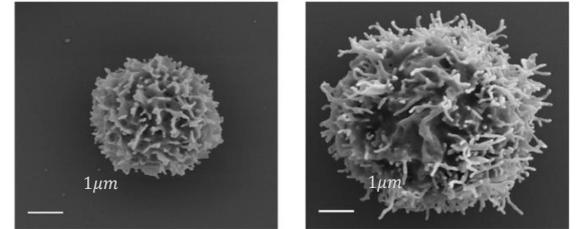
- > Performance equivalent to SPARCOM, but with no prior knowledge regarding PSF or parameter selection
- >  $10 \times$  improved convergence rate



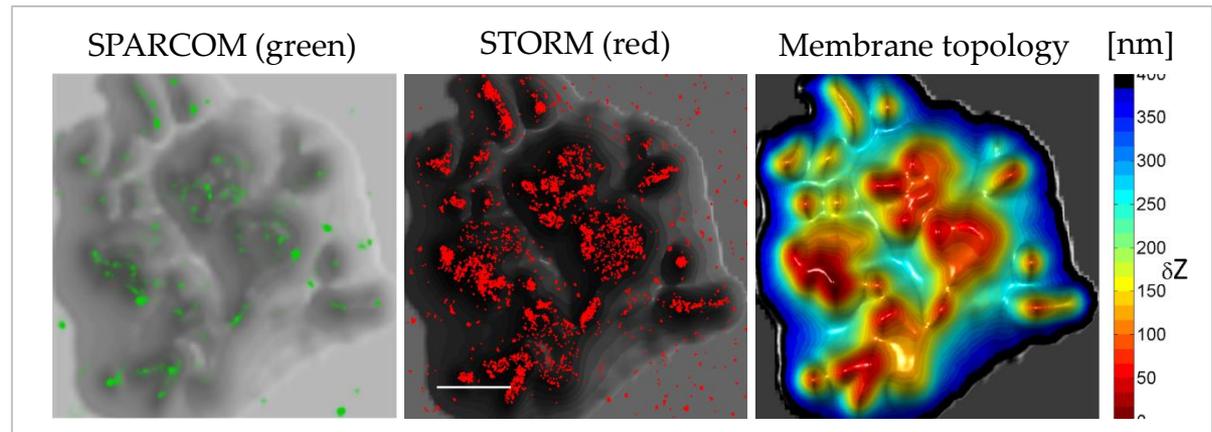
# Super-resolution of T-cell Receptors

> Collaboration with the group of Prof. Haran from Weizmann

- > Immune response of T-cells involves T-cell receptor (TCR) molecules
- > TCRs are clustered inside the microvilli
- > STORM experiment with 30000 exposures
- > SPARCOM performs reliable recovery with **100 times shorter acquisition period**



May lead to live cell inspection of TCR arrangement



# Super Resolution Contrast Enhanced Ultrasound

> Bar Zion et. al 18

Bolus **injection** of micro-bubbles into the blood stream

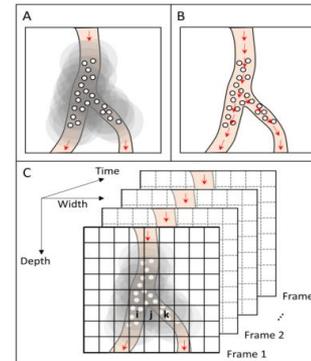
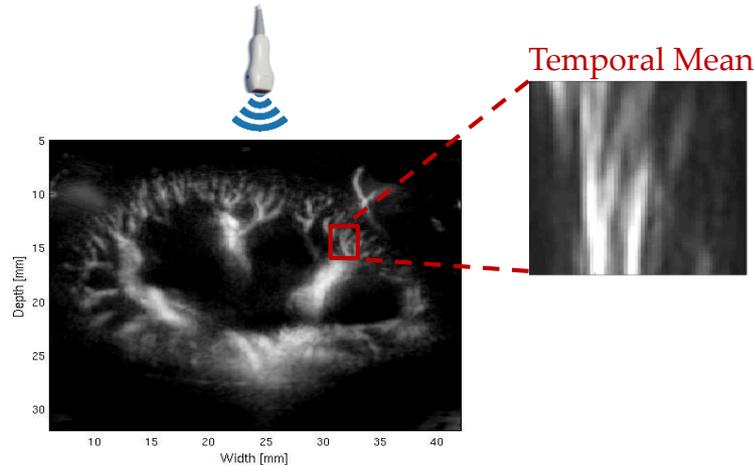


**Acquisition** of consecutive frames



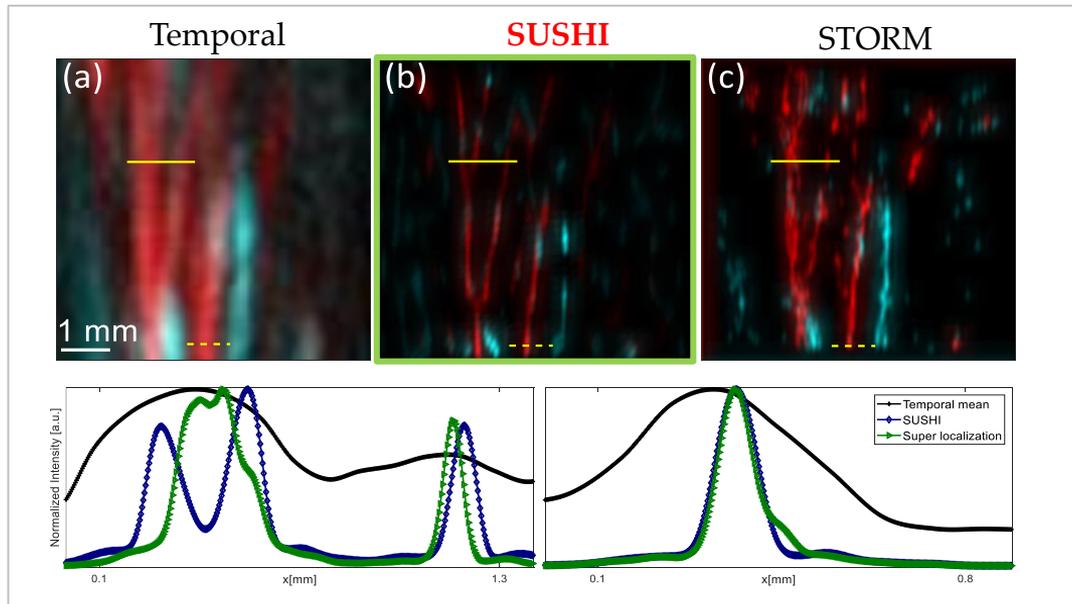
**Sub-wavelength image**

**Micro-bubbles act as point emitters in the bloodstream**



# SUSHI: Sparsity-Based Ultrasound Super-resolution Hemodynamic Imaging

- › Super-resolution imaging using CEUS in real-time
- › Applications: Relapse detection & treatment monitoring in Crohn's disease, breast-cancer screening
- › Clinical evaluation: Drs. Anat Ilivitzki (Crohn), Ahuva Grubstein and Yael Rapson (breast cancer)



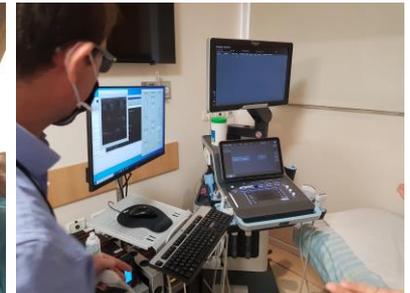
# Super Resolution Ultrasound for Breast Lesions

> Collaboration with Drs. Ahuva Grubstein, Yael Rapson, and Dror Suhami

- > Many imaging results are indeterminate requiring biopsy for pathologic confirmation
- > Problems: emotional stress, risk of complications and additional time and cost
- > Improved ultrasound imaging methods can provide advantages in screening and diagnosis

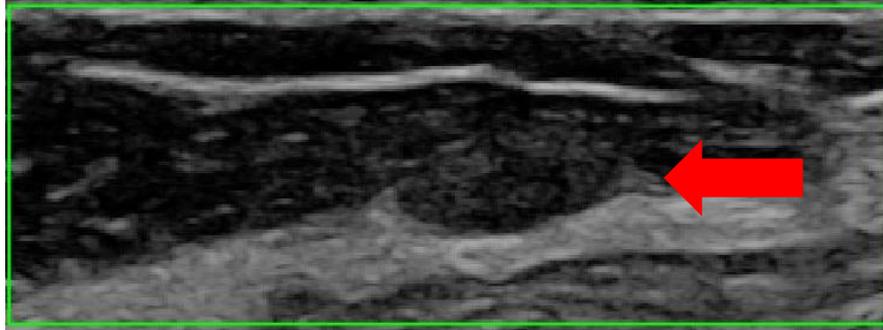
## Scanning with our methods:

- > One week of scans took place at Beilinson hospital
- > A total of 21 patients between the ages of 30-70 participated
- > 4 patients with malignant lesions and 17 patients with benign lesions
- > Advanced sparsity based deep learning methods were applied to the data to get super resolved images at real time (< 1 min)

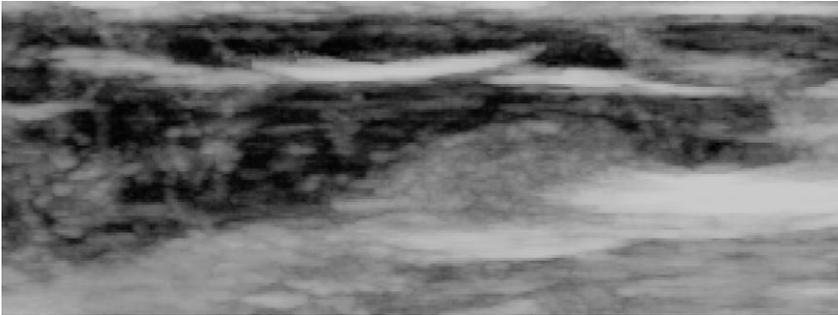


# Patient 2: Fibroadenoma

B mode

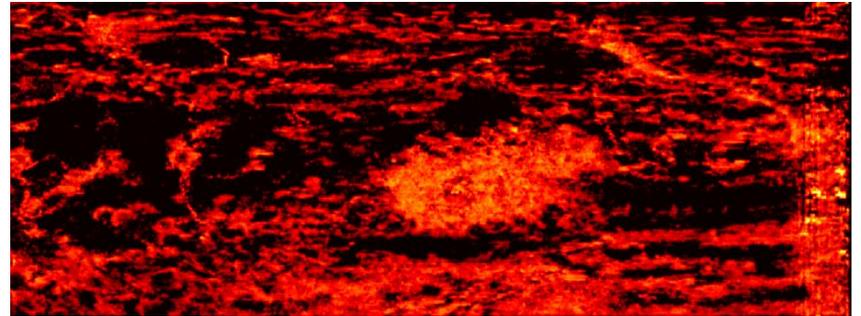


MIP



Standard maximum intensity projection. Difficult to separate lesion signal from tissue signal.

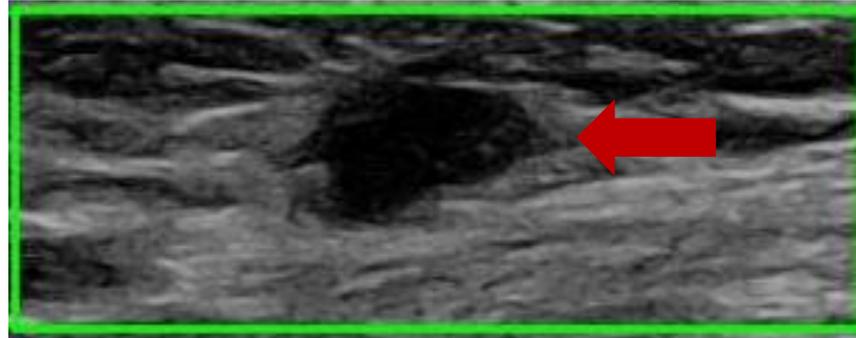
Deep unfolded ULM



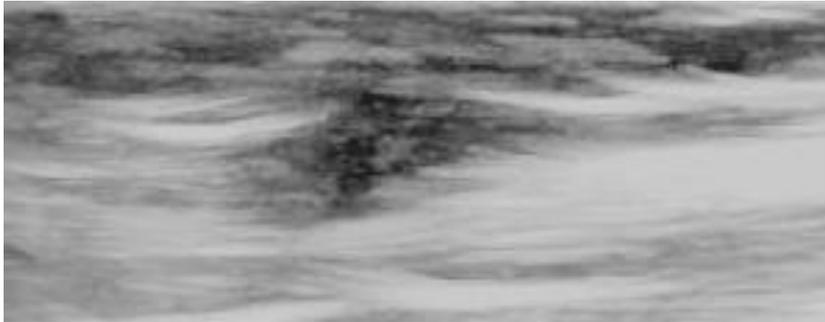
Super resolved image. Displays a highly vascularized lesion.

# Patient 18: Malignant mass

B mode

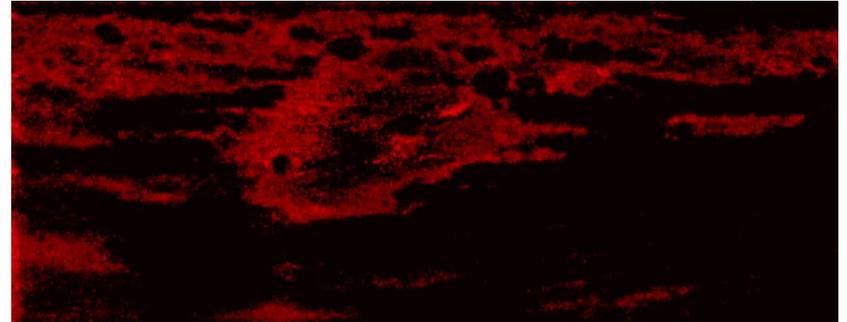


MIP

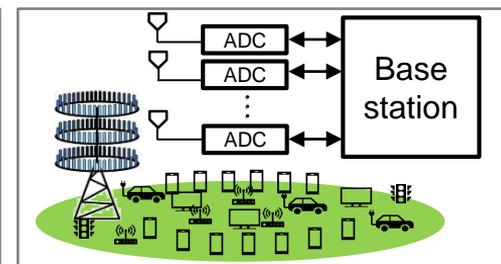
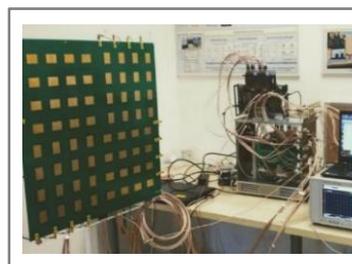
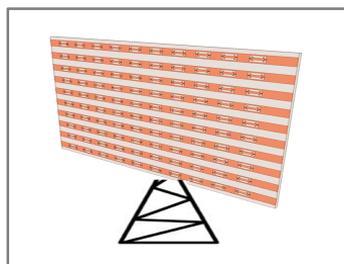
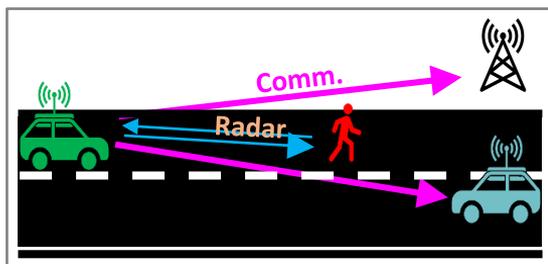


Standard maximum intensity projection. Difficult to separate lesion signal from tissue signal.

Deep unfolded ULM



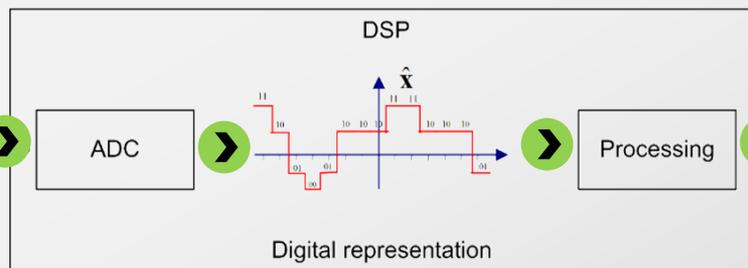
Super resolved image. Displays a high vascularization at the edges of the mass and a low concentration of blood vessels at the middle.



# Quantization



Observed physical signal



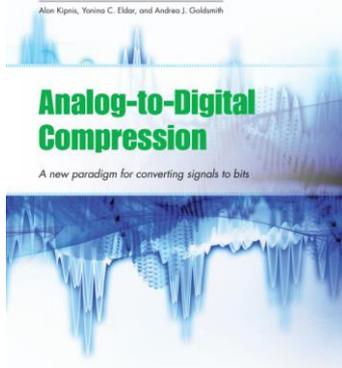
$\hat{s}$



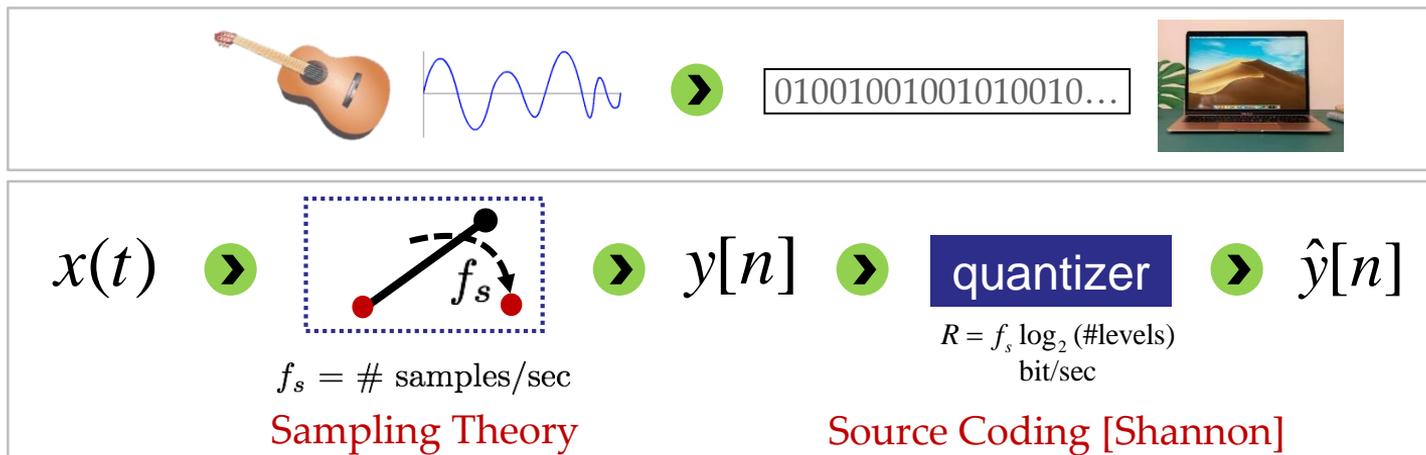
# Analog to Digital Compression

> Kipnis, Goldsmith, Eldar and Weissman 17-19

- > Until now we ignored quantization
- > Quantization introduces **inevitable distortion to the signal**
- > Since the recovered signal will be distorted due to quantization:

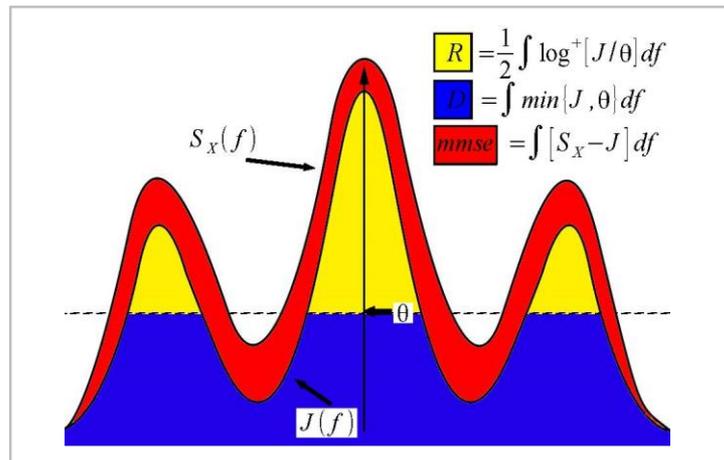
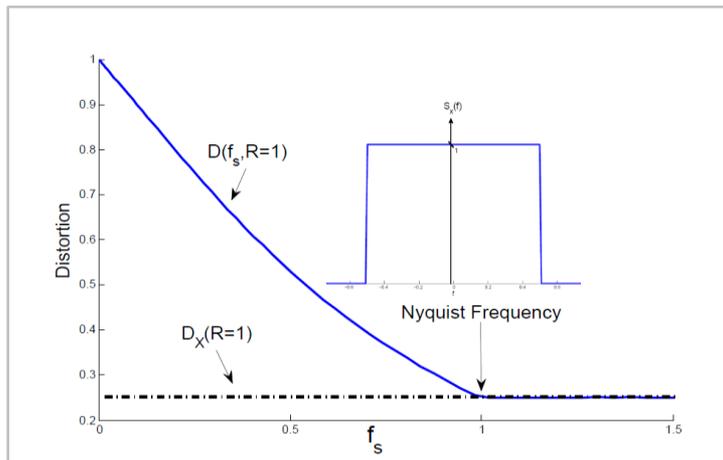


**Do we still need to sample at the Nyquist rate?**



**Goal: Unify sampling and rate distortion theory**

# Quantizing the Samples: Source Coding Perspective



- Preserve signal components above “noise floor”  $q$ , dictated by  $R$
- Distortion corresponds to mmse error + signal components below noise floor

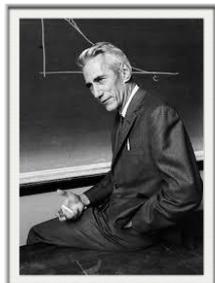
**Theorem** (Kipnis, Goldsmith, Eldar, Weissman 2016)

$$R(f_s, \theta) = \frac{1}{2} \int_{-\frac{f_s}{2}}^{\frac{f_s}{2}} \log^+ \left[ \tilde{S}_{X|Y}(f) / \theta \right] df$$

$$D(f_s, \theta) = mmse_{X|Y}(f_s) + \int_{-\frac{f_s}{2}}^{\frac{f_s}{2}} \min\{\tilde{S}_{X|Y}(f), \theta\} df$$

# Optimal Sampling Rate

> Kipnis, Eldar and Goldsmith 18



Shannon [1948]

*“we are not interested in exact transmission when we have a continuous source, but only in transmission to within a given tolerance”*

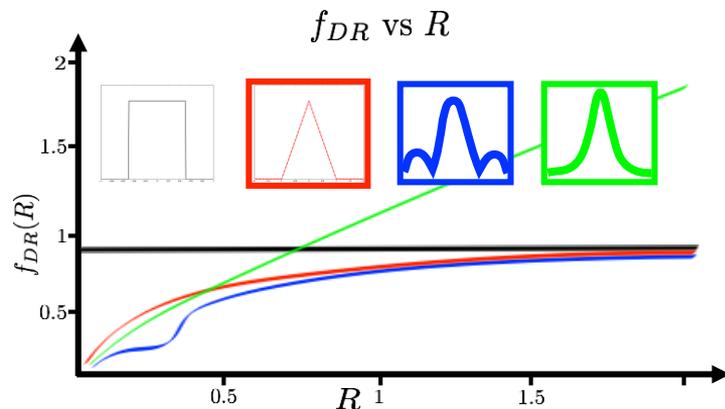
Can we achieve  $D(R)$  by sampling below  $f_{\text{Nyq}}$ ?

> Yes!

For any non-flat PSD of the input

$$D(R, f_s) = D(R) \text{ for}$$

$$f_s \geq f_{DR}(R)!$$

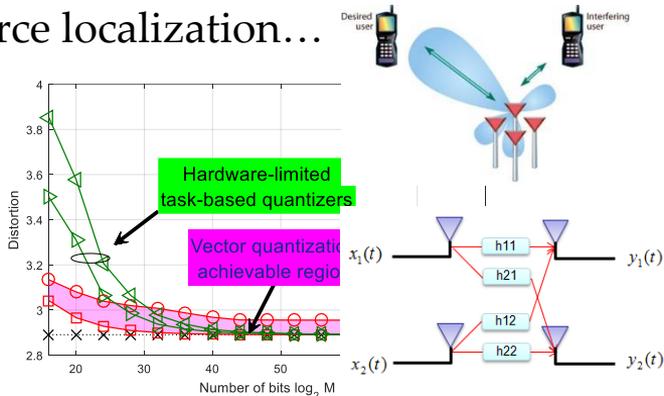


No optimality loss when sampling at sub-Nyquist (without input structure)!

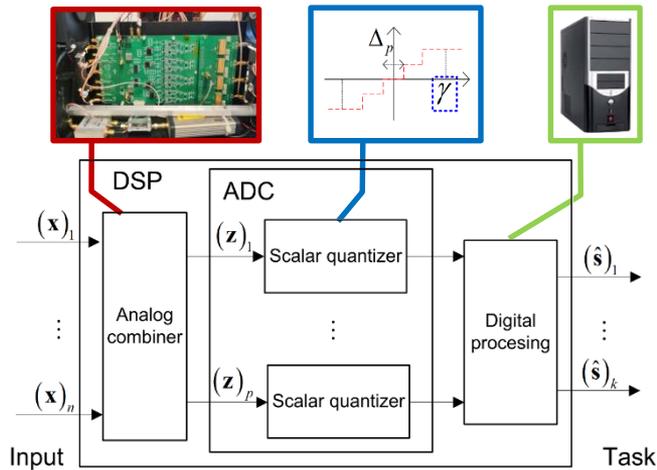
# Task-Based Hardware-Limited Quantization

> Shlezinger, Eldar, Rodrigues 19

- > Optimal quantization typically using vector quantizers
- > ADCs are usually serial scalar quantizers
- > Signals are often acquired for a task:
  - Channel estimation
  - Source localization...



Hybrid quantization system



Jointly optimize in light of the task

Analog combining	Quantizer support	Digital processing
------------------	-------------------	--------------------

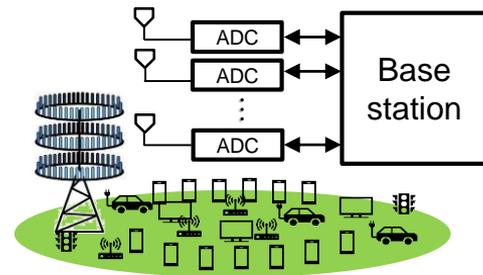
Exploit task to reduce number of bits and simplify hardware

**Tools:** Majorization theory, dithering, water filling

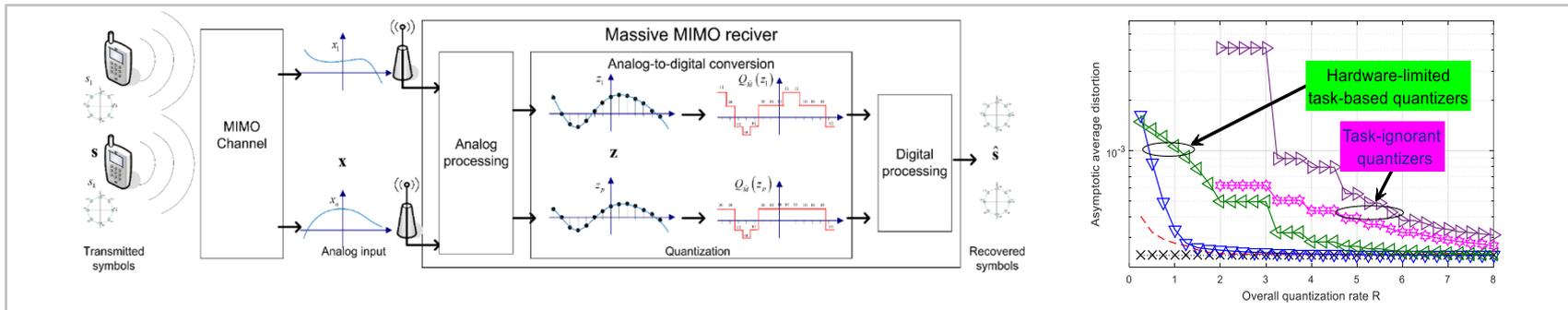
# Application: Massive MIMO

> Shlezinger, Eldar, and Rodrigues 19-20

- Next generation cellular communications
- Equip base stations with large antenna array
  - Increases throughput (Marzetta 10, Shlezinger and Eldar 19)
  - Costly in power and memory
  - Efficient quantization is essential
- Hybrid architectures are common (Mo et al 17), (Roth et al 17), (Stein and Eldar 19)....
- Lots of work on low bit ADCs: approximate ADC output and apply MMSE (Li et. al 17), (Choi, Mo, Heath 17), (Mollen et. al 17), (Mo et. al 18), (Jacobsson et. al 17), ...



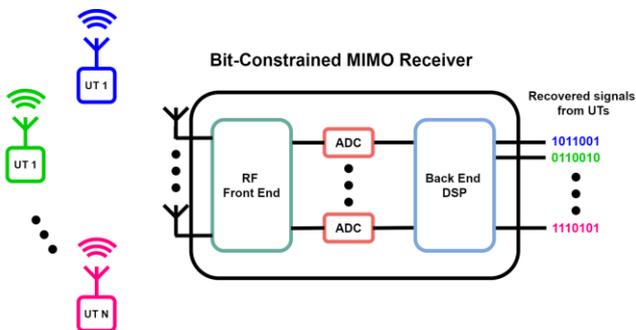
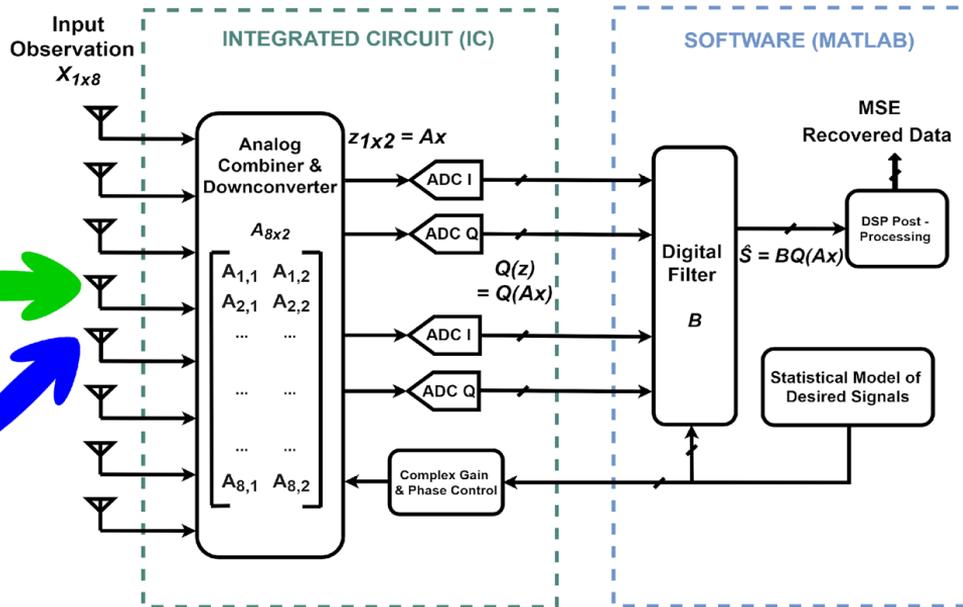
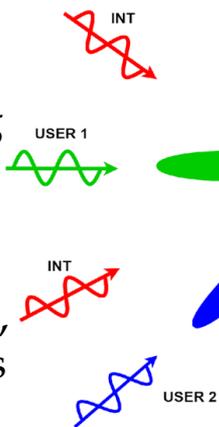
Jointly optimize as a task-based quantizer!



# Proposed Research: Task-Based MIMO IC

> Zirtiloglu, Shlezinger, Eldar, Yazicigil '21

- > Task is to minimize error vector magnitude (EVM)
- > Task-oriented architecture using low quantization rate
- > Configuring optimal analog pre-quantization matrix  $A$  and digital post-quantization filter  $B$ , using statistical model of signals
- > Analog/digital beamforming for spatial interferer rejection

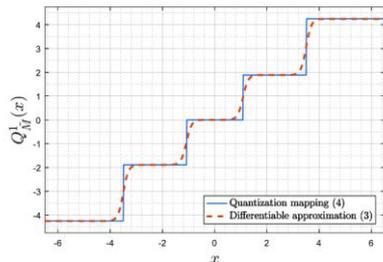


	Fully Digital (Conventional)	Orthogonal Beamforming (Golabighezalahmad et al 19)	Proposed Task-Based MIMO
RF Front End Power	LOW	HIGH	LOW
ADC Power	HIGH	LOW	LOW
Low Quantization Rate	✗	✗	✓
Spatial Filtering	✗	✓	✓

# Deep Task-Based Quantization

> Shlezinger and Eldar 19

- > Data-driven task-based quantization

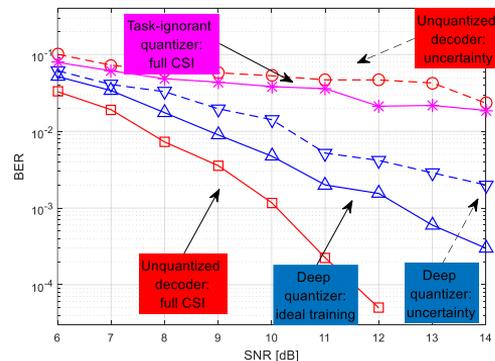
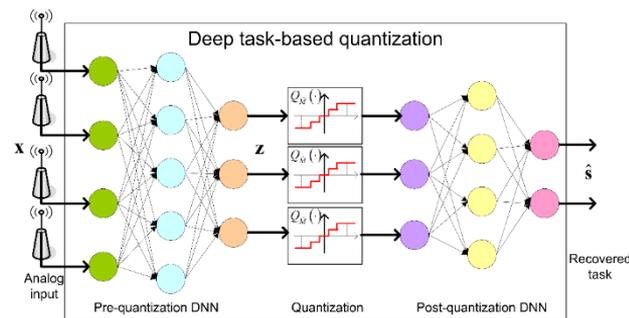


- > Learn mapping from training
- > Model-ignorant

Structure in the quantizer + the task



Simple and robust deep quantizers that achieve optimal performance!

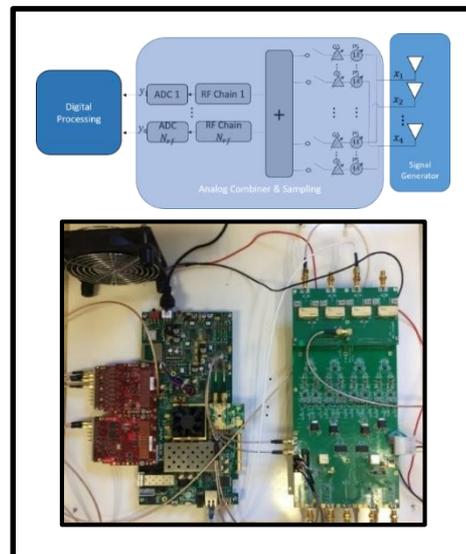


# Massive MIMO Demo

> Ioushua et. al 18-20

Practical MIMO receiver with fewer RF chains than antennas + low bit samplers

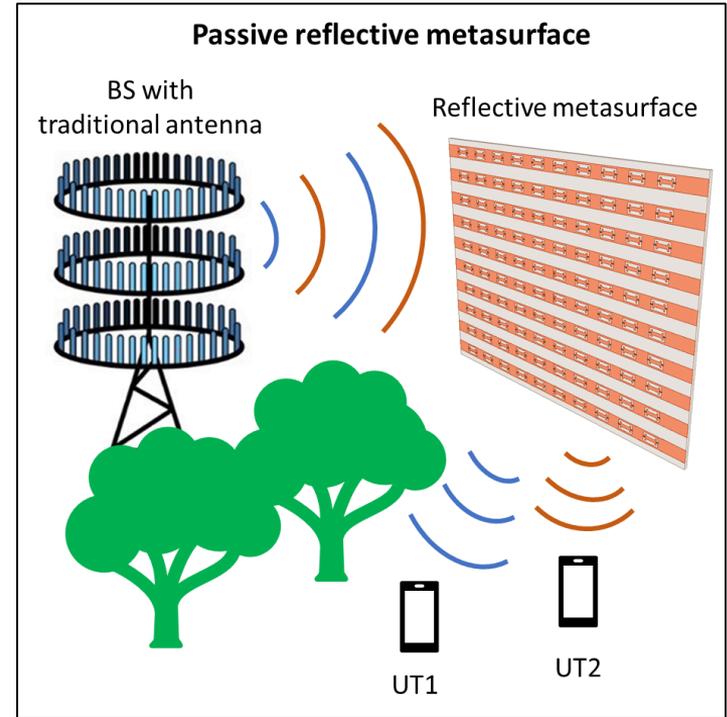
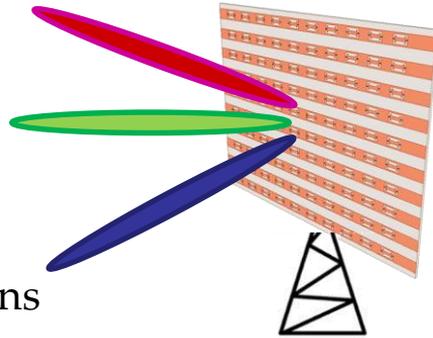
- > Significantly reduce power and hardware cost
- > Similar performance!



Task-based quantizers lead to simple low power hardware for comm and radar systems without degrading performance!

# Dynamic Metasurface Antennas

- › Emerging antenna technology:
  - › Scalable
  - › Low power
- › Dynamically configurable radiation pattern
- › Applications:
  - › Microwave imaging
  - › Radar systems
  - › Satellite communications
- › Intelligent reflective surfaces (Huang et al, TWC 19)



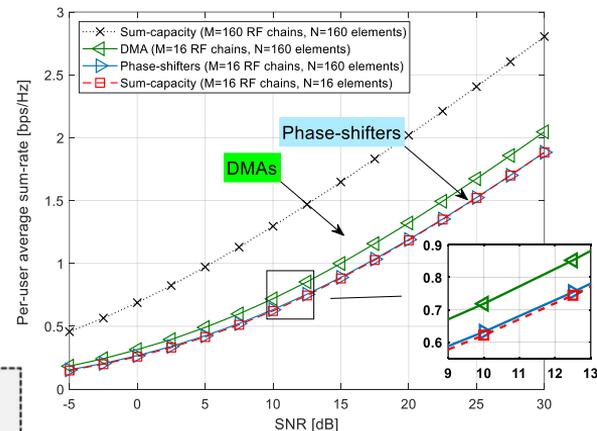
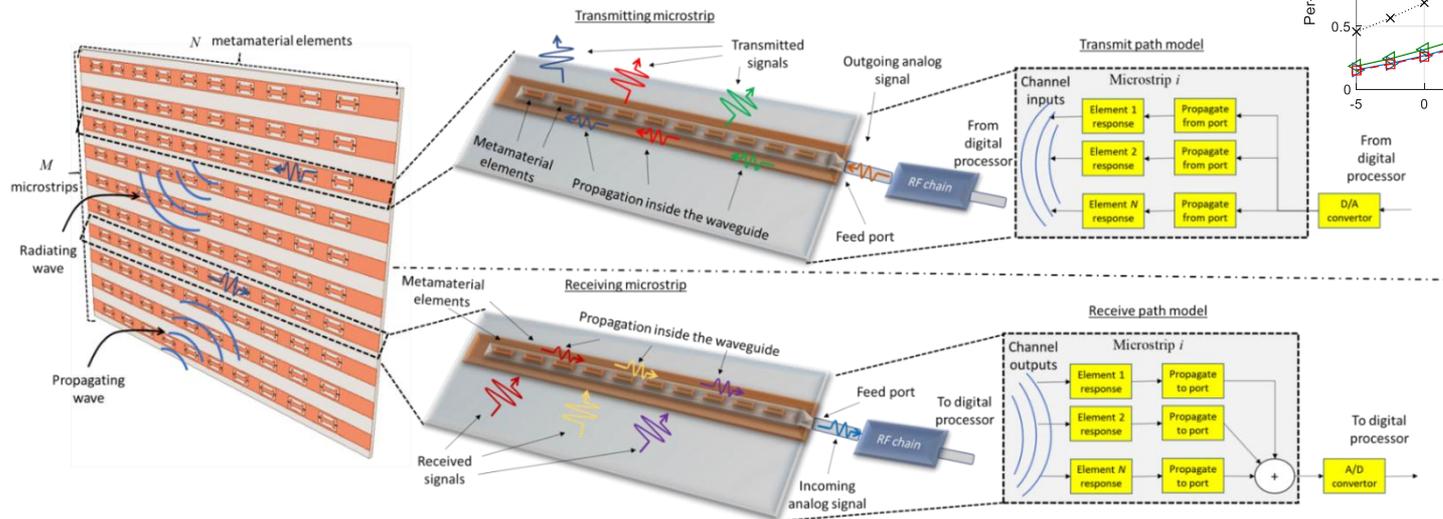
# Metasurfaces for Analog Precoding

> Shlezinger et. al 19-21

> Collaboration with the group of Prof. David Smith

Alternative approach to dedicated analog precoder hardware

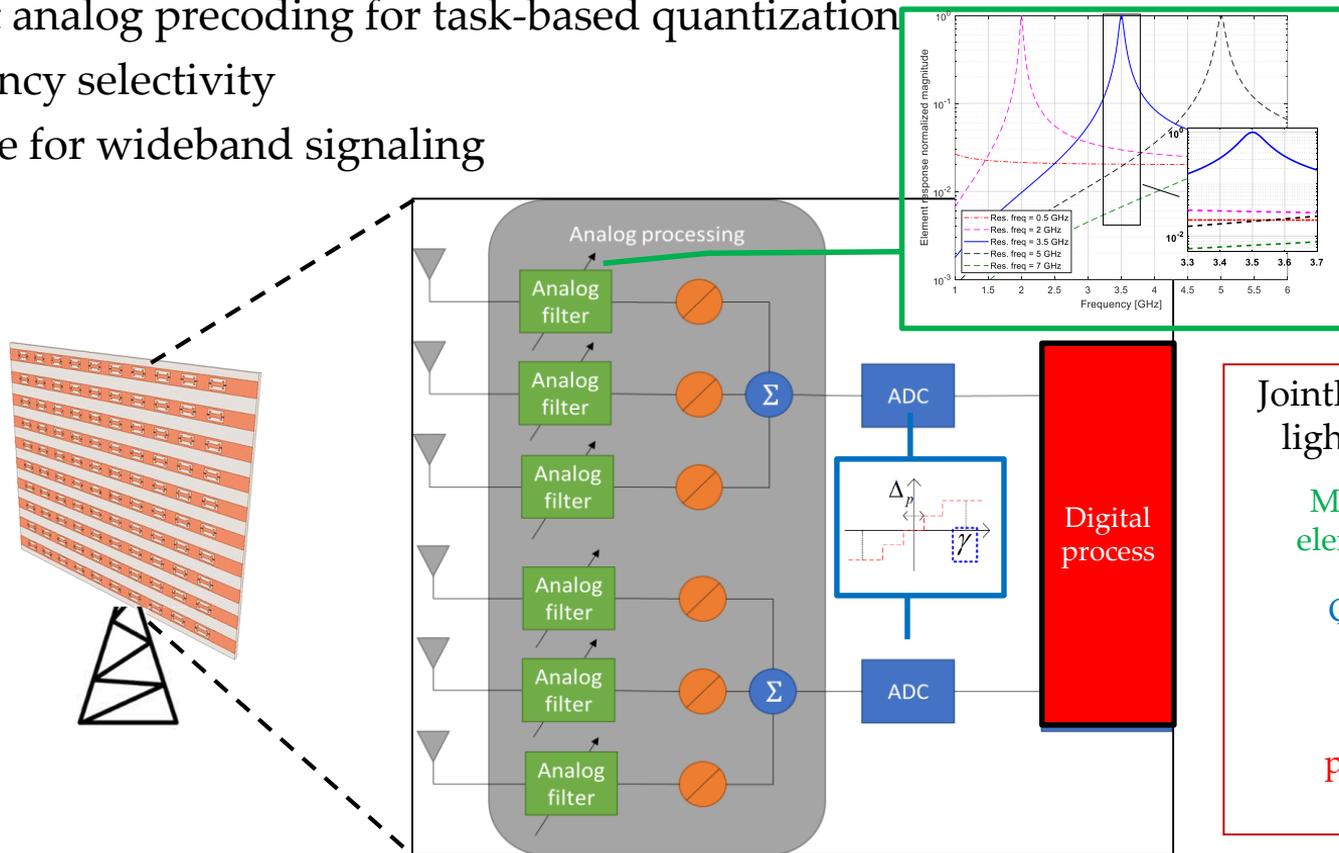
- > Inherent tunable analog precoding in the antenna structure
- > Low power, small hardware
- > Enhanced frequency-selective analog processing



# Metasurface Antennas with Low-Bit ADCs

> Wang et al. 20

- > Exploit analog precoding for task-based quantization
- > Frequency selectivity
- > Suitable for wideband signaling



Jointly optimize in  
light of the task

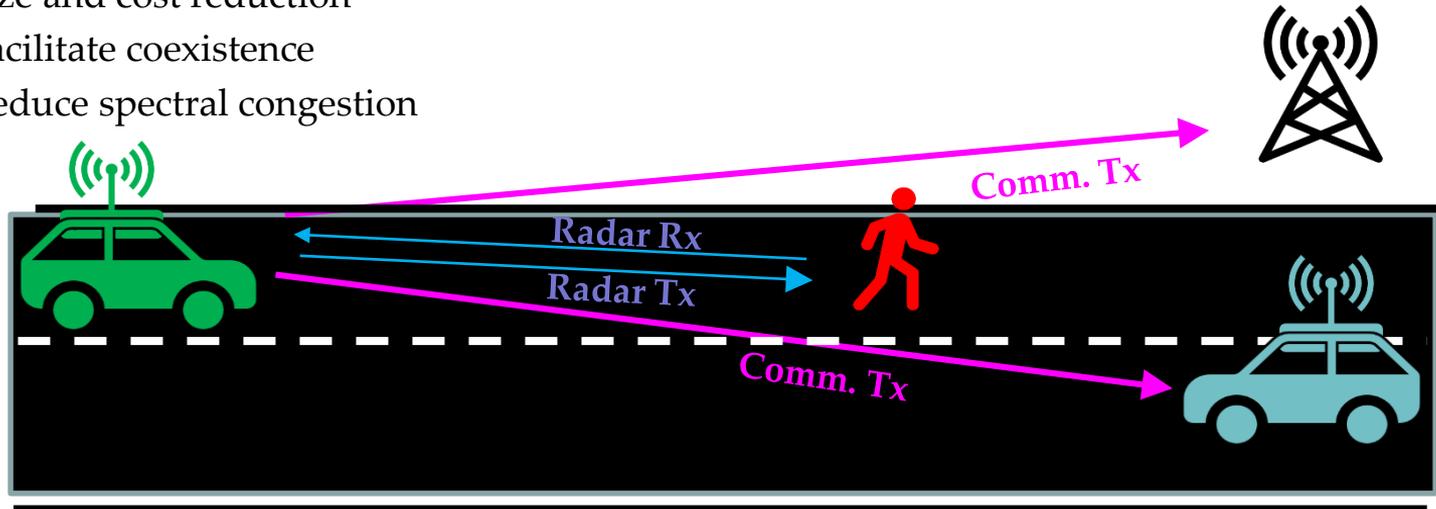
Metamaterial  
element setting

Quantizer  
support

Digital  
processing

# Joint Radar-Communications for Autonomous Driving

- › We have seen ways to reduce size, power, space in both radar and comm
- › Can we combine?
- › Autonomous cars constantly assess their environment requiring wireless communication transceivers and radars
- › Motivates designing these functionalities jointly
- › Dual-function radar communication (DFRC) systems:
  - Size and cost reduction
  - Facilitate coexistence
  - Reduce spectral congestion

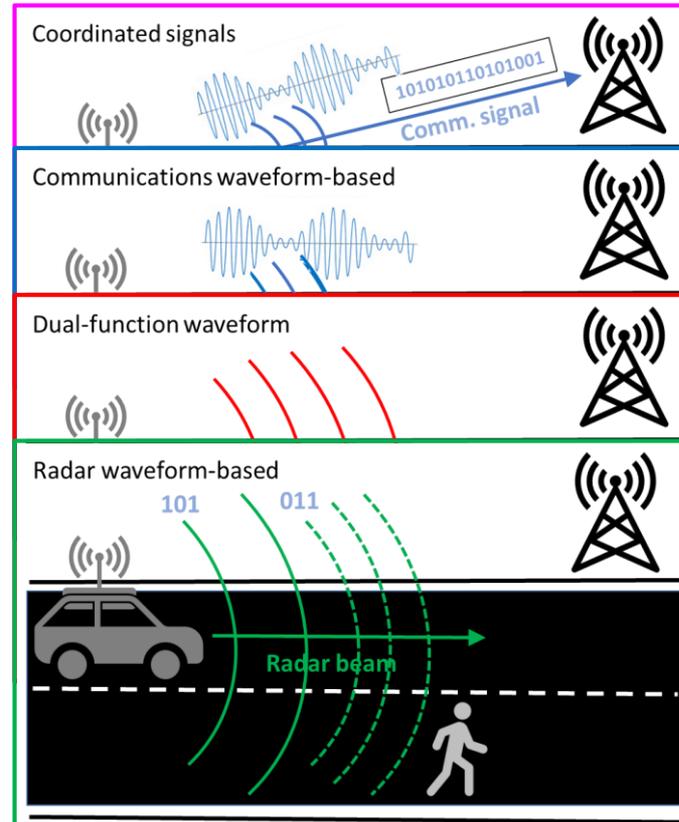


# DFRC Strategies

> Ma et al. SPMag 20

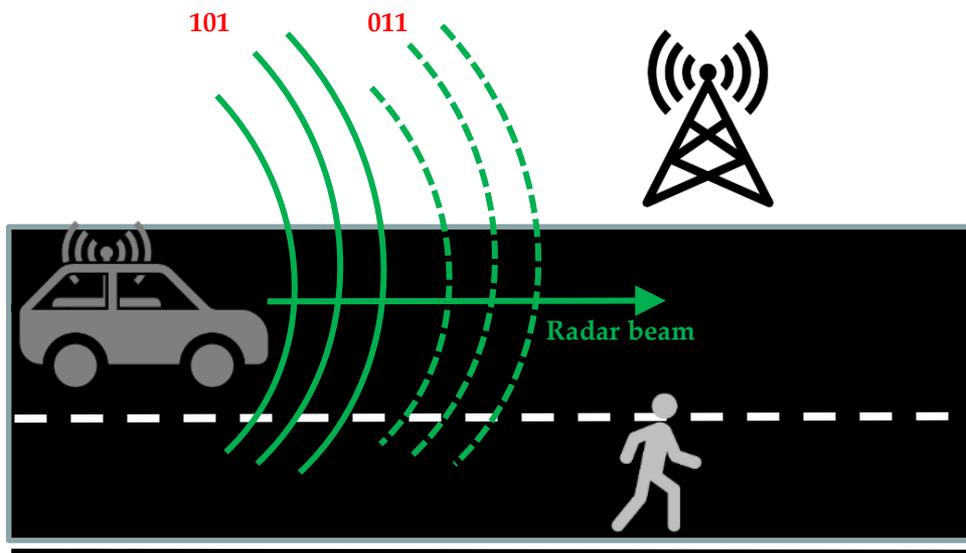
Leading design approaches:

- > Separate coordinated signals
  - > Beamform / orthogonalization
- > Communication waveform
  - > OFDM radar
- > Dual-function waveform
  - > Dedicated design
- > Radar waveform
  - > Embed message



# Embedding Information in Radar Waveforms

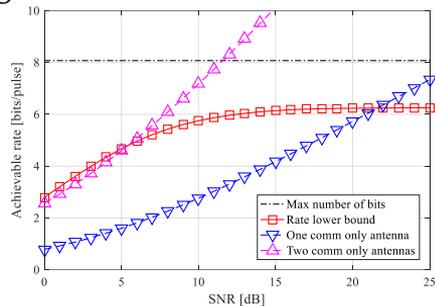
- › Convey digital messages with radar signals:
  - › Embed bits in the waveform parameters
  - › Index modulation: Frequencies, antenna elements
- › Benefits
  - › Use conventional radar signals
  - › Minimal radar degradation
- › Drawbacks
  - › Limited bit rates
  - › Challenging decoding



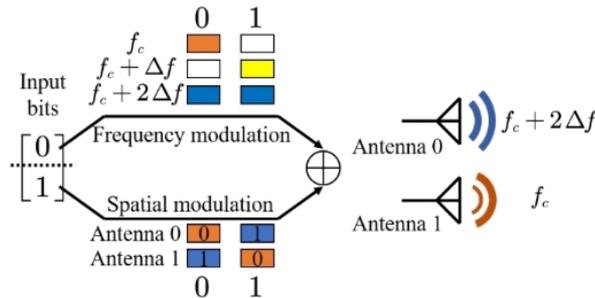
# MAJoRCom: Multi-carrier Agile Joint Radar Communications

> Huang et al. 20

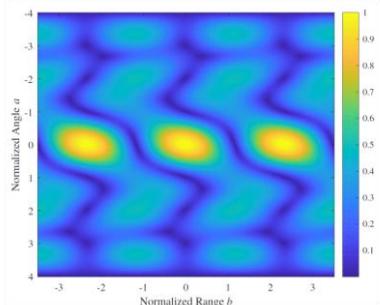
- > Use only radar waveforms
- > Embed information in:
  - > Frequency selection
  - > Antenna allocation
- > Spectrally efficient:
  - Upper bound
  - Lower bound
  - One dedicated antenna
  - Two dedicated antennas
- > Angular resolution:



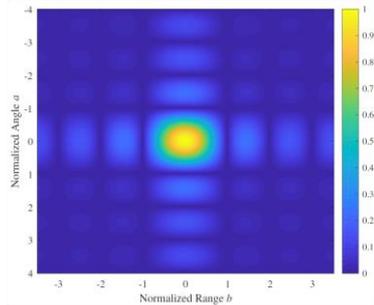
Comparable to using dedicated comm. antennas *without affecting radar*



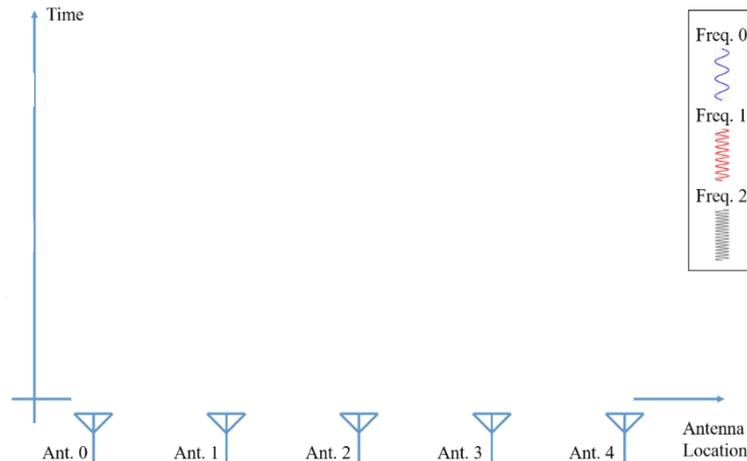
- > Angular resolution:



Instantaneous



Expected



# SpaCoR: Spatial Modulation Based Communication-Radar

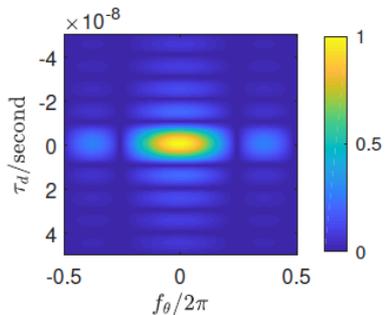
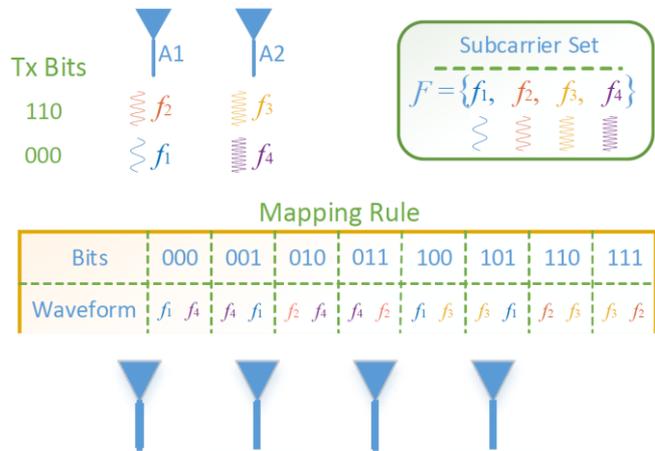
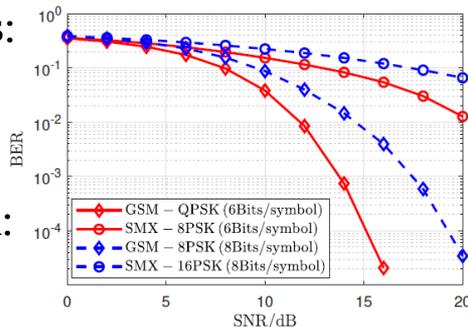
> Ma et al. 20

➤ Orthogonal transmissions:

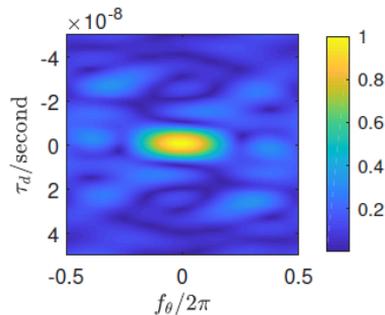
- Distinct bands
- Distinct antennas

➤ Toggle antenna allocation:

- Spatial modulation
- Spatial agility
- Improved resolution and throughput



(a) Full Antenna Array

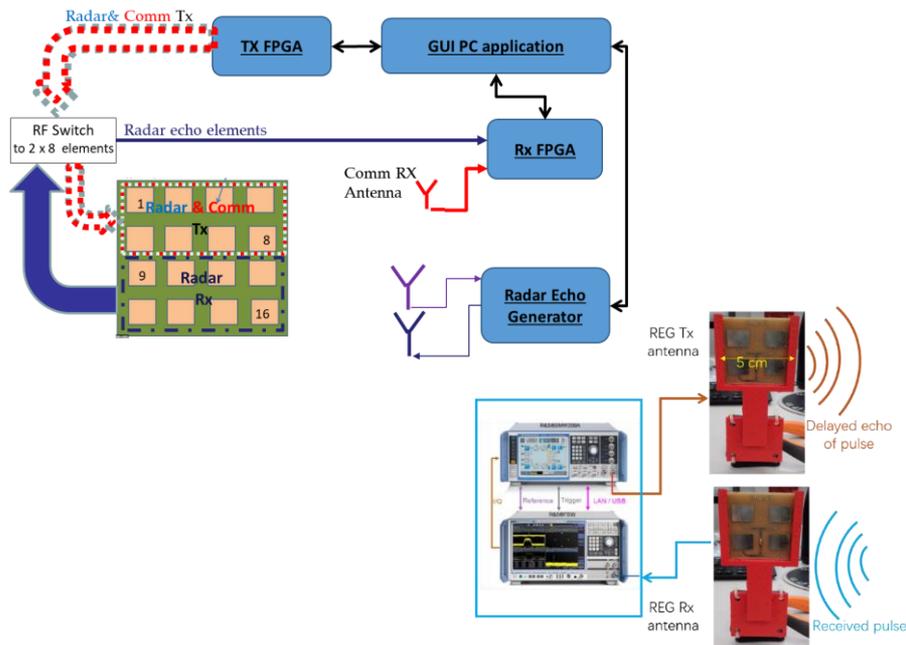


(b) SpaCoR

$m = 0$     $m = 1$     $m = 2$     $m = 3$

# Hardware Prototype

- Using over-the-air signaling
- 16 antenna elements
- Radar echo generator (REG)

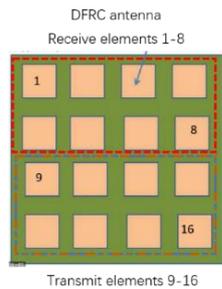
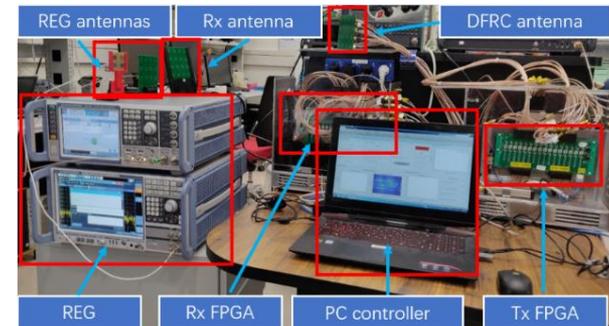


מכון ויצמן למדע  
WEIZMANN INSTITUTE OF SCIENCE

清华大学  
Tsinghua University

## Joint Radar and Communication System Prototype Based on Generalized Spatial Modulation

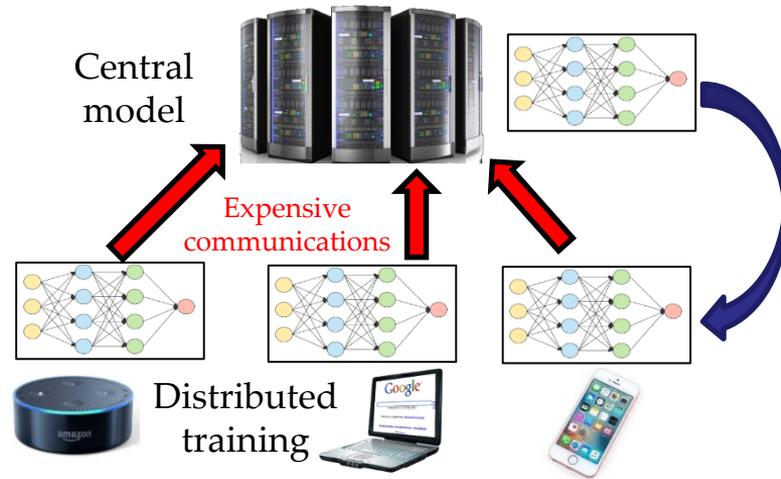
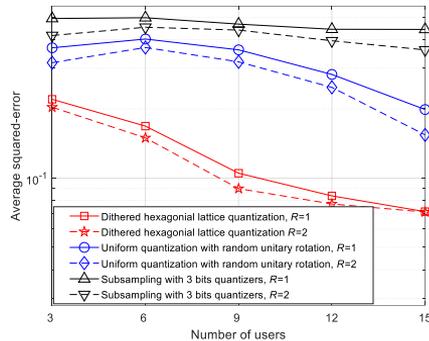
SX-MPL  
Signal Acquisition Modeling and Processing Lab



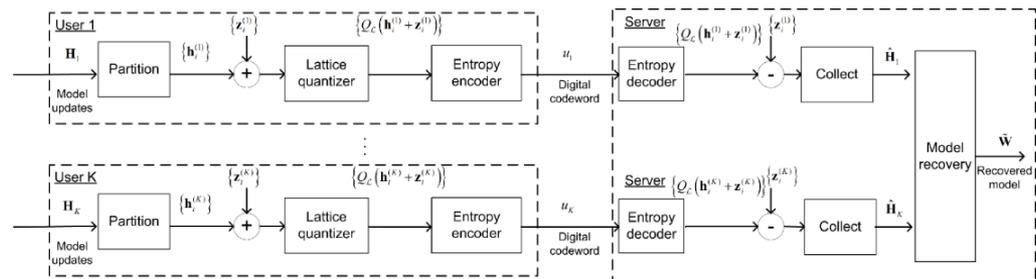
# Task-Based Quantization for Federated Learning

> Shlezinger, Chen, Eldar, Poor, Cui, 19

- > Train on edge devices
- > Quantize model updates
- > Aggregate quantized weights



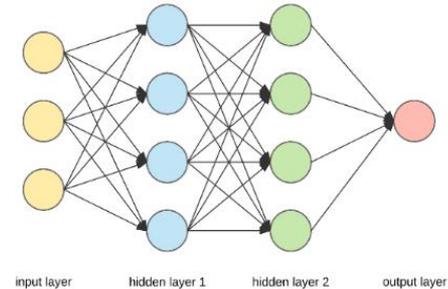
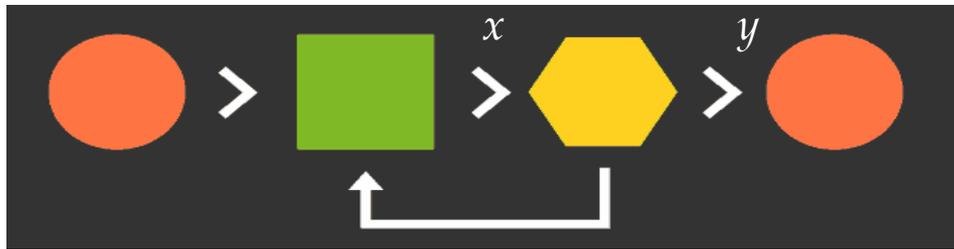
Reliable centralized model with less communication



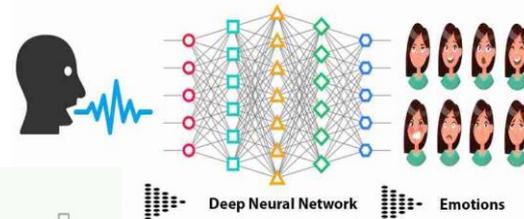


## Part 3:

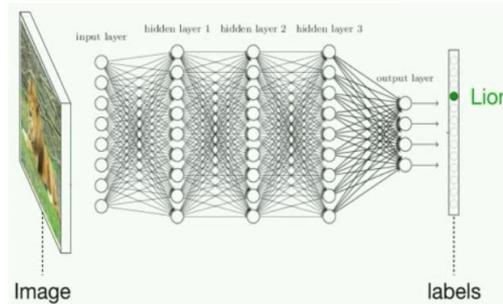
# Model-based deep learning



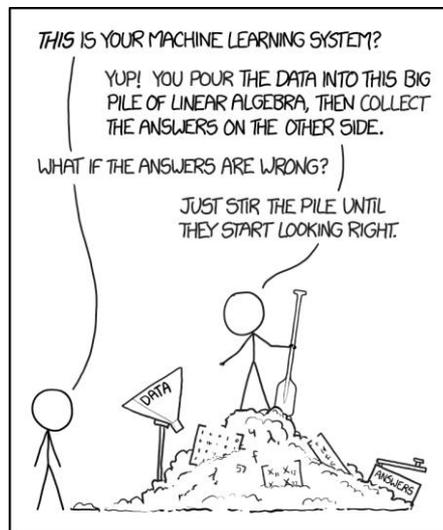
# Black-Box Deep Learning



- Deep neural networks (DNNs) achieve superior performance in:
  - Computer vision
  - Speech processing
  - Problems which are hard to tackle with models



- Challenges:
  - Large training sets
  - Interpretability?
  - Robustness?
  - Generalization limited
  - Generic architectures

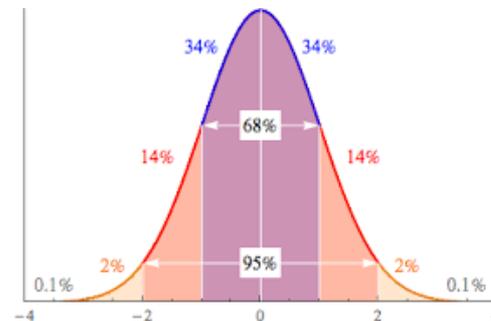
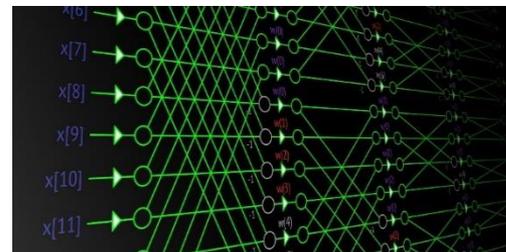


# Model Based Signal Processing

- › Signal processing is based on modeling
- › Can incorporate domain knowledge and structure
- › Allows inference from relatively small amounts of data
- › Analytical techniques to assess quality of the output

## However:

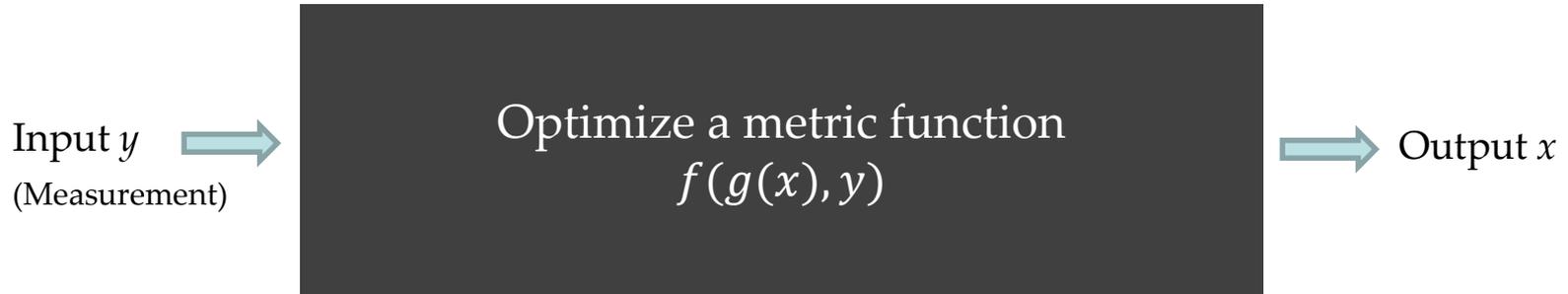
- › Requires accurate model knowledge
- › Inference can be slow



**Combining model-based algorithms and deep learning:  
Compact, interpretable, and simple to train data-driven systems!**

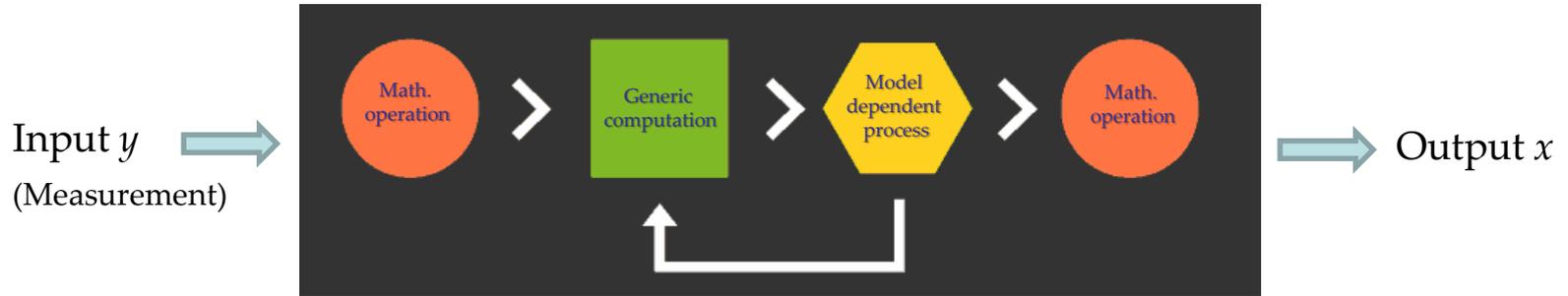
# Model-Based vs. Deep Learning

- > Model-based signal processing:

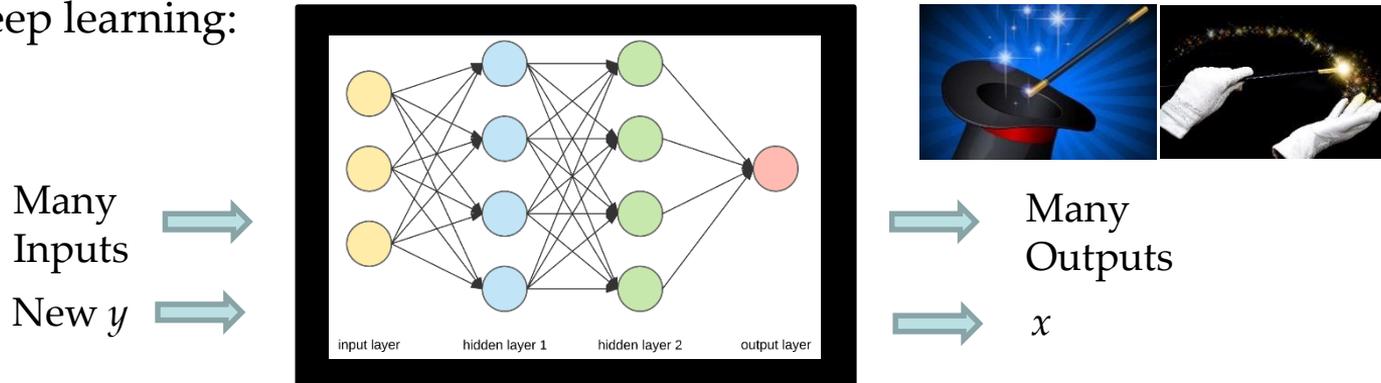


# Model-Based vs. Deep Learning

- > Model-based signal processing:

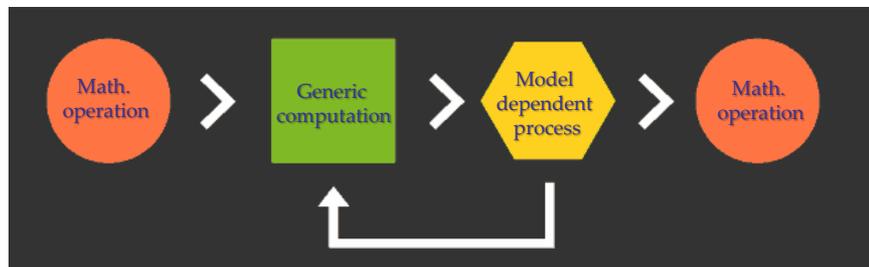


- > Deep learning:

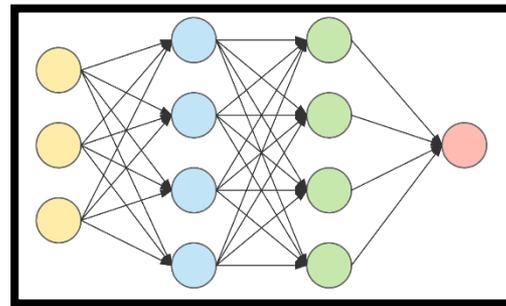


# Model-Based Deep Learning

› Model-based signal processing:



› Deep learning:



› How to combine?



1. Integrate model-based algorithms into deep networks

**Deep unfolding / unrolling**

2. Integrate deep networks into model-based algorithms

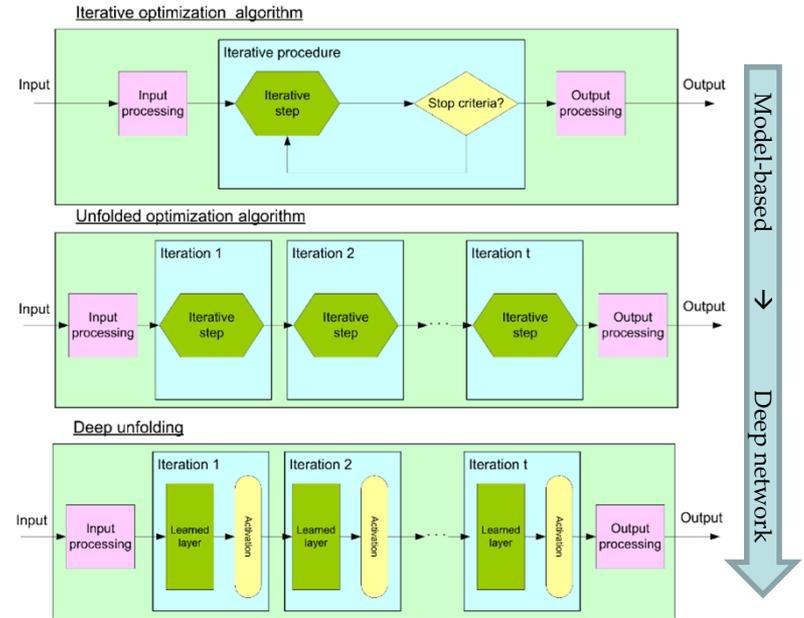
**Data-driven hybrid algorithms**



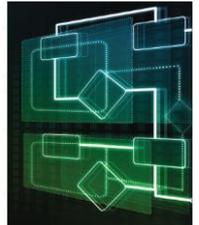
# Deep Unfolding

> Gregor and LeCun 10; Hershey, Le Roux, and Weininger 14

- Deep networks inspired by iterative model-based algorithm:
  - Unfold iterations into layers
  - Learn parameters of the layer from data
  - Model-driven network
- Benefits:
  - Faster convergence
  - Less trainable parameters
  - Interpretable network
  - Better performance from less training data



Vishal Monga, Yuelong Li, and Yonina C. Eldar



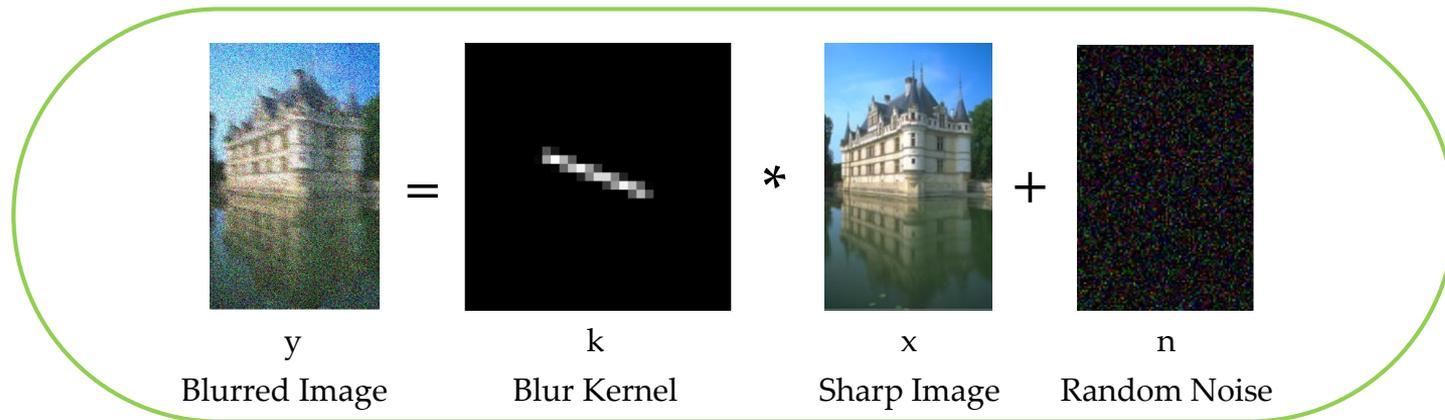
Recent review in SP Magazine

**Algorithm Unrolling**

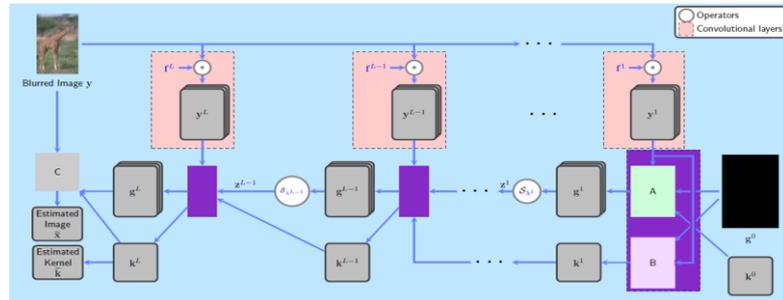
Interpretable, efficient deep learning for signal and image processing

# DUBLID: Deep Unrolling for Blind Deblurring

> Li, Tofighi, Monga and Eldar, 19



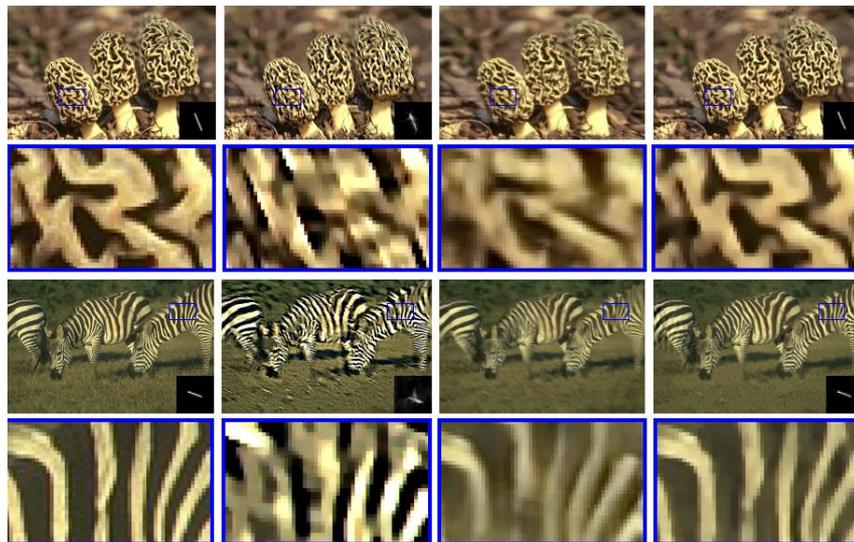
- > Many deblurring methods based on optimization (e.g. total variation)
- > We perform total variation in the gradient domain  $\nabla \mathbf{y} \approx \mathbf{k} * \nabla \mathbf{x}$
- > We solve the problem by a variable splitting approach and then unfold



# Deblurring Results

> Li, Tofighi, Monga and Eldar, 19

- > Training based on BSDS500 dataset
- > Blur kernels of linear motion with different lengths and angles



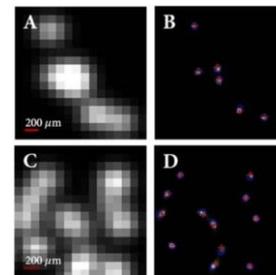
(a) truth (b) Perrone *et. al* (c) Nah *et. al* (d) DUBLID

**Superior performance, parameter free and computational benefits. All code available online.**

# Super-resolution via Deep Learning

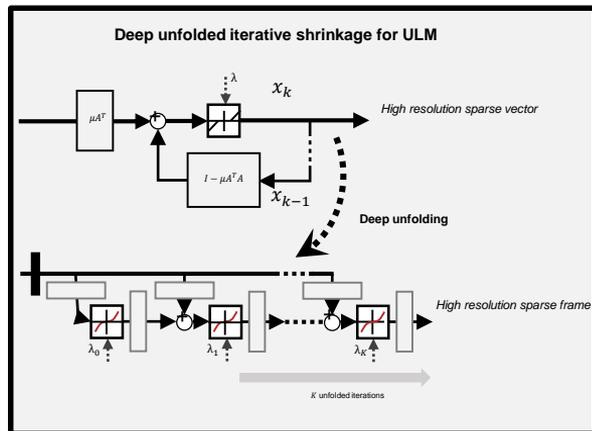
> Van Sloun et. al. 2018

- Resolve overlapping bubbles via deep network scheme
  - Improved performance over sparse recovery methods
  - Faster execution time
- Relies on a learned ISTA approach via unrolling

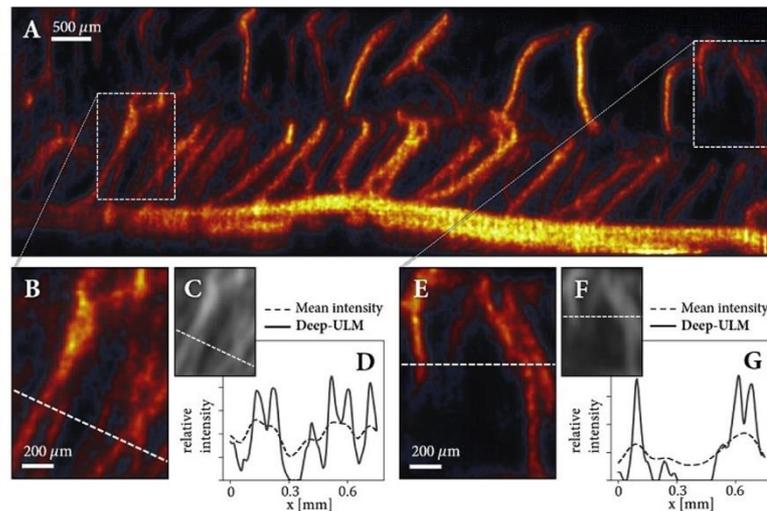


## ➤ Cost function:

$$\|f(x|\theta) - G * y\|_2^2 + \lambda \|f(x|\theta)\|_1$$



## Super-resolution of rat spinal cord vasculature

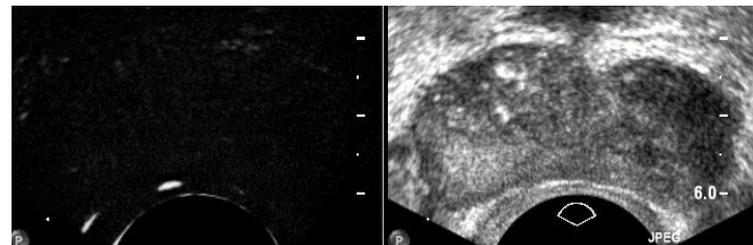


# Removing Tissue Background via Deep Learning

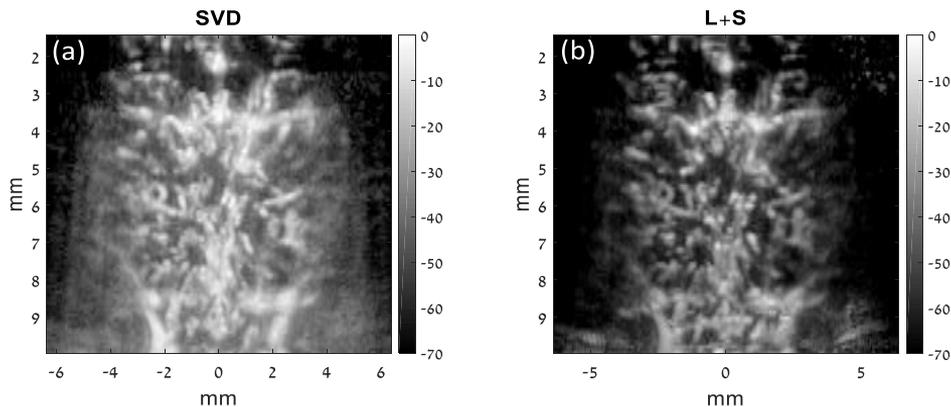
## CORONA: Convolutional rObust pRincipal cOmpoNent Analysis

> Solomon et. al. 2018

- > Blood signal is cluttered by unwanted tissue
- > We use the model:
  - low rank (background) +
  - sparse (contrast signal)
- > Use model based deep learning
- > Improved performance in terms of noise, frame rate



In-vivo contrast rat brain scan



INVITED  
PAPER

Van Sloun, Cohen, Eldar

## Deep Learning in Ultrasound Imaging

*This article provides an overview of use of deep, data-driven learning strategies in ultrasound systems, from the front-end to advanced applications. The authors discuss the use of these new computational approaches in all aspects of ultrasound imaging, ranging from ideas that are at the interface of raw signal acquisition (including adaptive beam forming) and image formation, to learning compressive codes for color Doppler acquisition to learning strategies for performing clutter suppression.*

By RUUD J. G. VAN SLOUN<sup>1</sup>, Member IEEE, REGEV COHEN, Graduate Student Member IEEE, AND YONINA C. ELДАР<sup>2</sup>, Fellow IEEE

**ABSTRACT** | In this article, we consider deep learning strategies in ultrasound systems, from the front end to advanced applications. Our goal is to provide the reader with a broad understanding of the possible impact of deep learning methodologies on many aspects of ultrasound imaging. In particular, we discuss methods that lie at the interface

### INTRODUCTION

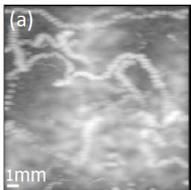
Diagnostic imaging plays a critical role in healthcare, serving as a fundamental asset for timely diagnosis, disease staging, and management, as well as for treatment choice, planning, guidance, and follow-up. Among the diagnostic imaging options, ultrasound imaging [1] is

# DL for Clutter Suppression

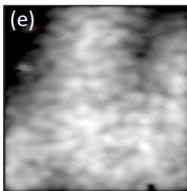
## Low-rank + sparse model (L+S, RPCA)

$$\min_{\mathbf{L}, \mathbf{S}} \frac{1}{2} \|\mathbf{D} - \mathbf{L} - \mathbf{S}\|_F^2 + \lambda_1 \|\mathbf{L}\|_* + \lambda_2 \|\mathbf{S}\|_{1,2}$$

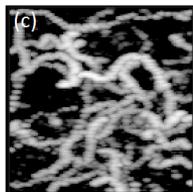
Data



Low-rank tissue clutter



Sparse MBs

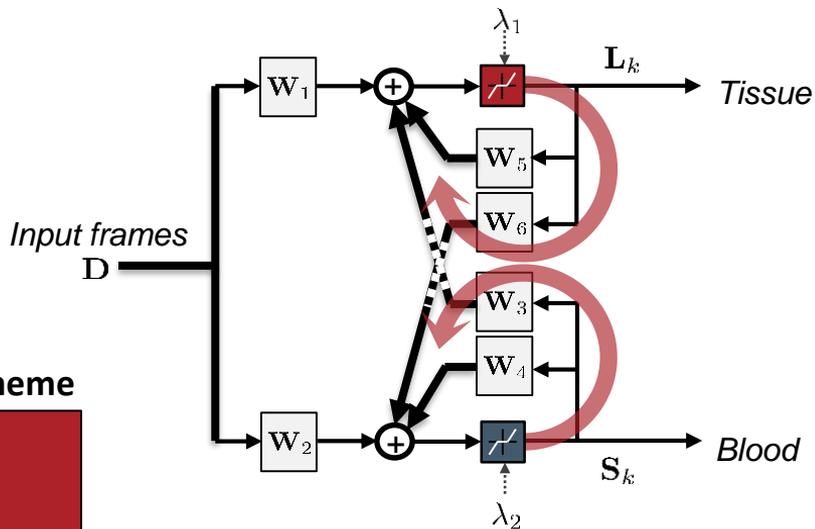


## Iterative proximal gradient scheme

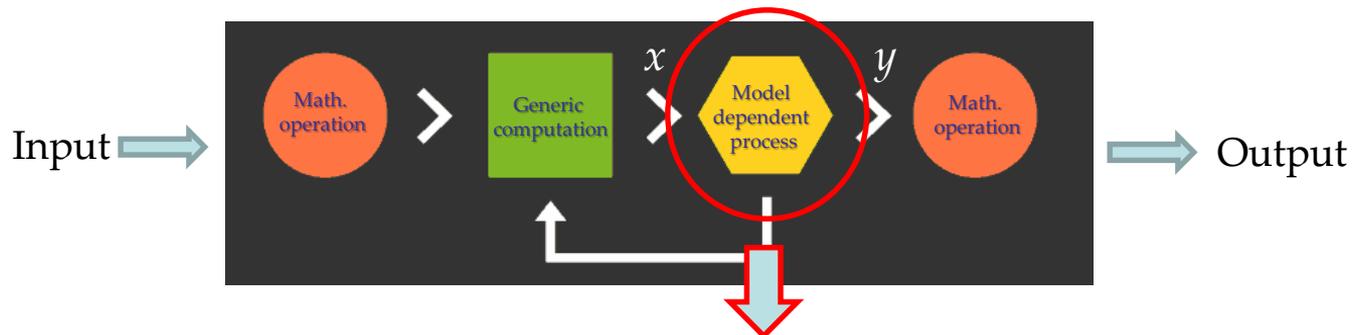
$$\mathbf{L}^{k+1} = \text{SVT}_{\lambda_1/2} \left( \frac{1}{2} \mathbf{L}^k - \mathbf{S}^k + \mathbf{D} \right)$$

$$\mathbf{S}^{k+1} = \mathcal{T}_{\lambda_2/2} \left( \frac{1}{2} \mathbf{S}^k - \mathbf{L}^k + \mathbf{D} \right)$$

## ISTA for RPCA

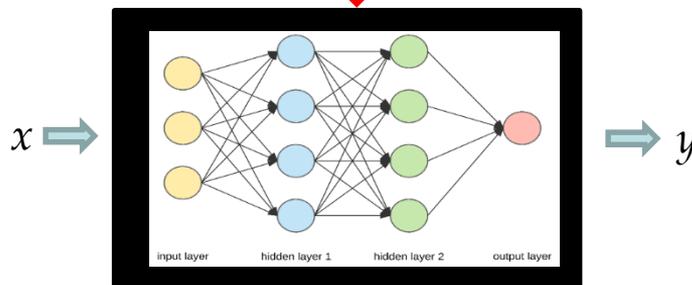


# Data Driven Hybrid Algorithms



## Advantages:

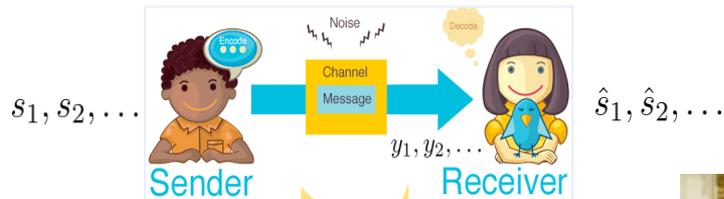
- › Limited training data
- › Maintain optimality when no uncertainty
- › Allows for model distortions
- › Once trained, easy computation



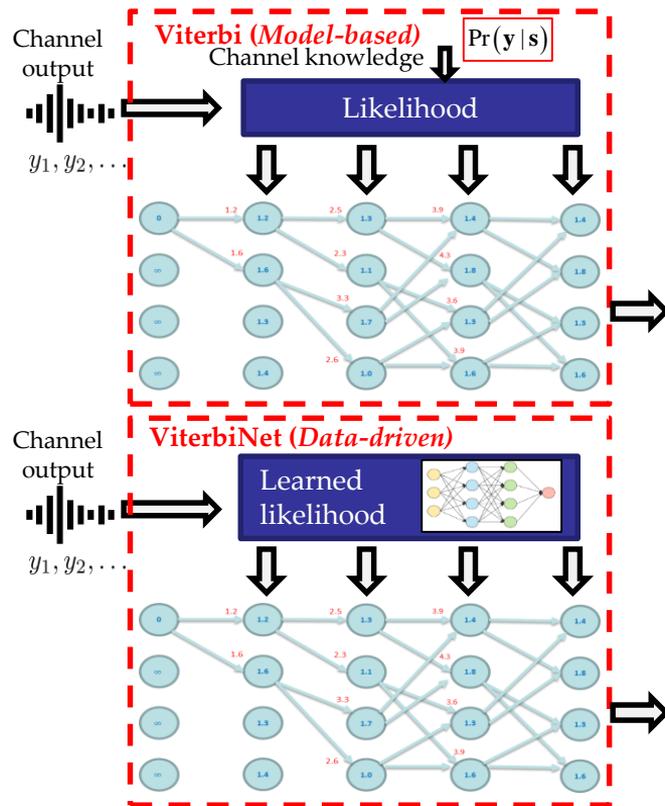
Recent review: Nariman et. al, "Data-Driven Symbol Detection via Model-Based Machine Learning"

# Viterbinet: Symbol Detection with Unknown Channels

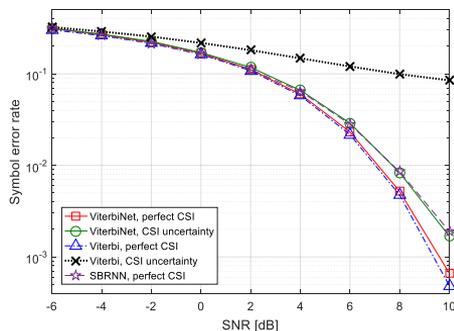
> Shlezinger, Farsad, Eldar and Goldsmith 19



- > Viterbi detection algorithm
- > Requires channel knowledge
- > Viterbinet: Model based deep detection
- > Unknown computations → DNNs



Optimal symbol detection from minimal training

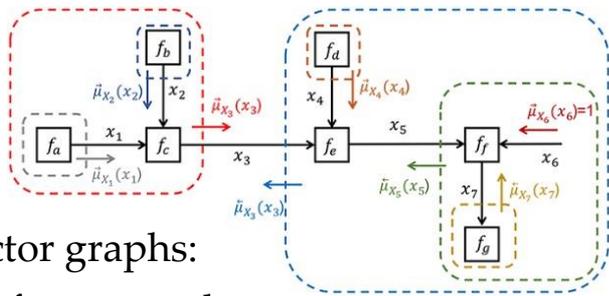


# Data-Driven Factor Graph Methods

> Shlezinger, Farsad, Eldar and Goldsmith 20

> A family of signal processing algorithms

- Represent distribution as graph
- Message passing

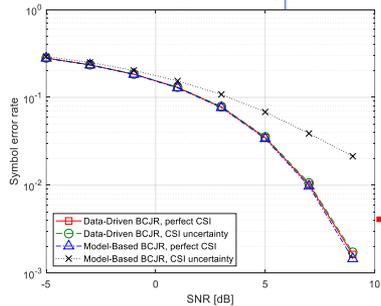
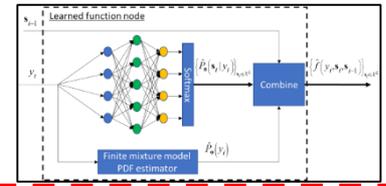
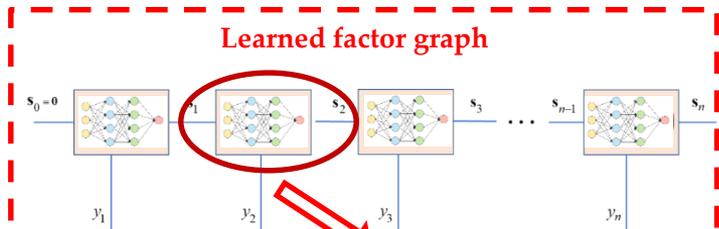
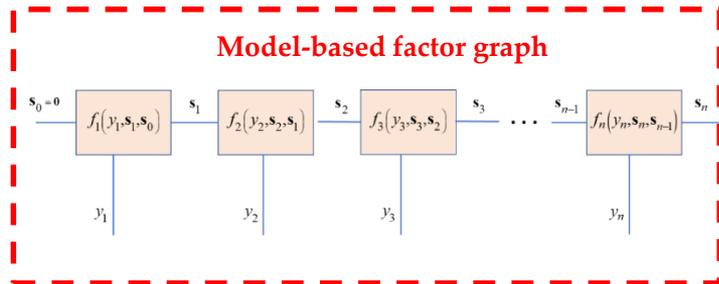


> Data-driven factor graphs:

- Learn the factor graph
- Message passing over graph

> Example: BCJRnet

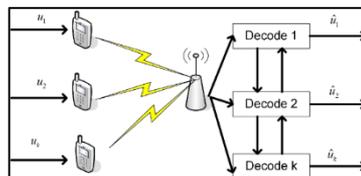
- Learned BCJR detector:



Learned MAP symbol detection

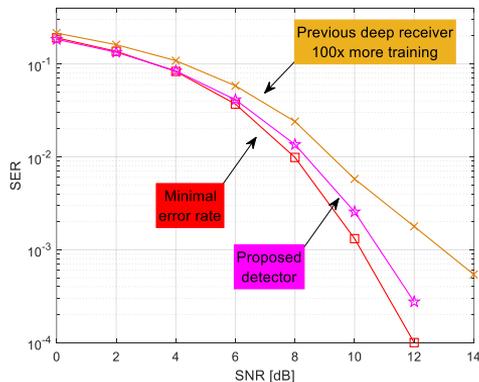
# DeepSIC: Deep Soft Interference Cancellation for Massive MIMO

> Massive MIMO symbol detection

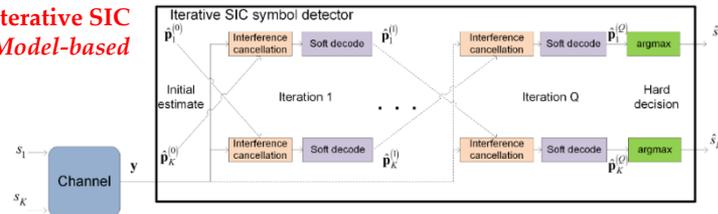


> Shlezinger, Fu and Eldar 19

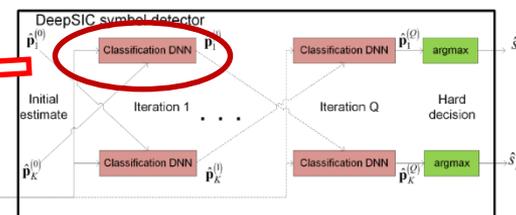
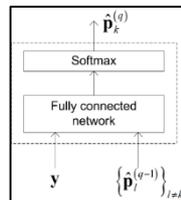
> Learn how to cancel interference



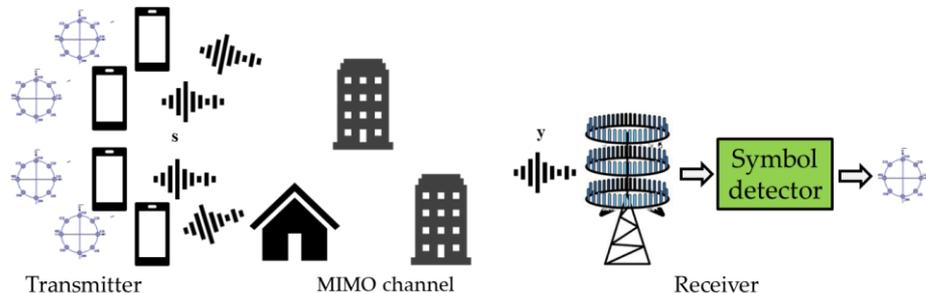
**Iterative SIC**  
*Model-based*



**DeepSIC**  
*Data-driven*



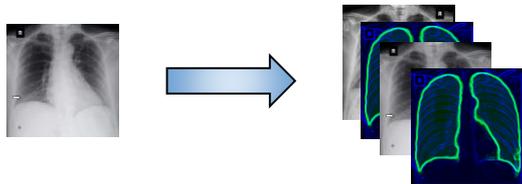
**No channel knowledge**  
**Applicable in non-linear channels**



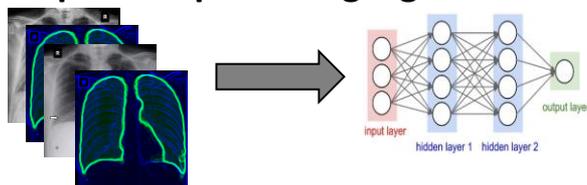
# COVID19 Task Force

- Put together a task force of 4 hospitals and AI experts
- COVID19 detection using Xray: Over 90% detection rate! (PCR achieves 70%)
- Based on model-based features
- Starting to deploy in Beilinson
- Next steps in project including postcovid

## Step 1: Pre-processing + Segmentation



## Step 2: Deep learning algorithm



## COVID-19 Classification of X-ray Images Using Deep Neural Networks

Elisha Goldstein<sup>1\*</sup>, Daphna Keidar<sup>2\*</sup>, Daniel Yaron<sup>3\*</sup>, Yair Shachar<sup>4</sup>, Ayelet Blass, Leonid Charbinsky MD<sup>5</sup>, Israel Aharony MD<sup>5</sup>, Liza Lifshitz MD<sup>5</sup>, Dimitri Lumelsky MD<sup>5</sup>, Ziv Neeman MD<sup>5</sup>, Matti Mizrahi MD<sup>6</sup>, Majd Hajouj MD<sup>6</sup>, Nethanel Eizenbach MD<sup>6</sup>, Eyal Sela MD<sup>6</sup>, Chedva S Weiss MD<sup>7</sup>, Philip Levin MD<sup>7</sup>, Ofer Benjaminov MD<sup>7</sup>, Gil N Bachar MD<sup>8</sup>, Shlomit Tamir MD<sup>8</sup>, Yael Rapson MD<sup>8</sup>, Dror Suhami MD<sup>8</sup>, Amiel A Dror MD PhD<sup>8</sup>, Naama R Bogot MD<sup>7</sup>, Ahuva Grubstein MD<sup>9</sup>, Nogah Shabshin MD<sup>5</sup>, Yishai M Elyada PhD<sup>9</sup>, Yonina C Eldar PhD<sup>3</sup>



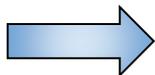
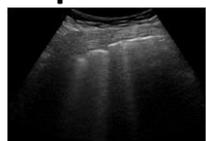
# COVID19 Task Force

- > Collaboration with Prof. Libertario Demi et. al
- > COVID19 detection from LUS + severity grading
- > Based on model-based features
- > Close to 80% detection

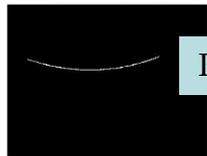
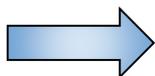


IEEE TRANSACTIONS ON MEDICAL IMAGING, PREPRINT – UNDER REVIEW

## Step 1: Line Detection



B-lines

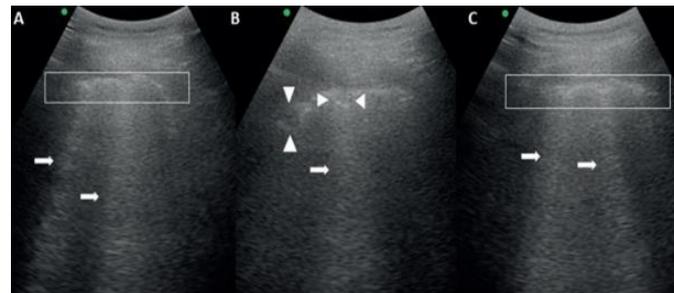
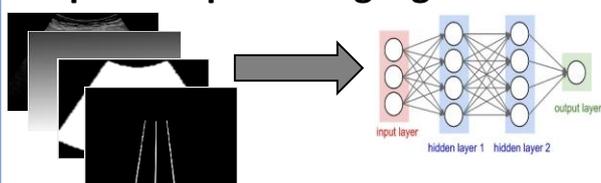


Pleural line

## A Framework for Integrating Domain Knowledge into Deep Networks for Lung Ultrasound, and its Applications to COVID-19

Oz Frank, Nir Schipper, Mordehay Vaturi, Gino Soldati, Andrea Smargiassi, Riccardo Inchingolo, Tiziano Perrone, Federico Mento, Libertario Demi, *Member, IEEE*, Meirav Galun, Yonina C. Eldar, *Fellow, IEEE*, and Shai Bagon

## Step 2: Deep learning algorithm



# Efficient, Interpretable, High Resolution Sensing: Results and Vision

To learn more from less data we must take advantage of all the information possible!

Exploit structure and goal in model based and data driven methods

## Mathematical limits:

Sampling rates  
Coding rates  
Superresolution limits

## Engineering Research:

Development of new samplers  
Technological applications  
that break existing barriers

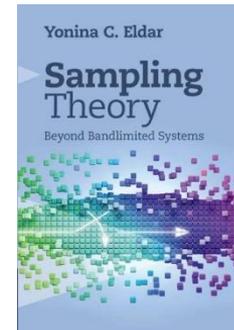
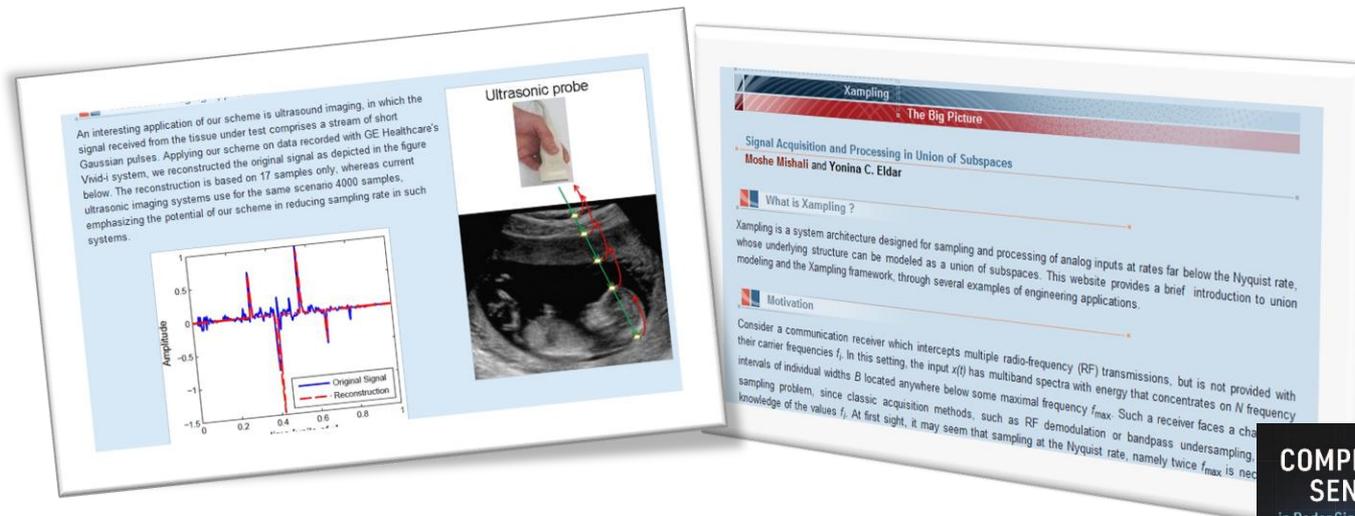
## Scientific/clinical breakthroughs:

Thanks to the possibility of  
seeing what we could  
not see before ...



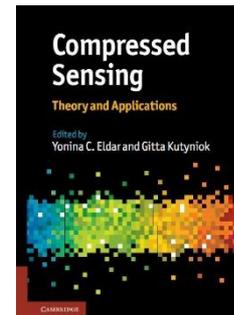
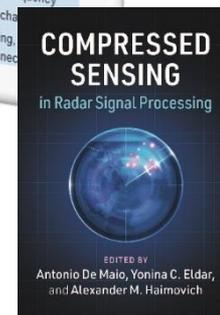
# Visit Our Webpage

Y. C. Eldar, "Sampling Theory: Beyond Bandlimited Systems", Cambridge University Press, 2015



Y. C. Eldar and G. Kutyniok, "Compressed Sensing: Theory and Applications", Cambridge University Press, 2012

A. D. Maio, Y. C. Eldar and A. M. Haimovich, "Compressed Sensing in Radar Signal Processing", Cambridge University Press, 2019



<http://www.wisdom.weizmann.ac.il/~yonina/YoninaEldar>



*If you want to go fast go alone  
If you want to go far bring others*

# Collaborators (Partial...)



**Miguel Rodrigues**



**Andrea Goldsmith**



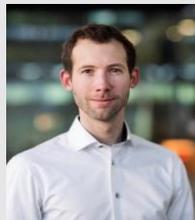
**David Smith**



**Alon Kipnis**



**Shai Tejman-Yarden**



**Ruud Van Sloun**



**Vishal Monga**



**Nir Shlezinger**

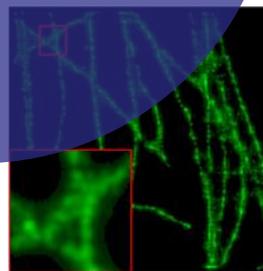
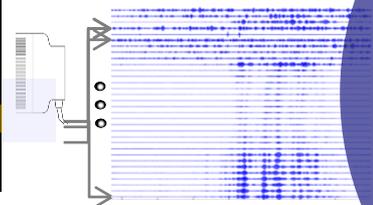
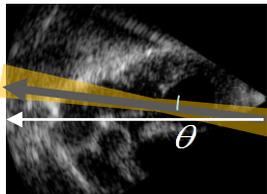
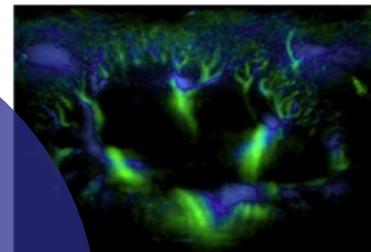


**Tianyao Huang**



**Geert Leus**

# Thank You!



If you found this interesting ...  
Looking for graduate students  
and post-docs!