# RESHORING, AUTOMATION, AND LABOR MARKETS UNDER TRADE UNCERTAINTY

#### HAMID FIROOZ, SYLVAIN LEDUC, AND ZHENG LIU

ABSTRACT. We study the implications of trade uncertainty for reshoring, automation, and U.S. labor markets. Rising trade uncertainty creates incentives for firms to reduce exposure to foreign suppliers by moving production and distribution processes to domestic producers. However, we argue that reshoring does not necessarily bring jobs back to the home country or boost domestic wages, especially when firms have access to labor-substituting technologies such as automation. Automation improves labor productivity and facilitates reshoring, but it can also displace jobs. Furthermore, automation poses a threat that weakens the bargaining power of unskilled workers in wage negotiations, depressing their wages and raising the skill premium and wage inequality. Our model predictions are in line with industry-level empirical evidence.

#### I. Introduction

The COVID-19 pandemic has exposed important vulnerabilities in global supply chains. Ongoing trade tensions as well as increasing risks from climate change and geopolitical conflicts are making global production strategies riskier than in the past. In this new economic environment, moving some production and distribution processes from abroad back to domestic suppliers (i.e., reshoring) is becoming an increasingly attractive option to mitigate the risks of supply chain disruptions.<sup>1</sup>

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Firooz: University of Rochester; email: hfirooz@ur.rochester.edu. Leduc: Federal Reserve Bank of San Francisco; email: Sylvain.Leduc@sf.frb.org. Liu: Federal Reserve Bank of San Francisco; email: Zheng.Liu@sf.frb.org. We are grateful to our discussants Federico Mandelman and Eugenia Gonzalez-Aguado at the 2024 NBER International Seminar on Macroeconomics for their helpful comments and suggestions. We also thank Nick Bloom, Steve Davis, Jordi Gali, Ricardo Reis, Joe Steinberg, Linda Tesar, Ken West, David Wiczer, and seminar participants in the 2024 NBER ISoM, the Federal Reserve Bank of San Francisco, the 2024 SITE conference on macro uncertainty and volatility, and Santa Clara University for helpful comments. We thank Deepika Baskar Prabhakar for excellent research assistance and Anita Todd for editorial assistance. The views expressed herein are those of the authors and do not necessarily reflect the views of the Federal Reserve Bank of San Francisco or of the Federal Reserve System.

<sup>1</sup>According to a Thomas Industrial Survey, about two-thirds of North American manufacturers reported they are likely to bring manufacturing production and sourcing back to North America because of concerns

How this process will unfold and what the impacts on labor markets will be remain highly uncertain. One possibility is that reshoring could increase jobs in the home country and boost wages for domestic workers, reversing the effects of the China shock originally studied by Autor et al. (2013). In this paper, we argue that reshoring may not necessarily increase domestic employment and wages when labor-substituting technologies, such as automation, are available for firms to lower labor costs.

Over the past three decades, advanced economies that offshored production processes have also experienced a steady increase in the adoption of automation technologies, such as artificial intelligence, machine learning, and robotics. Empirical evidence suggests that automation raises labor productivity (Graetz and Michaels, 2018) and reduces unit labor costs and worker wages (Acemoglu and Restrepo, 2020). The increased ability to automate labor-intensive production processes could reduce firms' need to offshore production to contain labor costs. In line with these changing incentives, import growth has slowed significantly relative to GDP since the trade collapse during the Great Recession.

Coupled with a greater ability to automate, recent increases in trade uncertainty may have accelerated the trend in reshoring. While reshoring tends to raise domestic labor demand and real wages, firms' options to automate help mitigate the increase in labor costs, since it acts as a threat against workers—especially unskilled workers who can be easily substituted by robots—in wage bargaining. This automation threat channel—originally studied by Leduc and Liu (2023)—helps contain the rise in labor costs, reinforcing the incentive for reshoring. Since robots substitute for unskilled workers and complement skilled workers, increased automation spurred by reshoring may also raise the skill premium and income inequality.

In this paper, we formalize this perspective by developing a macro framework featuring automation, heterogeneous worker skills, and international trade frictions. We use this framework to examine the impacts of a rise in trade uncertainty on reshoring, automation, and domestic labor markets. We generalize the automation threat channel in the Leduc and Liu (2023) model to a small open economy with trade in intermediate inputs. Trade is subject to time-varying iceberg costs with stochastic volatility meant to capture trade uncertainty arising from geopolitical, climate, and trade policy risks. To produce a final good, firms use a mixture of domestic and foreign intermediate goods. We capture the interaction between reshoring and automation by assuming that domestic intermediate goods producers can use two types of technologies: a labor-only technology that uses unskilled workers and an automated process that uses both robots and skilled workers as inputs.<sup>2</sup>

about the global supply chain disruptions following the COVID-19 pandemic. In addition, about a quarter of those manufacturers are considering expanding industrial automation.

<sup>&</sup>lt;sup>2</sup>We focus on automation decisions at the business cycle frequency. However, automation can also be the result of long-run technological improvements that can allow the automation of tasks previously done

We assume that unskilled workers search for jobs in a frictional labor market, subject to search frictions as in the standard Diamond-Mortensen-Pisarides (DMP) framework. Unskilled wages are determined by Nash bargaining between a firm and a worker. Because firms have the option to automate unfilled vacancies, the threat of automation acts as an outside option for the firm and weighs on bargained wages.<sup>3</sup> This effect is compounded when firms do actually automate, since the associated productivity boost lowers domestic marginal costs of production further.

In our framework, heightened trade uncertainty operates through three key channels. First, trade uncertainty has an expenditure-switching effect that redirects the demand for intermediate goods toward domestic producers (i.e., reshoring).<sup>4</sup> This expenditure-switching effect stimulates automation investment, raising the demand for skilled workers. While a greater use of automated processes has a job-creating effect through raising the value of unfilled vacancies, this channel is more than offset by the job-displacing effect of automation on unskilled workers. Second, trade uncertainty also generates greater precautionary savings, which reduces the real interest rate and further stimulates automation. Third, heightened trade uncertainty raises the option value of waiting, discouraging automation investment.

We show that, with our calibration, the positive effects from expenditure switching and precautionary savings dominate the negative option-value effect, such that trade uncertainty boosts automation, raises unemployment for unskilled workers, and also raises the skill premium. These effects of trade uncertainty are amplified for an economy that is more open to trade, has more automated production, or faces more persistent trade uncertainty.

Our model produces a rich set of empirically testable predictions. First, the model predicts that an increase in trade uncertainty increases reshoring and stimulate automation investment. Second, increased automation triggered by trade uncertainty raises labor productivity. Third, the threat of automation depresses wages and employment of unskilled workers while raising wages of skilled workers, resulting in an increase in the skill premium. These effects should be stronger in an economy more open to international trade.

by labor. We view this form of automation as occurring relatively infrequently and instead focus on an environment with fixed production technologies.

<sup>&</sup>lt;sup>3</sup>Unlike the standard DMP framework, we assume that vacancy creation incurs a random fixed cost (Fujita and Ramey, 2007; Leduc and Liu, 2020), such that an unfilled vacancy retains value in equilibrium and captures the firms' outside option and ability to automate in the future.

<sup>&</sup>lt;sup>4</sup>To keep the analysis tractable, we model reshoring or offshoring in a reduced-form way. We do not model firms' choices of production locations. We interpret importing of intermediate goods as production that could have been done domestically but is instead *offshored*. Similarly, we interpret a decline in imports of intermediate goods as *reshoring*.

The model predictions are consistent with empirical evidence from industry-level data. We use data on industrial robots, intermediate goods imports, employment, value-added, and wages in two-digit North American Industry Classification System (NAICS) industries to construct measures of automation, offshoring, labor productivity, and the skill premium.<sup>5</sup> We measure trade uncertainty using aggregate trade policy uncertainty (TPU) constructed by Caldara et al. (2020), interacted with a measure of initial exposure to offshored production. We show that, controlling for industry and time fixed effects, an increase in trade uncertainty is associated with larger increases in automation and larger declines in offshoring in industries that are more exposed to offshoring.<sup>6</sup>

We also find that an increase in trade uncertainty is associated with larger increases in labor productivity and the skill premium in industries that are more exposed to offshoring and that these effects work partly through an automation channel. We examine the channeling effects using a two-stage least squares approach (Bertrand and Mullainathan, 2001). In the first stage, we regress a measure of automation (robot density) on trade uncertainty, controlling for industry and time fixed effects. In the second stage, we regress each variable of interest (including labor productivity, employment, value-added, and the skill premium) on robot density predicted from the first-stage regression. The estimated coefficient in the second-stage regression indicates the sensitivity of each of the macroeconomic variables to changes in robot density that comes from trade policy uncertainty. We find that an increase in robot density driven by trade uncertainty is associated with an increase in both labor productivity and the skill premium. The increase in labor productivity primarily reflects a

<sup>&</sup>lt;sup>5</sup>Due to data limitations, this paper focuses on industrial robots, a specific type of automation technology. We use the terms "automation" and "robots" interchangeably. Robotics constitute an important component of the automation technology. According to the Annual Business Survey, 8.7% of U.S. manufacturing firms, which account for 45% of manufacturing employment, utilize robotics in their production processes (Acemoglu et al., 2022).

<sup>&</sup>lt;sup>6</sup>Our model's prediction that trade uncertainty raises automation investment does not necessarily contradict the empirical finding of Caldara et al. (2020) that trade uncertainty reduces business investment (such as nonresidential structures and general capital equipment). It would be straightforward to generalize our model to incorporate business investment. For example, one could modify the traditional technology (i.e., the non-automation technology) that uses unskilled labor as the only input in our baseline model by assuming that both capital and labor are required as input factors. We conjecture that, in such a model, an increase in trade uncertainty could boost automation investment, which in turn could displace unskilled jobs and reduce business investment, in line with the findings of Caldara et al. (2020).

decline in employment (rather than an increase in value-added), suggesting that automation raises labor productivity through substituting for workers.<sup>7</sup>

Our work contributes to a relatively new but growing literature on the effects of reshoring. Empirically, drawing clear conclusions about the effects of reshoring has been challenging given the novelty of the practice and thus the lack of data. Nonetheless, a few papers have assessed the empirical links between reshoring and automation. For instance, Dachs et al. (2019) find a positive relationship between reshoring and investment in Industry 4.0 technologies for 1,700 firms in Austria, Germany, and Switzerland. More broadly, our paper is also related to the literature on the effects of trade policy on the structure of trade and global supply chains (Fajgelbaum et al., 2021; Alfaro and Chor, 2023; Utar et al., 2023; Grossman et al., 2024).8

By emphasizing the effects of uncertainty on reshoring and automation, our paper complements recent work that examines the effects of changes in automation on trade. In particular, a growing body of literature has documented the interaction between automation and offshoring and showed that automation tends to reduce offshoring (De Backer et al., 2018; Artuc et al., 2019; Stemmler, 2019; Faber, 2020; Carbonero et al., 2020; Krenz et al., 2021; Bonfiglioli et al., 2022). Mandelman and Zlate (2022) argue that offshoring and automation reduce employment and wages of middle-skill occupations but enhance those for high-skilled ones. We examine the nexus between offshoring and automation from a different angle by showing how trade uncertainty induces reshoring and boosts automation investment and how the interactions between reshoring and automation affect the responses of domestic labor market variables to trade uncertainty.

Our paper also adds to an extensive literature on the effects of trade policy uncertainty (e.g., Handley and Limão, 2015, 2017, 2022; Feng et al., 2017; Crowley et al., 2018; Alessandria et al., 2019, 2021; Poilly and Tripier, 2023; Choi et al., 2023; Alessandria et al., 2024; Rodrigue et al., 2024), and more broadly, on the macroeconomic effects of uncertainty (e.g., Bloom, 2009; Fernández-Villaverde et al., 2011; Alessandria et al., 2015; Leduc and Liu, 2016; Basu and Bundick, 2017). Related to our study, Novy and Taylor (2020) argue that trade flows can be more sensitive to uncertainty shocks than domestic production because of higher fixed costs of orders of foreign inputs. Caldara et al. (2020) show that an increase in

<sup>&</sup>lt;sup>7</sup>While these results are broadly in line with our theoretical predictions, we note that we are using a relatively small sample of industries over a relatively short time period and therefore one should interpret our empirical results with caution.

<sup>&</sup>lt;sup>8</sup>The literature has also studied the importance of global supply chains in optimal trade policy; see, for example, Blanchard et al. (2017); Grossman et al. (2023); Antràs et al. (2024).

TPU reduces business investment, both in the data and in an open-economy model. Complementary to these studies, our paper highlights how trade uncertainty can drive three-way interactions between reshoring, automation, and labor markets.

#### II. THE MODEL

This section presents a small open economy model featuring labor search frictions, endogenous decisions of automation, and offshoring.

II.1. **Key features in the model.** Final consumption goods are produced using intermediate goods that are imported or domestically produced. Domestic intermediate goods can be produced using two types of technologies, a labor-only technology that uses unskilled workers as the only input and an automation technology that uses both robots and skilled workers as inputs.

Following Leduc and Liu (2023), we assume that a firm that chooses to use the automation technology can adopt a robot at a random sunk cost and hire a skilled worker from a competitive spot skilled labor market. If the firm chooses to operate the labor-only technology, then it can hire an unskilled worker subject to labor market search frictions in the spirit of the standard DMP framework.

In the beginning of a period t, firms carry over the stock of unfilled vacancies from the previous period, a fraction of which is automated by adopting robots. The stock of vacancies  $v_t$  available for hiring workers consists of the remaining vacancies after automation, the jobs separated in the beginning of the period, and newly created vacancies. The job seekers (the mass of which is  $u_t$ ) randomly match with the vacancies ( $v_t$ ) in the labor market, with the number of new matches ( $m_t$ ) determined by a matching technology. Production then takes place, using either a labor-only or an automation technology. The unfilled vacancies and the pool of employed workers at the end of the period are carried over to the next period, and the same sequence of economic activities repeats in period t + 1.

Compared to the standard DMP model, our model introduces four new features. First, we replace the free-entry assumption in the DMP model with costly vacancy creation, as in Fujita and Ramey (2007) and Leduc and Liu (2020). Since creating a new vacancy incurs a fixed cost, a vacancy has a positive value even if it is not filled by an unskilled worker. The number of vacancies becomes a slow-moving state variable (instead of a jump variable, as in the standard DMP framework), enabling our model to match the persistent vacancy dynamics in the data.

Second, we introduce endogenous automation decisions. In the beginning of period t, each firm draws a sunk cost of automation, which determines whether the firm will automate production or post the vacancy for hiring a worker. If the automation cost lies below a

threshold value, then the firm automates production by adopting a robot and hiring skilled workers to operate the robot. In that case, the firm obtains the automation value and the vacancy would be taken offline. If the automation cost exceeds the threshold, then the firm posts the vacancy for hiring an unskilled worker.

Third, we allow for worker skill heterogeneity, with skilled and unskilled workers, who are all members of the representative household. In our model, robots and skilled workers are complementary inputs, whereas they are substitutes for unskilled workers. This feature allows us to examine the joint effects of automation and offshoring on employment of workers with different skills and also on income inequality stemming from the skill premium.

Fourth, we introduce offshoring by allowing final goods producers to import intermediate goods. Changes in trade costs caused by, for example, global supply chain disruptions or trade wars can affect the effective costs of offshoring, which in turn affects the relative demand for intermediate goods that are imported versus domestically produced. Such changes in relative demand in turn drive changes in automation decisions, employment, and income distribution.

II.2. The frictional labor market for unskilled workers. At the beginning of period t, there are  $N_{t-1}$  existing job matches for unskilled workers. The measure of unemployed job seekers is given by

$$u_t = 1 - (1 - \delta)N_{t-1},\tag{1}$$

where  $\delta \in (0,1)$  denotes the job separation rate and we have assumed full labor force participation with the size of unskilled labor normalized to one.

The stock of vacancies  $v_t$  at the beginning of period t consists of unfilled vacancies carried over from period t-1 that are not automated plus the separated employment matches and newly created vacancies. The law of motion for vacancies is given by

$$v_t = (1 - q_{t-1}^v)(1 - q_t^a)v_{t-1} + \delta N_{t-1} + \eta_t,$$
(2)

where  $q_{t-1}^v$  denotes the job filling rate in period t-1,  $q_t^a$  denotes the automation probability in period t, and  $\eta_t$  denotes newly created vacancies (i.e., entry).

In the labor market, new job matches (denoted by  $m_t$ ) are formed between job seekers and open vacancies based on the matching function

$$m_t = \mu u_t^{\alpha} v_t^{1-\alpha},\tag{3}$$

where  $\mu$  is a scale parameter that measures matching efficiency and  $\alpha \in (0, 1)$  is the elasticity of job matches with respect to the number of job seekers.

The flow of new job matches adds to the employment pool, whereas job separations subtract from it. Aggregate employment evolves according to the law of motion

$$N_t = (1 - \delta)N_{t-1} + m_t. (4)$$

At the end of period t, the searching workers who failed to find a job remain unemployed. Thus, unemployment is given by

$$U_t = u_t - m_t = 1 - N_t. (5)$$

For convenience, we define the job finding probability  $q_t^u$  as

$$q_t^u = \frac{m_t}{u_t}. (6)$$

Similarly, we define the vacancy filling probability  $q_t^v$  as

$$q_t^v = \frac{m_t}{v_t}. (7)$$

II.3. The representative household. The representative household has the utility function

$$\mathbb{E}\sum_{t=0}^{\infty}\beta^{t}\left(\ln C_{t}-\chi N_{t}\right),\tag{8}$$

where  $\mathbb{E}[\cdot]$  is an expectation operator,  $\beta \in (0,1)$  is a subjective discount factor,  $C_t$  denotes consumption, and  $N_t$  denotes the fraction of unskilled household members who are employed.

The representative household faces the sequence of budget constraints

$$C_t + B_t = r_{t-1}B_{t-1} + w_{nt}N_t + w_{st}\bar{s} + \phi(1 - N_t) + d_t - T_t, \quad \forall t \ge 0,$$
(9)

where  $B_t$  denotes the household's holdings of a risk-free bond (in units of final goods) at the real interest rate  $r_t$ ;  $w_{nt}$  and  $w_{st}$  denote the real wage rates of unskilled and skilled workers (also in units of final consumption goods), respectively;  $d_t$  denotes the household's share of firm profits; and  $T_t$  denotes lump-sum taxes. The parameter  $\phi$  measures the flow benefits of unemployment. For simplicity, we assume that the aggregate supply of skilled labor is fixed at  $\bar{s}$ .

Denote by  $V_t(B_{t-1}, N_{t-1})$  the value function for the representative household. The household's optimizing problem can be written in the recursive form

$$V_t(B_{t-1}, N_{t-1}) \equiv \max_{C_t, N_t, B_t} \ln C_t - \chi N_t + \mathbb{E}_t D_{t,t+1} V_{t+1}(B_t, N_t), \tag{10}$$

subject to the budget constraint (9) and the employment law of motion (4) for unskilled workers, which can be written as

$$N_t = (1 - \delta)N_{t-1} + q_t^u u_t, \tag{11}$$

where we have used the definition of the job finding probability  $q_t^u$  with the measure of job seekers  $u_t$ . In the optimizing decisions, the household takes the economy-wide job finding rate  $q_t^u$  as given.

The stochastic discount factor (SDF) is given by

$$D_{t,t+1} \equiv \beta \frac{\Lambda_{t+1}}{\Lambda_t},\tag{12}$$

where  $\Lambda_t$  denotes the Lagrange multiplier for the budget constraint (9).

We define the employment surplus (i.e., the value of employment relative to unemployment) as  $S_t^H \equiv \frac{1}{\Lambda_t} \frac{\partial V_t(B_{t-1}, N_{t-1})}{\partial N_t}$ . The optimizing decision for employment implies that the employment surplus satisfies the Bellman equation

$$S_t^H = w_{nt} - \phi - \frac{\chi}{\Lambda_t} + \mathbb{E}_t D_{t,t+1} (1 - q_{t+1}^u) (1 - \delta) S_{t+1}^H.$$
 (13)

The employment surplus has a straightforward economic interpretation. If the household adds a new unskilled worker in period t, then the current-period gain would be wage income net of the opportunity costs of working, including unemployment benefits and the disutility of working. The household also enjoys the continuation value of employment if the employment relation continues. Having an extra unskilled worker today adds to the employment pool tomorrow (provided that the employment relation survives job separation); however, adding a worker today would also reduce the pool of searching workers tomorrow, a fraction  $q_{t+1}^u$  of whom would be able to find jobs. Thus, the marginal effect of adding a new worker in period t on employment in period t+1 is given by  $(1-q_{t+1}^u)(1-\delta)$ , resulting in the effective continuation value of employment shown in the last term of Eq. (13).

Finally, the household's optimizing consumption-savings decision implies the intertemporal Euler equation

$$1 = \mathbb{E}_t D_{t,t+1} r_t. \tag{14}$$

II.4. Final goods production. A homogeneous final good is produced using two types of intermediate inputs, one produced by domestic firms (denoted by  $Y_{dt}$ ) and the other imported from the foreign country  $(Y_{ft})$ . Importing goods is subject to a delivery lag such that imported intermediate goods today can be used for final goods production tomorrow.<sup>9</sup> The production function of final goods is given by

$$Y_t = \left[ \alpha_d^{\frac{1}{\theta}} Y_{dt}^{\frac{\theta - 1}{\theta}} + (1 - \alpha_d)^{\frac{1}{\theta}} Y_{f,t-1}^{\frac{\theta - 1}{\theta}} \right]^{\frac{\theta}{\theta - 1}},\tag{15}$$

where the parameter  $\theta$  measures the elasticity of substitution between home-produced and imported intermediate goods, and the parameter  $\alpha_d$  measures the importance of domestic

<sup>&</sup>lt;sup>9</sup>We incorporate delivery lags for imported inputs to enhance the realism of our model. As demonstrated in Appendix D, the results remain qualitatively similar even when these delivery lags are excluded.

intermediate goods for final goods production. We assume that intermediate goods are tradable while final goods are nontradable. To keep the analysis tractable, we interpret importing of intermediate goods as part of the production that could have been undertaken domestically but is instead offshored.<sup>10</sup>

We denote by  $p_{dt}$  and  $p_{ft}$  the relative prices of intermediate goods (i.e., in units of final consumption goods) produced domestically and imported, respectively. The relative price of imported goods faced by domestic final goods producers is given by

$$p_{ft} = \frac{\tau_t P_t^*}{P_t} = \tau_t \mathcal{Q}_t, \tag{16}$$

where  $\tau_t$  denotes an iceberg trade cost,  $P_t$  is the price of final consumption goods,  $P_t^*$  is the foreign price level, and  $Q_t \equiv \frac{P_t^*}{P_t}$  is the real exchange rate (RER). The small open economy takes the foreign price level  $P_t^*$  as exogenously given. Without loss of generality, we normalize  $P_t^* = 1$  such that the real exchange rate is isomorphic to the domestic price level.

We assume that, for every unit of goods delivered to the destination,  $\tau_t > 1$  units of goods need to be shipped. The trade cost  $\tau_t$  is an exogenous process with a time-varying volatility, which captures trade uncertainty related to factors such as trade wars, geopolitical tensions, or climate change risks that might cause global supply chain disruptions. Sepecifically, we assume that the trade cost follows the stationary stochastic process

$$\ln(\tau_t) = (1 - \rho_\tau) \ln(\bar{\tau}) + \rho_\tau \ln(\tau_{t-1}) + \sigma_{\tau t} \varepsilon_{\tau t}, \tag{17}$$

where  $\bar{\tau}$  is the mean of  $\tau_t$ ,  $\rho_{\tau} \in (-1,1)$  is a persistence parameter, and  $\varepsilon_{\tau t}$  is a white noise innovation. The term  $\sigma_{\tau t}$  is a stochastic volatility of the trade cost shock, which we interpret as trade uncertainty, and it follows the process

$$\sigma_{\tau t} = (1 - \rho_{\sigma \tau})\sigma_{\tau} + \rho_{\sigma \tau}\sigma_{\tau, t-1} + \eta_{\tau}u_{\tau t}. \tag{18}$$

Here,  $\rho_{\sigma\tau} \in (-1, 1)$  is the persistence and  $\eta_{\tau}$  is the standard deviation of the trade uncertainty shock,  $u_{\tau t}$  is a white noise innovation, and  $\sigma_{\tau}$  is the average standard deviation of the trade cost shock

Final goods producers take all prices as given and choose  $Y_{dt}$  and  $Y_{ft}$  to maximize the expected present value of profit flows. The optimizing problem is described by the Bellman equation

$$V_t(Y_{f,t-1}) = \max_{Y_{dt}, Y_{ft}} Y_t - p_{dt}Y_{dt} - p_{ft}Y_{ft} + \mathbb{E}_t D_{t,t+1}V_{t+1}(Y_{ft}), \tag{19}$$

<sup>&</sup>lt;sup>10</sup>In addition, we treat the rest of the world as a uniform area subject to the same degree of trade uncertainty. Thus, we abstract from the possibility that higher trade uncertainty in a specific region could lead firms to diversify the sourcing of their products to other regions. While that is an interesting and relevant issue, it is beyond the scope of this paper.

subject to the technology constraint (15), where  $V_t(Y_{f,t-1})$  denotes the value function, which depends on the state variable  $Y_{f,t-1}$ . The first-order conditions for this optimizing problem are given by

$$p_{dt} = \frac{\partial Y_t}{\partial Y_{dt}}, \quad p_{ft} = \mathbb{E}_t D_{t,t+1} V'_{t+1}(Y_{ft}). \tag{20}$$

The envelope condition implies that

$$V_t'(Y_{f,t-1}) = \frac{\partial Y_t}{\partial Y_{f,t-1}}. (21)$$

Combining (20) and (21), we obtain

$$p_{dt} = \left(\frac{\alpha_d Y_t}{Y_{dt}}\right)^{\frac{1}{\theta}}, \quad p_{ft} = \mathbb{E}_t D_{t,t+1} \left(\frac{(1 - \alpha_d) Y_{t+1}}{Y_{ft}}\right)^{\frac{1}{\theta}}. \tag{22}$$

The domestic intermediate good is itself a Constant Elasticity of Substitution (CES) aggregate of two types of intermediate goods produced using labor-only technology and automation technology. In particular, the quantity of domestically produced intermediate goods  $Q_{dt}$  is given by

$$Q_{dt} = \left[\alpha_n^{\frac{1}{\sigma}} Y_{nt}^{\frac{\sigma-1}{\sigma}} + (1 - \alpha_n)^{\frac{1}{\sigma}} Y_{at}^{\frac{\sigma-1}{\sigma}}\right]^{\frac{\sigma}{\sigma-1}},\tag{23}$$

where  $Y_{nt}$  denotes the intermediate goods produced using the labor-only technology,  $Y_{at}$  denotes the intermediate goods produced using the automation technology, the parameter  $\sigma$  is the elasticity of substitution between the two types of intermediate goods, and the parameter  $\alpha_n$  governs the relative importance of  $Y_{nt}$  in the aggregation technology.

Some domestically produced intermediate goods are exported to the foreign country. Thus, we have

$$Q_{dt} = Y_{dt} + \tau_t X_t, \tag{24}$$

where  $X_t$  denotes the quantity of exports.

The optimal choices of domestic intermediate goods producers imply that

$$\frac{p_{nt}}{p_{dt}} = \left(\frac{\alpha_n Y_{dt}}{Y_{nt}}\right)^{\frac{1}{\sigma}}, \quad \frac{p_{at}}{p_{dt}} = \left(\frac{(1 - \alpha_n) Y_{dt}}{Y_{at}}\right)^{\frac{1}{\sigma}}.$$
 (25)

The zero-profit condition for domestic intermediate goods producers implies that

$$p_{dt} = \left[ \alpha_n \ p_{nt}^{1-\sigma} + (1 - \alpha_n) \ p_{at}^{1-\sigma} \right]^{\frac{1}{1-\sigma}}.$$
 (26)

Discussion. To maintain tractability, our model abstracts from a few potentially important adjustment channels. On the household side, we exclude potential effects of automation on labor force participation (e.g., Grigoli et al., 2020) or the reallocation of workers to the services sector (Autor and Dorn, 2013). However, these adjustment channels are more likely to be quantitatively important in the longer term rather than at the business cycle frequency, which is the focus of our paper. Taking these additional adjustment channels into account would likely reduce the impact of trade uncertainty on unemployment in the long run. On the production side, we abstract from firms' ability to smooth unexpected changes in demand arising from trade uncertainty through variations in inventories (e.g., Alessandria et al., 2019).

II.5. Domestic production of intermediate goods. A firm makes automation decisions at the beginning of the period t. Adopting a robot requires a sunk cost  $\nu$  in units of consumption goods, which is drawn from the i.i.d. distribution  $G(\nu).^{11}$  A firm chooses to adopt a robot if and only if the cost of automation is less than the benefit. For any given benefit of automation, there exists a threshold value  $\nu_t^*$  in the support of the distribution  $G(\nu)$ , such that automation occurs if and only if  $\nu \leq \nu_t^*$ . If the firm adopts a robot to replace the job position, then the vacancy will be taken offline and will not be available for hiring a worker. Thus, the automation threshold  $\nu_t^*$  depends on the value of automation (denoted by  $J_t^a$ ) relative to the value of a vacancy (denoted by  $J_t^v$ ). In particular, the threshold for automation decision is given by

$$\nu_t^* = J_t^a - J_t^v. \tag{27}$$

The probability of automation is then given by the cumulative density of the automation costs evaluated at  $\nu_t^*$ . That is,

$$q_t^a = G(\nu_t^*). (28)$$

The flow of automated job positions adds to the stock of automated positions (denoted by  $A_t$ ), which becomes obsolete at the rate  $\rho^o \in [0, 1]$  in each period. Thus,  $A_t$  evolves according to the law of motion

$$A_t = (1 - \rho^o)A_{t-1} + q_t^a(1 - q_{t-1}^v)v_{t-1}, \tag{29}$$

where  $q_t^a(1-q_{t-1}^v)v_{t-1}$  is the number of newly automated job positions.<sup>12</sup>

<sup>&</sup>lt;sup>11</sup>The assumption that adopting a robot requires a sunk cost implies that the automation decision is irreversible. This irreversibility tends to reduce the incentive to automate in response to trade uncertainty, making our results conservative. In contrast, if the automation decision was reversible (e.g., involving a per-period fixed cost of automation), the automation response to trade uncertainty would likely be stronger, as the option value of delaying automation would no longer exist in this case.

<sup>&</sup>lt;sup>12</sup>If a vacancy is "filled" by a robot, it will be taken offline once and for all. Even if the robot later becomes obsolete, the vacated position does not return to the stock of vacancies.

If the firm adopts a robot, then it optimally chooses the input of skilled workers  $s_t$ , with the production function

$$y_{at} = Z_t \zeta^{\gamma_a} s_t^{1-\gamma_a}, \tag{30}$$

where  $\gamma_a \in (0,1)$  denotes the elasticity of output with respect to the robot input,  $Z_t$  denotes a total factor productivity (TFP) shock, and  $\zeta$  denotes an automation-specific productivity.<sup>13</sup> TFP follows a stationary AR(1) stochastic process

$$\ln(Z_t) = (1 - \rho_z)\ln(\bar{Z}) + \rho_z\ln(Z_{t-1}) + \sigma_z\varepsilon_{zt},\tag{31}$$

where  $\bar{Z}$  is the mean of  $Z_t$ ,  $\rho_z \in (-1,1)$  is a persistence parameter,  $\varepsilon_{zt}$  is a white noise innovation, and  $\sigma_z$  is the standard deviation of the TFP shock.<sup>14</sup>

The firm takes the skilled real wage rate  $w_{st}$  as given and chooses  $s_t$  to maximize the profit before paying the robot operation cost  $\kappa_a$ . The value of automation is then given by

$$J_t^a = \pi_t^a (1 - \kappa_a) + (1 - \rho^o) \mathbb{E}_t D_{t,t+1} J_{t+1}^a, \tag{32}$$

where  $\pi_t^a \equiv \max_{s_t} p_{at} Z_t \zeta^{\gamma_a} s_t^{1-\gamma_a} - w_{st} s_t = \gamma_a p_{at} Z_t \zeta^{\gamma_a} s_t^{1-\gamma_a}$ .

If the automation sunk cost exceeds the threshold  $\nu_t^*$ , then the firm chooses not to adopt a robot and instead chooses to post the vacancy in the labor market for hiring an unskilled worker. In addition, newly separated jobs and newly created vacancies add to the stock of vacancies for hiring unskilled workers. Following Leduc and Liu (2020), we assume that creating a new vacancy incurs an entry cost e in units of consumption goods, which is drawn from an i.i.d. distribution F(e). A new vacancy is created if and only if the net value of entry is non-negative. The benefit of creating a new vacancy is the vacancy value  $J_t^v$ . Thus, the number of new vacancies  $\eta_t$  is given by the cumulative density of the entry costs evaluated at  $J_t^v$ . That is,

$$\eta_t = F(J_t^v). \tag{33}$$

Posting a vacancy incurs a per-period fixed cost  $\kappa$  (in units of final consumption goods). If the vacancy is filled (with probability  $q_t^v$ ), the firm obtains the employment value  $J_t^e$ . Otherwise, the firm carries over the unfilled vacancy to the next period, which will be automated with the probability  $q_{t+1}^a$ . If the vacancy is automated, then the firm obtains the automation value  $J_{t+1}^a$  net of the expected robot adoption costs; otherwise, the vacancy will

<sup>&</sup>lt;sup>13</sup>In our baseline model, the use of robots is not subject to trade costs. However, in practice, firms' automation technology may partly be imported and thus subject to trade costs and trade uncertainty. We consider this more general case in a robustness exercise below.

<sup>&</sup>lt;sup>14</sup>We focus on trade uncertainty in the main analysis, although we also examine the effects of TFP uncertainty, which is measured by time-varying volatility of the TFP shock (see Appendix D).

remain open, and the firm receives the vacancy value  $J_{t+1}^v$ . Thus, the vacancy value satisfies the Bellman equation

$$J_t^v = -\kappa + q_t^v J_t^e + (1 - q_t^v) \mathbb{E}_t D_{t,t+1} \left\{ q_{t+1}^a J_{t+1}^a - \int_0^{\nu_{t+1}^*} \nu dG(\nu) + (1 - q_{t+1}^a) J_{t+1}^v \right\}.$$
 (34)

If a firm successfully hires an unskilled worker, then it can produce  $Z_t$  units of intermediate goods. The value of employment satisfies the Bellman equation

$$J_t^e = p_{nt} Z_t - w_{nt} + \mathbb{E}_t D_{t,t+1} \left\{ (1 - \delta) J_{t+1}^e + \delta J_{t+1}^v \right\}. \tag{35}$$

Hiring a worker generates a flow profit  $p_{nt}Z_t - w_{nt}$  in the current period (in final consumption units). If the job is separated in the next period (with probability  $\delta$ ), then the firm receives the vacancy value  $J_{t+1}^v$ . Otherwise, the firm receives the continuation value of employment.

II.6. The Nash bargaining wage. When a job match is formed, the wage rate is determined through Nash bargaining. The bargaining wage splits the joint surplus of a job match between the unskilled worker and the firm. The worker's employment surplus is given by  $S_t^H$  in equation (13). The firm's surplus is given by  $J_t^e - J_t^v$ . The possibility of automation affects the value of a vacancy and thus indirectly affects the firm's reservation value and its bargaining decisions.

The Nash bargaining problem is given by

$$\max_{w_{nt}} (S_t^H)^b (J_t^e - J_t^v)^{1-b}, \tag{36}$$

where  $b \in (0,1)$  represents the bargaining weight for workers.

Define the total surplus as

$$S_t \equiv J_t^e - J_t^v + S_t^H. \tag{37}$$

Then the bargaining solution is given by

$$J_t^e - J_t^v = (1 - b)S_t, \quad S_t^H = bS_t.$$
 (38)

The bargaining outcome implies that the firm's surplus is a constant fraction 1 - b of the total surplus  $S_t$  and the household's surplus is a fraction b of the total surplus.

The bargaining solution (38) and the expression for household surplus in equation (13) together imply that the Nash bargaining wage  $w_{nt}^N$  satisfies the Bellman equation

$$\frac{b}{1-b}(J_t^e - J_t^v) = w_{nt}^N - \phi - \frac{\chi}{\Lambda_t} + \mathbb{E}_t D_{t,t+1} (1 - q_{t+1}^u) (1 - \delta) \frac{b}{1-b} (J_{t+1}^e - J_{t+1}^v).$$
(39)

In the baseline model, we assume that real wages are flexible and are given by the Nash bargaining wage (i.e.,  $w_{nt} = w_{nt}^{N}$ ).

II.7. Export demand. To close the model, we follow Chang et al. (2015) and specify the export demand schedule

$$X_t = \left(\tau_t \frac{P_{dt}}{P_t^*}\right)^{-\theta} X_t^* = \left(\frac{\tau_t p_{dt}}{Q_t}\right)^{-\theta} X_t^*, \tag{40}$$

where  $X_t^*$  denotes an exogenous foreign demand shifter. Demand for exported intermediate goods is inversely related to the effective price of exports, consisting of both the relative price  $p_{dt}$ , converted to foreign goods units by the real exchange rate, and the iceberg trading cost  $\tau_t$ . We assume that the demand elasticity for home exports is identical to the demand elasticity for imported intermediate goods (both elasticities are given by  $\theta$ ).

II.8. Government policy and search equilibrium. The government finances unemployment benefit payments  $\phi$  for unemployed workers through lump-sum taxes. We assume that the government balances the budget in each period such that

$$\phi(1 - N_t) = T_t. \tag{41}$$

In a search equilibrium, the markets for final goods, intermediate goods, and skilled labor all clear. We also assume that trade is balanced such that export revenue equals the import costs.

Market clearing for domestic intermediate goods along with that for skilled labor implies that

$$Y_{nt} = Z_t N_t, \quad Y_{at} = Z_t (\zeta A_t)^{\gamma_a} \bar{s}^{1-\gamma_a}. \tag{42}$$

Final goods market clearing requires that consumption spending, vacancy posting costs, robot operation costs, robot adoption costs, and vacancy creation costs add up to aggregate final goods output. The aggregate robot operation cost is given by  $\gamma_a p_{at} Y_{at}$ . Thus, the aggregate resource constraint is

$$C_t + \kappa v_t + \kappa_a \gamma_a p_{at} Y_{at} + (1 - q_{t-1}^v) v_{t-1} \int_0^{\nu_t^*} \nu dG(\nu) + \int_0^{J_t^v} e dF(e) = Y_t.$$
 (43)

We focus on a balanced-trade equilibrium. In such an equilibrium, the revenue from exporting intermediate goods equals the costs of importing foreign intermediate goods, such that

$$\tau_t p_{dt} X_t = p_{ft} Y_{ft}. \tag{44}$$

We assume that the initial foreign asset holdings are  $B_{-1} = 0$ . Then, with balanced trade, the current account balance is also zero for all periods, and we have  $B_t = 0$  for all t.

Appendix A summarizes the equilibrium conditions.

Table 1. Calibrated parameters

	Parameter Description	value
β	Subjective discount factor	0.99
α	Elasticity of matching function	0.50
φ	Unemployment benefit	0.25
b	Nash bargaining weight	0.50
δ	Job separation rate	0.10
$\rho^o$	Automation obsolescence rate	0.03
$\kappa_a$	Flow cost of automated production	0.98
$\mu$	Matching efficiency	0.6606
κ	Vacancy posting per-period fixed cost	0.1128
$\alpha_n$	Share of worker-produced intermediate goods	0.39
$\sigma$	Elasticity of substitution between domestic intermediate goods	2.03
$\bar{e}$	Scale of vacancy creation cost distribution	3.07
$ar{ u}$	Scale of automation cost distribution	8.57
$\alpha_d$	Weight on domestic intermediate input (home bias)	0.85
$\theta$	Substitution elasticity between domestic and imported goods	0.8
$ar{ au}$	Average iceberg trade cost	1.74
$ar{Z}$	Average level of TFP	1
$\bar{s}$	Supply of skilled workers	0.3
$\gamma_a$	Share of automation equipment in production	0.32
ζ	Automation-specific productivity	3.4422
$\chi$	Disutility of working	0.3741
$\rho_z$	Persistence of TFP shock	0.95
$\sigma_z$	Volatility of TFP shock	0.01
$ ho_{ au}$	Persistence of first-moment trade cost shock	0.99
$\sigma_{ au}$	Volatility of first-moment trade shock	0.00215
$\rho_{\sigma  au}$	Persistence of trade uncertainty shock	0.96
$\eta_{ au}$	Volatility of trade uncertainty shock	0.37

# III. PARAMETER CALIBRATION

We use our model to study the macroeconomic impact of trade uncertainty shocks. We solve the model based on third-order approximations to the equilibrium conditions. To solve the model requires assigning values to the parameters. Table 1 shows the calibrated parameter values.

We have a quarterly model. We set the subjective discount factor to  $\beta=0.99$ , such that the steady-state real interest rate is 4 percent per year. We set the matching function elasticity to  $\alpha=0.5$ , in line with the literature (Blanchard and Galí, 2010; Gertler and Trigari, 2009a). Following Hall and Milgrom (2008), we set the worker bargaining weight to b=0.5 and the unemployment benefit parameter to  $\phi=0.25$ . Based on the data from the Job Openings and Labor Turnover Survey (JOLTS), we calibrate the steady-state job separation rate to  $\delta=0.10$  at the quarterly frequency. We set  $\rho^o=0.03$ , so that automation equipment depreciates at an average annual rate of 12 percent, in line with the depreciation rate of industrial robots used by the International Federation of Robotics (IFR) for estimating the average life span of robots and for constructing their measure of the operation stocks of robots. Following Leduc and Liu (2023), we set the flow cost of automation to  $\kappa_a=0.98$ . We calibrate the vacancy posting cost  $\kappa=0.1128$  such that the flow cost of vacancy posting is

about 1 percent of aggregate output. We set the matching efficiency parameter to  $\mu = 0.6606$  such that the quarterly job filling rate is  $q^v = 0.71$  in the steady state, as calibrated by den Haan et al. (2000).

We follow Leduc and Liu (2023) and assume that the distribution functions F(e) for vacancy creation costs and  $G(\nu)$  for automation costs both follow a uniform distribution, such that

$$F(e) = \frac{e}{\bar{e}}, \quad G(\nu) = \frac{\nu}{\bar{\nu}}.$$
 (45)

We calibrate the scale parameter of the vacancy creation cost function to  $\bar{e}=3.07$  to match the estimation of Leduc and Liu (2023). We calibrate the scale of the automation cost function to  $\bar{\nu}=8.57$  such that the model implies a steady-state automation probability of  $q^a=0.096$ , or about 38 percent at the annual frequency, which lies within the range of firm-level estimates. For example, in a recent study based on the 2019 Annual Business Survey (ABS) of the U.S. Census Bureau, Acemoglu et al. (2022) report that, in total, 30.4 percent of U.S. workers are employed at firms using advanced technologies for automating tasks. Exposure to automation is higher in manufacturing, with 52 percent of manufacturing workers employed at firms using advanced technologies for automation. Outside of manufacturing, the exposure to automation is lower, at 28.3 percent. The model-implied automation probability in the steady state (38 percent), which corresponds to the measured automation exposure, lies within this empirical range.

Based on Firoz et al. (2023), we calibrate the weight of worker-produced intermediate goods in final goods production to  $\alpha_n = 0.39$  and the elasticity of substitution between intermediate goods produced by automation equipment and by workers to  $\sigma = 2.03$ .<sup>15</sup>

Following Leduc and Liu (2023), we set the output elasticity with respect to automation equipment to  $\gamma_a = 0.32$ . We normalize the average level of TFP to  $\bar{Z} = 1$ . We also normalize the supply of skilled workers to  $\bar{s} = 0.3$ , matching the median ratio of employment of college-educated workers to aggregate employment in the period from 2000 to 2019. We calibrate the average level of the automation-specific productivity to  $\zeta = 3.4422$  such that the model implies a steady-state skill premium of 55 percent, in line with the observed ratio of median weekly earnings of workers with a bachelor's degree or higher to those with some college or associate degrees reported by the Bureau of Labor Statistics.

We set the average iceberg trade cost to  $\bar{\tau} = 1.74$ , which lies within the range of empirical estimates as surveyed by Anderson and van Wincoop (2004). We calibrate the weight on domestically produced intermediate goods in the aggregation technology for final goods

<sup>&</sup>lt;sup>15</sup>Firooz et al. (2023) calibrate these two parameters to target the 2016 level of robot density in the U.S. manufacturing sector of 0.02 and the cumulative increase of robot density of about 300 percent from 2002 to 2016 while the relative price of robots declined by 40 percent during the same period.

to  $\alpha_d = 0.85$ , reflecting home bias in goods consumption. We calibrate the elasticity of substitution between domestic goods and imported goods to  $\theta = 0.8$ , which is in line with empirical literature. For example, Boehm et al. (2023) find that the elasticity of trade flows to exogenous changes in tariffs is about -0.76 in the short run and about -2 in the long run (see also di Giovanni et al., 2023; Corsetti et al., 2008). Since our model focuses on the short-run fluctuations induced by trade uncertainty, our calibration of  $\theta = 0.8$  is consistent with the short-run elasticity estimated by Boehm et al. (2023). We normalize the export demand shifter to  $X_t^* = 1$ , which implies a steady-state export share of about 10.8 percent of GDP.

We calibrate the disutility of working to  $\chi = 0.3741$  such that the model implies a steady-state unemployment rate of 5.9 percent, matching the average unemployment rate from 2000 to 2019.

For the parameters in the TFP shock processes, we set  $\rho_z = 0.95$  and  $\sigma_z = 0.01$ , in line with the real business cycle literature. For the first-moment shock to trading costs, we set  $\rho_{\tau} = 0.99$  and  $\sigma_{\tau} = 0.00215$  based on the estimates of Caldara et al. (2020). The trade uncertainty shock parameters are also calibrated based on the study of Caldara et al. (2020). Specifically, we set  $\rho_{\sigma\tau} = 0.96$  and  $\eta_{\tau} = 0.37$ .

# IV. MACROECONOMIC EFFECTS OF TRADE UNCERTAINTY

To study the macroeconomic effects of trade uncertainty, we use our calibrated parameters and solve the model based on third-order perturbations around the steady-state equilibrium. We then compute impulse responses to a trade uncertainty shock following the approach of Fernández-Villaverde et al. (2011) and Leduc and Liu (2016).<sup>16</sup> To illustrate the model's mechanism, we perform several counterfactual exercises.

IV.1. Trade uncertainty in the baseline model. Figure 1 presents the impulse responses of several key macroeconomic variables following a one-standard-deviation shock to trade uncertainty. An increase in trade uncertainty reduces imports, redirecting production of intermediate goods from foreign sources toward domestic producers (i.e., reshoring). This expenditure-switching effect stimulates automation investment. Trade uncertainty further boosts automation through a precautionary-savings channel, which lowers the real interest rate and therefore raises the present value of automation. However, trade uncertainty could discourage automation through an option-value channel. Under our calibration, the positive effects from expenditure switching and precautionary savings dominate the option-value

<sup>&</sup>lt;sup>16</sup>The impulse responses of a given variable to a trade uncertainty shock are measured by the differences between the values of that variable in the presence of the shock and its value in the stochastic steady state (i.e., its ergodic mean).

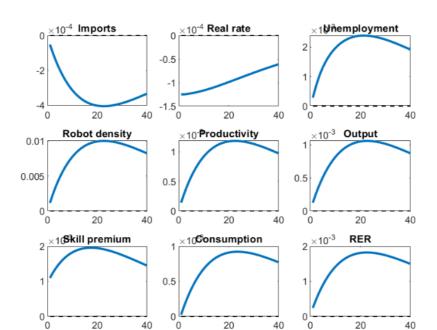


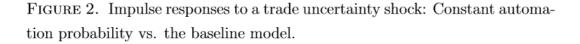
FIGURE 1. Impulse responses to a trade uncertainty shock in the baseline model

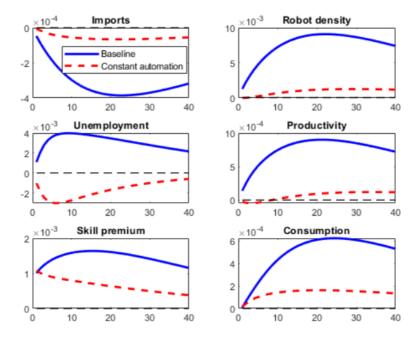
effect, such that trade uncertainty leads to an increase in automation measured by the robot density.

Increased automation raises labor productivity, stimulating the incentive for creating new vacancies. However, with our calibration, this job-creating effect is more than offset by the job-displacing effect of automation, leading to an increase in unemployment of unskilled workers. Nonetheless, aggregate output and consumption both rise persistently because the productivity gains stemming from automation outweigh the drags from lowered imports and domestic production by unskilled workers. The automation-driven productivity gains also lowers the domestic price level, leading to a real exchange rate depreciation (i.e., an increase in  $Q_t$ ).

The increased threat of automation also weakens the bargaining power of unskilled workers in wage negotiations, lowering their wages. In contrast, skilled workers are a complementary input with automation equipment. Thus, automation raises demand for skilled workers, pushing up the skilled wage while depressing the unskilled wage, resulting in a higher skill premium.

IV.2. **Transmission channels.** The model embeds two important transmission channels for trade uncertainty shocks: an automation channel and a trade channel.





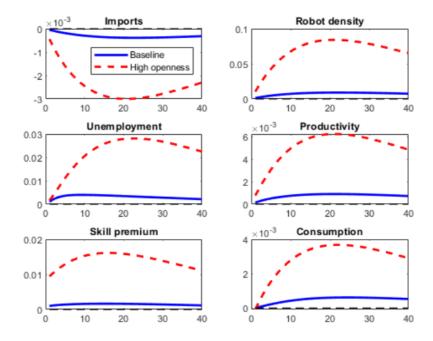
IV.2.1. The automation channel. To examine the importance of the automation channel, we consider a counterfactual version of the model with a constant automation probability. In particular, we keep the automation probability  $q_t^a$  fixed at the steady-state level.

Figure 2 shows the impulse responses to a trade uncertainty shock in the counterfactual model with a constant automation probability (red dashed line) compared to those in the baseline model (blue solid line). Absent adjustments in the automation probability, the effects of trade uncertainty on the macroeconomic variables are more muted than in the baseline model. Furthermore, in the counterfactual model, trade uncertainty reduces unemployment because it creates an expenditure switching effect, boosting demand for domestic goods. Since firms cannot adjust automation investment, they can meet the increased demand for domestic goods only by raising domestic employment.

IV.2.2. Trade openness. Exposure to trade (or equivalently, offshoring) is also important for the transmission of trade uncertainty shocks. To illustrate this, we consider a counterfactual with high openness to international trade. Specifically, we lower the home-bias parameter  $\alpha_d$  to 0.6 from the baseline value of 0.85.

Figure 3 shows the impulse responses in this counterfactual (red dashed line) versus those in the baseline model (blue solid line). When the economy is more open to international trade, the effects of trade uncertainty are amplified. Trade uncertainty leads to larger declines

FIGURE 3. Impulse responses to a trade uncertainty shock: Higher openness vs. the baseline model.



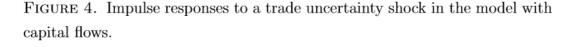
in imports and larger increases in robot density, unemployment, productivity, consumption, and the skill premium.

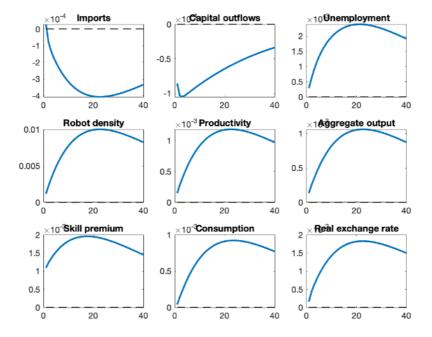
## IV.3. Robustness. The main results are robust to several variations of our model.

IV.3.1. Capital flows. Our model features a closed capital account such that the interest rate is endogenous. As an extension, we consider an alternative framework where international capital flows are allowed. In particular, the small open economy can borrow from or lend to the rest of the world at an exogenous world interest rate  $r_t^*$  (in units of foreign consumption goods). To capture the frictions in capital markets, we assume that changes in capital flows are subject to an adjustment cost. Since the real interest rate is fixed, the precautionary-savings channel is absent in this alternative model, and therefore, trade uncertainty boosts automation through the expenditure-switching channel only. Appendix B presents this alternative framework and equilibrium conditions.

Figure 4 shows the impulse responses to a trade uncertainty shock in the model with capital flows.<sup>17</sup> Increased trade uncertainty reduces imports and capital outflows, triggering an expenditure-switching effect that boosts automation. The resulting increase in robot density raises the unemployment of unskilled workers. Increased automation also boosts

<sup>&</sup>lt;sup>17</sup>We calibrate the bond adjustment cost parameter to  $\psi = 2$  for solving the model.

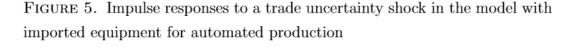


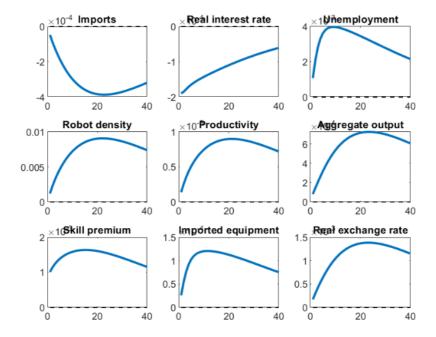


labor productivity, aggregate output, and the skill premium. This in turn leads to a rise in consumption and a real exchange rate depreciation. Overall, these impulse responses are qualitatively and quantitatively similar to those obtained in our baseline model under financial autarky.

IV.3.2. Imported intermediate inputs for automated production. In our baseline model, a firm that operates the automation technology uses robots and skilled workers for production. However, in practice, firms' automation technology may also rely on imported intermediate goods (e.g., robot parts or other automation equipment). To incorporate this channel, Appendix C considers a generalization of the baseline model to include imported intermediate goods for automating firms. In particular, we assume that imported intermediates are a complement input to robots in the automation technology.

Figure 5 plots the impulse responses to a trade uncertainty shock in this model. The impulse responses are similar to those in our baseline model. Trade uncertainty reduces imports and raises demand for domestic goods through an expenditure-switching effect. Since employment is a long-term relation, firms reduce hiring as the option value of waiting increases. To meet the increased demand for domestic intermediate goods, firms rely more on automation, raising the demand for robots. All else being equal, an increase in trade uncertainty would lower demand for imported equipment in the automation sector. However,



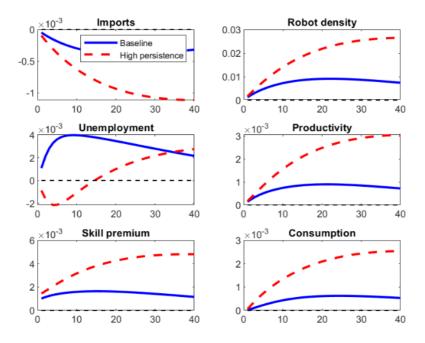


the increased reliance on robots for producing domestic intermediate goods raises the demand for imported equipment since imported intermediate inputs complement robots. Overall, trade uncertainty reduces imported goods and domestic employment, and raises robot density and imported equipment for automated production. As in the baseline model, the increased automation also boosts labor productivity and the skill premium.

IV.3.3. Persistence of trade uncertainty. Trade uncertainty may be more persistent than past data suggest for the calibration of the baseline model. Trade tensions, geopolitical conflicts, and climate change risks may be part of a new normal with persistently elevated trade uncertainty. We consider a counterfactual case with a higher persistence of the trade uncertainty shock by raising the persistence parameter  $\rho_{\sigma\tau}$  from 0.96 in the baseline calibration to 0.99, proxying for a quasi-permanent regime with higher trade uncertainty.

Figure 6 shows the impulse responses in this counterfactual case (red dashed line) versus those in the baseline model (blue solid line). Near-permanent trade uncertainty generates a stronger expenditure-switching effect, resulting in greater reshoring (i.e., larger declines in imports) and a larger increase in automation investment. The stronger expenditure-switching effect in this case is such that it raises domestic employment of unskilled workers in the short run, although the job displacing effects of automation dominates over time, leading to a rise in unemployment. The larger boom in automation investment also results in greater gains in

FIGURE 6. Impulse responses to a trade uncertainty shock: More persistent trade uncertainty shock vs. the baseline model.



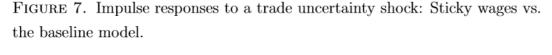
productivity and larger increases in the skill premium and consumption than in the baseline model.

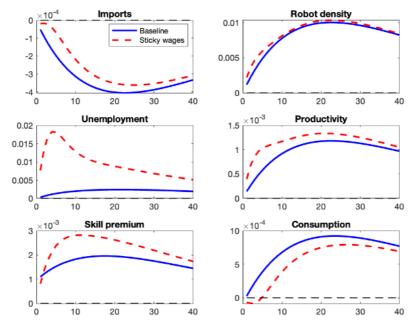
IV.3.4. The role of wage rigidity. In the baseline model, we assume that real wages are flexible. We now examine the robustness of the results to wage stickiness. Following the literature (Hall, 2005a; Shimer, 2005), we assume that the real wage of unskilled workers is a geometrically weighted average of the Nash bargaining wage and the wage rate in the previous period, such that

$$w_{nt} = w_{n,t-1}^{\gamma_w} (w_{nt}^N)^{1-\gamma_w}, (46)$$

where  $\gamma_w \in (0,1)$  represents the degree of real wage rigidity. We follow Leduc and Liu (2016) and set the real wage rigidity parameter to  $\gamma_w = 0.8$ , which is in line with Gertler and Trigari (2009b), who calibrate the probability of nonrenegotiation of wage contracts at 0.89.

Figure 7 compares the impulse responses from the case with wage rigidities (red dashed line) to those in the baseline case with flexible wages (blue solid line). As in the standard DMP framework, wage rigidities amplify the increase in unemployment following the trade uncertainty shock, reflecting the Shimer volatility puzzle (Shimer, 2005; Hall, 2005b). The impulse responses of the other macroeconomic variables are similar to those in the baseline model.





IV.3.5. Delivery lags. In the baseline model, we assume that importing intermediate inputs for final goods production requires a delivery lag. Appendix D.1 presents a version of the model without delivery lags. The impulse responses to trade uncertainty in the model without delivery lags are similar to those obtained in the baseline model. In particular, trade uncertainty reduces imports, and increases unemployment and robot density. We note that trade uncertainty in this version of the model still activates the expenditure-switching channel because of the curvature in the import demand schedule.

IV.3.6. Other shocks. Appendix D.2 considers other shocks to the economy and shows that impulse responses to these shocks are quite different from those of trade uncertainty. In particular, we consider first-moment shocks to trade costs as well as first and second-moment shocks to TFP.

IV.4. Welfare consequences of automation. The labor search frictions in our model lead to a congestion externality as in the standard DMP model, implying that the competitive equilibrium allocations are not necessarily Pareto optimal. More importantly, fluctuations in the automation probability lead to endogenous fluctuations in the workers' relative bargaining power in wage negotiations (Leduc and Liu, 2023). Thus, even if the Hosios condition holds (i.e., the bargaining weight b is equal to the elasticity of the matching function  $\alpha$ ,

which is true under our calibration), endogenous variations in the worker bargaining power driven by fluctuations in automation could push the equilibrium allocations away from the social optimum.

To examine the welfare consequences of endogenous automation, we compute the welfare gains of moving from our baseline model to a counterfactual economy with a constant automation probability (i.e., the counterfactual model that we have examined in Section IV.2.1). Under our calibrated parameters, allowing automation to fluctuate (as in our baseline model) incurs a modest welfare loss of about 0.75 percent of consumption equivalent. This result is driven by the fact that automation amplifies macroeconomic fluctuations as shown in Figure 2 and thus reduces the welfare of the risk-averse representative household. 19

#### V. EMPIRICAL EVIDENCE

Our theoretical model predicts that trade uncertainty can stimulate automation investment and reduce imported intermediate goods. The increased automation driven by trade uncertainty in turn raises labor productivity, value added, and the skill premium and reduces domestic employment. We now present some empirical evidence supporting the model predictions.

V.1. Data. We measure trade uncertainty using the U.S. TPU index constructed by Caldara et al. (2020), which is based on the frequency of articles in several major U.S. newspapers that discuss economic policy uncertainty and contain one or more phrases related to trade policy (such as "import tariffs," "import barriers," "WTO," "trade policy," and "trade agreement"). The monthly TPU index is available starting from 1960.<sup>20</sup>

We measure automation using robot density in U.S. manufacturing industries. Specifically, we define robot density in industry j and year t ( $Robot_{jt}$ ) as the operational stock of industrial robots per thousand employees. We obtain the data of industrial robots for each two-digit manufacturing industry based on the International Standard Industrial Classification (ISIC,

$$V_t = \sum_{t=0}^{\infty} \beta^t \left[ \log(\tilde{C}_t(1+\Delta)) - \chi \tilde{N}_t \right] = \frac{\log(1+\Delta)}{1-\beta} + \tilde{V}_t, \tag{47}$$

where  $V_t$  and  $\tilde{V}_t$  denote, respectively, the welfare in the baseline economy and the counterfactual and  $\tilde{C}_t$  and  $\tilde{N}_t$  denote the consumption and employment in the counterfactual.

<sup>19</sup>Our framework can be extended to study the welfare implications of tax policies in a model with automation and labor search frictions, which is an important subject for future research.

<sup>20</sup>Caldara et al. (2020) also develop a firm-level measure of TPU and another aggregate measure of TPU based on a stochastic volatility model for U.S. import tariffs.

<sup>&</sup>lt;sup>18</sup>The welfare gain (or loss) of keeping the automation probability constant relative to the baseline economy is measured by a constant  $\Delta$  such that

Rev. 4) from the International Federation of Robotics (IFR). We obtain employment data for each manufacturing industry at the two-digit NAICS 2017 level from the NEBR-CES database. We match the industries by cross-walking two-digit ISIC codes to NAICS codes. The matched sample contains 12 industries (at the NAICS two-digit level) for the years 2004 to 2018, thus restricting our sample to the pre-pandemic period.

To help explore the differential effects of trade uncertainty across industries with different exposure to offshoring, we construct a measure of industry-level offshoring exposure using the initial share of imported intermediate goods in gross output (i.e., in the beginning year of our sample) for each two-digit NAICS manufacturing industries. We obtain data on the gross imports of intermediate products from OECD Trade in Value-Added, and on gross output from the Bureau of Economic Analysis. For each industry-year pair, we also use the import-weighted average of tariffs that the U.S. imposes on its imports from the World Integrated Trade Solution (WITS). The annual sample covers 15 two-digit NAICS industries for the years from 1997 to 2018.

We measure labor productivity for a two-digit NAICS industry by the ratio of real value added to total employment in that industry, using data from the NBER-CES. We construct a measure of the skill premium using data from the Current Population Survey (CPS). In particular, the skill premium is measured by the earnings per hour of skilled workers (i.e., with a college degree or above) divided by those of unskilled workers (with a high school degree).

Since we have annual data on industrial robots and imports of intermediate goods, we aggregate the TPU index from a monthly frequency to an annual frequency by taking the within-year average.

Table 2 reports the summary statistics of our data. Robot density (in log units) in the data displays substantial variations across industries and time, with a standard deviation of 2.73, which is over four times its sample mean. The interaction between TPU (in log units) and the initial share of intermediate imports also displays significant variations, with a standard deviation (0.246) of about 70 percent of its mean. The share of imported intermediate goods (in log units)—our measure of offshoring activity—has more modest variations across industries and time, with a standard deviation of about 30 percent of the mean (in absolute value). The real outcome variables, including labor productivity, employment, value-added, and the skill premium, are relatively stable, with standard deviations between 6 and 20 percent of their respective means.

V.2. Trade uncertainty, automation, and offshoring. To examine the empirical relationship between automation and offshoring with trade uncertainty, we consider the following

SDMin Max IQR Mean Count log Robot density .615 161 2.731 -6.570 6.040 3.520  $\log TPU \times$ Initial share of intermediate imports .345264 .246 .059 1.553 .152 log Share of intermediate imports -2.234264 .684 -4.188-.961.708 log Labor Productivity 264 .488 6.522 .628 5.176 4.136 log Employment 6.476 264 .6115.174 7.6301.070 log Real Value-Added 11.652 264 .76910.055 13.563 .920log Skill premium .484264 .101 .247 .768 .139 log(1+Tariff)200 264 0.023.113.0124Observations 264

Table 2. Summary Statistics

Note: The table shows the summary statistics of the variables used in the regressions. Robot density is defined as the operation stock of industrial robots per thousand employees in each industry. The share of intermediate imports is the ratio of imported intermediate goods to gross output in each industry. TPU is the trade policy uncertainty index, which is an aggregate time series constructed by Caldara et al. (2020). Labor productivity is the ratio of value-added to employment in each industry. Skill premium is the ratio of hourly earnings of workers with a college degree or above to those with a high school education. Tariff is the industry-year-specific import-weighted average of tariffs that the U.S. imposes on its imports. See the text for data sources.

empirical specification

$$\ln Robot_{it} = \alpha_0 + \alpha_1 ImpShare_i \times \ln TPU_t + \alpha_2 \ln(1 + Tariff_{it}) + \eta_i + \theta_t + \varepsilon_{it}, \quad (48)$$

where  $ImpShare_j$  is the share of imported intermediate goods in gross output for industry j at the beginning of our sample (2004), as a proxy for the initial exposure of the industry to offshoring. The terms  $\eta_j$  and  $\theta_t$  denote industry and time fixed effects, respectively, and  $\varepsilon_{jt}$  denotes the regression residuals. In the regression, we include industry-level tariffs (i.e.,  $\ln(1 + Tariff_{jt})$ ) as an additional control variable to mitigate potential confounding effects of changes in trade barriers.

The key parameter of interest is  $\alpha_1$ , which measures the sensitivity of an industry's robot density to changes in trade policy uncertainty, depending on the industry's initial exposure to offshoring. In what follows, we refer to the interaction between TPU (in log units) and the import share as "trade uncertainty exposures." Our theory suggests that an increase in trade uncertainty should be associated with an increase in robot density, and this response should be stronger for industries that are more exposed to offshoring. Specifically, the impulse responses in Figure 3 show that, in a more open economy, trade uncertainty should lead to a larger increase in robot density. Thus, the theory predicts that  $\alpha_1 > 0$ .

This prediction is supported by the data, as shown in Table 3 (Column (1)). The table shows that, after controlling for the industry and time fixed effects as well as tariffs, an increase in TPU is associated with a larger increase in robot density in industries that are more exposed to offshoring. This correlation is statistically significant at the 99 percent

(2) (1) log(Robot density) log(Import share) Initial import share  $\times \log(\text{TPU})$ 5.251\*\* -1.001\* (1.369)(0.425) $\log(1+Tariff)$ 18.21 -7.598(85.48)(8.167)Industry fixed effect Time fixed effect Observations 161 308  $R^2$ 0.917 0.956Years 2004:2018 1997:2018 No. of industries 14

Table 3. Trade policy uncertainty, automation, and offshoring

Note: Column (1) reports the estimates of the regression of robot density on trade uncertainty proxied by the interaction between TPU and initial exposure to offshoring. Column (2) reports the estimates of the regression of the share of imported intermediate goods in gross output on trade uncertainty. Both regressions control for industry and time fixed effects as well as industry-time-specific tariffs that the U.S. imposes on its imports. Standard errors clustered at the industry level are shown in parentheses. The levels of statistical significance are denoted by asterisks: \*\*\* for p < 0.01, \*\* for p < 0.05, and \* for p < 0.1.

confidence level and economically important. A one-standard-deviation increase in trade uncertainty exposures is associated with an increase in robot density of about 1.29 log points  $(5.251 \times 0.246 \approx 1.29)$ , which is about half of the standard deviation of the logarithm of the robot density (2.73).

Our model also predicts that heightened trade uncertainty reduces offshoring, especially in industries that are initially more exposed to offshoring (see the impulse response of imports to trade uncertainty in Figure 3). This model prediction aligns well with the empirical evidence. Table 3 (Column (2)) shows that, controlling for industry and time fixed effects as well as industry tariffs, an increase in TPU is associated with a larger decline in offshoring for industries that are initially more exposed to importing of intermediate goods.<sup>21</sup> The estimated negative correlation between trade uncertainty and imports of intermediate goods is also economically meaningful. A one-standard-deviation increase in trade uncertainty exposures is associated with a reduction in the share of imported intermediate goods of about  $0.246 \log points (-1.001 \times 0.246 \approx -0.246)$ , which is about one-third of the standard deviation of the import share  $(0.246/0.683 \approx 0.36)$ .<sup>22</sup>

<sup>&</sup>lt;sup>21</sup>We show in the Appendix that TPU has heterogeneous effects on imports from different origin countries. In particular, Table E.1 shows that an increase in TPU is associated with a large and significant decline in imports from China, partly reflecting the effects of sharp increases in bilateral trade tensions (beyond that explained by tariffs) between the United States and China.

<sup>&</sup>lt;sup>22</sup>The estimated coefficient on tariffs in the regression of import shares has the expected signs, but it is statistically insignificant, reflecting the lack of within-industry variations in tariffs in our sample.

	(1)	(2)	(3)	(4)
	log(Labor productivity)	log(Employment)	log(Value Added)	log(Skill premium
Initial import share $\times \log(\text{TPU})$	0.326**	-0.168	0.158	0.143**
	(0.125)	(0.201)	(0.193)	(0.0531)
log(1+Tariff)	-1.088	8.739	7.651	0.983
	(4.409)	(16.85)	(15.11)	(1.757)
Industry fixed effect	✓	✓	✓	✓
Time fixed effect	✓	✓	✓	✓
Observations	264	264	264	308
$\mathbb{R}^2$	0.970	0.943	0.961	0.790
Years	1997:2018	1997:2018	1997:2018	1997:2018
No. of industries	12	12	12	14

Table 4. Trade policy uncertainty, offshoring, and macroeconomic variables

Note: Columns (1), (2), (3), and (4) report the results of regressing labor productivity, employment, value-added, and skill premium, respectively, on the interaction between TPU and initial exposure to offshoring. All regressions control for industry and time fixed effects as well as industry-level tariffs imposed by the U.S.. Standard errors clustered at the industry level are shown in parentheses. The levels of statistical significance are denoted by asterisks: \*\*\* for p < 0.01, \*\* for p < 0.05, and \* for p < 0.1.

V.3. Trade uncertainty and other macroeconomic variables. Our model further predicts that heightened trade policy uncertainty should increase labor productivity, the skill premium, and value-added, while reducing employment (see Figure 1). These model predictions are broadly consistent with the data, as shown in Table 4.

The table shows the same regressions as in equation (48), where we replace the dependent variable with each of the macroeconomic variables of interest. As shown in the table, an increase in TPU is associated with a greater increase in labor productivity and the skill premium in industries more exposed to offshoring in the initial period. These effects are statistically significant and economically important. In particular, a one-standard-deviation increase in trade uncertainty exposures is associated with an increase in labor productivity of about 0.08 log points (0.326  $\times$  0.246  $\approx$  0.08), which is about 16 percent of the standard deviation of labor productivity (0.49). The same increase in trade uncertainty exposures is associated with an increase in the skill premium of about 0.035 log points (0.143  $\times$  0.246  $\approx$  0.035), which is about 35 percent of the standard deviation of the skill premium (0.1).

The correlations between TPU with employment and value-added are imprecisely estimated, reflecting the noise in the relatively small sample. However, the sign of the estimated coefficients are in line with our theoretical predictions.

V.4. The automation channel. In our model, the effects of trade uncertainty on employment, labor productivity, output, and the skill premium work through the automation channel. Specifically, as shown in Figure 2, the automation channel amplifies the responses of labor productivity and the skill premium to a trade uncertainty shock. Trade uncertainty

	(1)	(2)	(3)	(4)
	log(Labor productivity)	log(Employment)	log(Value Added)	log(Skill premium)
Predicted log(Robot density)	0.0608***	-0.0429*	0.0179	0.0389**
	(0.0201)	(0.0229)	(0.0265)	(0.0173)
log(1+Tariff)	-17.75**	-6.568	-24.32***	2.209
	(7.690)	(4.590)	(8.989)	(5.783)
Industry fixed effect	✓	✓	✓	✓
Time fixed effect	✓	✓	✓	✓
Observations	161	161	161	161
Years	2004:2018	2004:2018	2004:2018	2004:2018
No. of industries	12	12	12	12

Table 5. Two-stage least squares: Empirical importance of automation

Note: This table shows the second-stage regressions using the robot density predicted from the first-stage regression shown in Column (1) of Table 3 as the regressor. All regressions control for industry and time fixed effects as well as industry-time-specific tariffs that the U.S. imposes on its imports. Standard errors clustered at the industry level are shown in parentheses. The levels of statistical significance are denoted by asterisks: \*\*\* for p < 0.01, \*\* for p < 0.05, and \* for p < 0.1.

also reduces low-skilled employment in our baseline model, whereas it raises employment in the counterfactual economy with a constant automation probability.

We now present some empirical evidence that is consistent with our model's automation channel. Trade uncertainty can influence macroeconomic variables through multiple channels. To highlight the automation channel, we follow the two-stage estimation procedure of Bertrand and Mullainathan (2001). In the first stage, we regress robot density on the interactions of TPU with initial exposure to offshoring, controlling for industry and time fixed effects. In the second stage, we regress the variables of interest (labor productivity, skill premium, etc.) on the predicted robot density from the first-stage regression, controlling for industry tariffs. We interpret the estimated coefficient on the predicted robot density in the second-stage regression (shown in Table 5) as reflecting the sensitivity of those macroeconomic variables to trade policy uncertainty through the automation channel.

Table 5 shows that an increase in robot density driven by an increase in trade uncertainty is associated with a statistically significant increase in both labor productivity and the skill premium. An increase in robot density driven by trade uncertainty also reduces employment significantly, although it does not have significant effects on value-added. Thus, the increase in labor productivity primarily reflects the job-displacing effects of automation.

The responses of labor productivity, employment, and the skill premium to trade uncertainty through the automation channel are economically important. A one-standard-deviation increase in trade uncertainty exposures is associated with an increase in robot density of 1.29 log points (as shown in the first-stage regression). Working through this automation channel, trade uncertainty raises labor productivity by about 7.8 percent, which is about 16 percent of its standard deviation (1.29  $\times$  0.0608/0.488  $\approx$  0.16). Trade uncertainty also raises the skill premium by about 5 percent, or half of its standard deviation

 $(1.29 \times 0.0389/0.101 \approx 0.5)$  and it reduces employment by about 5.5 percent, which is 9 percent of its standard deviation  $(1.29 \times (-0.0429)/0.611 \approx -0.09)$ . These results suggest that the automation channel is empirically important for the transmission of trade policy uncertainty.

### VI. CONCLUSION

Trade uncertainty has risen in recent years, stemming from risks associated with tariffs, geopolitical tensions, and climate change. This uncertainty has led to a reconsideration of the costs and benefits of offshoring to lower production costs.

In this paper, we have examined how automation affects domestic labor markets when trade uncertainty creates the incentive to reshore production processes from foreign sources back to the domestic market. In our model, domestic firms can produce intermediate goods using either a labor-only technology or an automation technology. Through an expenditure-switching effect, heightened trade uncertainty raises domestic production but not necessarily domestic employment because automation is a labor-substituting technology. Although automation raises productivity and thus labor demand, the job-displacing effect dominates under our calibration. As such, trade uncertainty boosts automation investment while raising unemployment of unskilled workers. Increased automation also leads to a higher skill premium.

Our model's predictions are in line with industry-level empirical evidence. Our evidence suggests that, in industries more exposed to offshoring, heightened trade uncertainty reduces offshoring while stimulating automation relative to other industries. Consistent with our model's predictions, this translates into higher productivity and pushes up the skill premium while lowering employment.

We focus on the positive aspects of the interactions between reshoring, automation, employment, and wages, taking government policy as given. Our model implies that, in line with Leduc and Liu (2023), the threat of automation (e.g., stemming from trade uncertainty) could weaken the bargaining power of unskilled workers. Such endogenous variations in workers' bargaining power can create a potential source of inefficiency that may call for policy interventions. Studying policy implications in a theoretical framework like ours is a promising avenue for future research, and it would complement the recent work of Grossman et al. (2023), who examine optimal policy in a model with critical production input in the face of global supply chain disruptions.

# APPENDIX A. SUMMARY OF EQUILIBRIUM CONDITIONS

A search equilibrium is a system of 30 equations for 30 variables summarized in the vector

$$[r_t, C_t, Y_t, Y_{ft}, Y_{dt}, Q_{dt}, Y_{at}, Y_{nt}, X_t, A_t, p_{dt}, p_{ft}, Q_t, p_{at}, p_{nt}, m_t, u_t, v_t, q_t^u, q_t^v, q_t^a, N_t, U_t, \eta_t, I_t^e, J_t^v, J_t^a, \nu_t^*, w_{nt}, w_{st}].$$

We write the equations in the same order as in the dynare code.

(1) Household's bond Euler equation:

$$1 = \mathcal{E}_t \beta \frac{C_t}{C_{t+1}} r_t, \tag{A.1}$$

(2) Matching function

$$m_t = \mu u_t^{\alpha} v_t^{1-\alpha},\tag{A.2}$$

(3) Job finding rate

$$q_t^u = \frac{m_t}{u_t},\tag{A.3}$$

(4) Vacancy filling rate

$$q_t^v = \frac{m_t}{v_t},\tag{A.4}$$

(5) Employment dynamics

$$N_t = (1 - \delta)N_{t-1} + m_t, \tag{A.5}$$

(6) Number of searching workers

$$u_t = 1 - (1 - \delta)N_{t-1},\tag{A.6}$$

(7) Unemployment

$$U_t = 1 - N_t, \tag{A.7}$$

(8) Vacancy dynamics

$$v_t = (1 - q_{t-1}^v)(1 - q_t^a)v_{t-1} + \delta N_{t-1} + \eta_t, \tag{A.8}$$

(9) Automation dynamics

$$A_t = (1 - \rho^o)A_{t-1} + q_t^a(1 - q_{t-1}^v)v_{t-1}, \tag{A.9}$$

(10) Employment value

$$J_t^e = p_{nt} Z_t - w_{nt} + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left[ \delta J_{t+1}^v + (1 - \delta) J_{t+1}^e \right], \tag{A.10}$$

(11) Vacancy value

$$J_t^v = -\kappa + q_t^v J_t^e + (1 - q_t^v) \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left\{ (1 - q_{t+1}^a) J_{t+1}^v + q_{t+1}^a J_{t+1}^a - \int_0^{\nu_{t+1}^*} \nu dG(\nu) \right\}. \quad (A.11)$$

(12) Automation value

$$J_t^a = p_{at} \gamma_a Z_t \zeta^{\gamma_a} \left( \frac{\bar{s}}{A_t} \right)^{1 - \gamma_a} (1 - \kappa_a) + (1 - \rho^o) \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} J_{t+1}^a, \tag{A.12}$$

(13) Automation threshold

$$\nu_t^* = J_t^a - J_t^v, \tag{A.13}$$

(14) Robot adoption

$$q_t^a = \left(\frac{\nu_t^*}{\bar{\nu}}\right)^{\eta_a},\tag{A.14}$$

(15) Vacancy creation

$$\eta_t = \left(\frac{J_t^v}{\bar{e}}\right)^{\eta_e},\tag{A.15}$$

(16) Final goods output

$$Y_t = \left[ \alpha_d^{\frac{1}{\theta}} Y_{dt}^{\frac{\theta - 1}{\theta}} + (1 - \alpha_d)^{\frac{1}{\theta}} Y_{f,t-1}^{\frac{\theta - 1}{\theta}} \right]^{\frac{\theta}{\theta - 1}}, \tag{A.16}$$

(17) Domestic intermediate goods production

$$Q_{dt} = \left[\alpha_n^{\frac{1}{\sigma}} Y_{nt}^{\frac{\sigma-1}{\sigma}} + (1 - \alpha_n)^{\frac{1}{\sigma}} Y_{at}^{\frac{\sigma-1}{\sigma}}\right]^{\frac{\sigma}{\sigma-1}},\tag{A.17}$$

(18) Domestic intermediate goods feasibility constraint.

$$Q_{dt} = Y_{dt} + \tau_t X_t, \tag{A.18}$$

(19) Intermediate goods produced by workers

$$Y_{nt} = Z_t N_t, \tag{A.19}$$

(20) Intermediate goods produced by robots

$$Y_{at} = Z_t(\zeta A_t)^{\gamma_a} \bar{s}^{1-\gamma_a}, \tag{A.20}$$

(21) Demand for domestically produced intermediate goods

$$p_{dt} = \left(\frac{\alpha_d Y_t}{Y_{dt}}\right)^{\frac{1}{\theta}},\tag{A.21}$$

(22) Demand for imported intermediate goods

$$p_{ft} = \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left( \frac{(1 - \alpha_d) Y_{t+1}}{Y_{ft}} \right)^{\frac{1}{\theta}}$$
(A.22)

(23) Relative price of worker-produced domestic intermediate goods

$$\frac{p_{nt}}{p_{dt}} = \left(\frac{\alpha_n Y_{dt}}{Y_{nt}}\right)^{\frac{1}{\sigma}},\tag{A.23}$$

(24) Relative price of robot-produced domestic intermediate goods

$$\frac{p_{at}}{p_{dt}} = \left(\frac{(1 - \alpha_n)Y_{dt}}{Y_{at}}\right)^{\frac{1}{\sigma}},\tag{A.24}$$

(25) Foreign demand for exported intermediate goods

$$X_t = \left(\frac{\tau_t p_{dt}}{\mathcal{Q}_t}\right)^{-\theta} X_t^*,\tag{A.25}$$

(26) Balanced trade condition:

$$\tau_t p_{dt} X_t = p_{ft} Y_{ft}, \tag{A.26}$$

(27) Import price:

$$p_{ft} = \tau_t \mathcal{Q}_t, \tag{A.27}$$

(28) Resource constraint

$$C_t + \kappa v_t + \kappa_a \gamma_a p_{at} Y_{at} + (1 - q_{t-1}^v) v_{t-1} \int_0^{\nu_t^*} \nu dG(\nu) + \int_0^{J_t^v} e dF(e) = Y_t.$$
 (A.28)

(29) Nash bargaining wage

$$\frac{b}{1-b}(J_t^e - J_t^v) = w_{nt} - \phi - \chi C_t + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} (1 - q_{t+1}^u)(1 - \delta) \frac{b}{1-b} (J_{t+1}^e - J_{t+1}^v), \quad (A.29)$$

(30) Skilled wage

$$w_{st} = (1 - \gamma_a) p_{at} Z_t \left(\frac{\zeta}{\bar{s}}\right)^{\gamma_a}. \tag{A.30}$$

## APPENDIX B. CAPITAL FLOWS

The baseline economy has a closed capital account, such that the interest rate is endogenous. Now we consider an alternative framework where international capital flows are allowed.

The small open economy can borrow from or lend to the rest of the world at the exogenous world interest rate  $r_t^*$  (in units of foreign consumption goods). Denote by  $B_t^*$  the net capital outflows (i.e., lending to the rest of the world). To capture the frictions in capital markets, we assume that changes in capital flows are subject to an adjustment cost. In this environment, the budget constraint for the representative household is given by

$$C_t + \mathcal{Q}_t B_t^* + \frac{\psi}{2} \mathcal{Q}_t (B_t^* - \bar{B}^*)^2 = r_{t-1}^* \mathcal{Q}_t B_{t-1}^* + w_{nt} N_t + w_{st} \bar{s} + \phi (1 - N_t) + d_t - T_t, \quad \forall t \ge 0, \text{ (B.1)}$$

where  $Q_t$  denotes the real exchange rate (units of domestic consumption goods per unit of foreign consumption goods),  $\psi \geq 0$  is a parameter measuring the size of the bond adjustment costs, and  $\bar{B}^*$  denotes the steady-state level of foreign lending.

The intertemporal Euler equation is given by

$$1 + \psi(B_t^* - \bar{B}^*) = E_t D_{t,t+1} \frac{Q_{t+1}}{Q_t} r_t^*.$$
 (B.2)

The Euler equation is a generalization of the standard uncovered interest parity (UIP) condition. The presence of bond adjustment costs implies an upward-sloping supply curve of foreign lending: the amount of foreign lending (relative to the steady-state level) increases with the world interest rate  $r_t^*$  adjusted for expected real exchange rate depreciation.

In equilibrium, the balance-of-payment condition implies that the current account balance (i.e., net capital outflows) should be equal to the trade balance (i.e., net exports) plus net interest payments received from abroad. This balance-of-payments condition is given by

$$Q_t(B_t^* - B_{t-1}^*) = \tau_t p_{dt} X_t - p_{ft} Y_{ft} + (r_t^* - 1) Q_t B_{t-1}^*.$$
(B.3)

The aggregate resource constraint is given by

$$C_{t} + \tau_{t} p_{dt} X_{t} - p_{ft} Y_{ft} = Y_{t} - \kappa v_{t} - \kappa_{a} \gamma_{a} p_{at} Y_{at} - (1 - q_{t-1}^{v}) v_{t-1} \int_{0}^{\nu_{t}^{*}} \nu dG(\nu) - \int_{0}^{J_{t}^{v}} e dF(e) - \frac{\psi}{2} \mathcal{Q}_{t} (B_{t}^{*} - \bar{B}^{*})^{2},$$
(B.4)

where the left side gives the real GDP, which equals consumption plus net exports.

B.1. Summary of equilibrium conditions. A search equilibrium is a system of 30 equations for 30 variables summarized in the vector

$$[B_t, C_t, Y_t, Y_{ft}, Y_{dt}, Q_{dt}, Y_{at}, Y_{nt}, X_t, A_t, p_{dt}, p_{ft}, Q_t, p_{at}, p_{nt}, m_t, u_t, v_t, q_t^u, q_t^v, q_t^a, N_t, U_t, \eta_t, J_t^e, J_t^v, J_t^a, \nu_t^*, w_{nt}, w_{st}].$$

We write the equations in the same order as in the dynare code.

(1) Household's bond Euler equation:

$$1 + \psi(B_t^* - \bar{B}^*) = E_t D_{t,t+1} \frac{Q_{t+1}}{Q_t} r_t^*$$
(B.5)

(2) Matching function

$$m_t = \mu u_t^{\alpha} v_t^{1-\alpha},\tag{B.6}$$

(3) Job finding rate

$$q_t^u = \frac{m_t}{u_t},\tag{B.7}$$

(4) Vacancy filling rate

$$q_t^v = \frac{m_t}{v_t},\tag{B.8}$$

(5) Employment dynamics

$$N_t = (1 - \delta)N_{t-1} + m_t, \tag{B.9}$$

(6) Number of searching workers

$$u_t = 1 - (1 - \delta)N_{t-1},\tag{B.10}$$

(7) Unemployment

$$U_t = 1 - N_t, \tag{B.11}$$

(8) Vacancy dynamics

$$v_t = (1 - q_{t-1}^v)(1 - q_t^a)v_{t-1} + \delta N_{t-1} + \eta_t,$$
(B.12)

(9) Automation dynamics

$$A_t = (1 - \rho^o)A_{t-1} + q_t^a (1 - q_{t-1}^v)v_{t-1}, \tag{B.13}$$

(10) Employment value

$$J_t^e = p_{nt} Z_t - w_{nt} + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left[ \delta J_{t+1}^v + (1 - \delta) J_{t+1}^e \right], \tag{B.14}$$

(11) Vacancy value

$$J_t^v = -\kappa + q_t^v J_t^e + (1 - q_t^v) \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left\{ (1 - q_{t+1}^a) J_{t+1}^v + q_{t+1}^a J_{t+1}^a - \int_0^{\nu_{t+1}^*} \nu dG(\nu) \right\}. \quad (B.15)$$

(12) Automation value

$$J_t^a = p_{at} \gamma_a Z_t \zeta^{\gamma_a} \left( \frac{\bar{s}}{A_t} \right)^{1 - \gamma_a} (1 - \kappa_a) + (1 - \rho^o) \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} J_{t+1}^a, \tag{B.16}$$

(13) Automation threshold

$$\nu_t^* = J_t^a - J_t^v, \tag{B.17}$$

(14) Robot adoption

$$q_t^a = \left(\frac{\nu_t^*}{\bar{\nu}}\right)^{\eta_a},\tag{B.18}$$

(15) Vacancy creation

$$\eta_t = \left(\frac{J_t^v}{\bar{e}}\right)^{\eta_e},\tag{B.19}$$

(16) Final goods output

$$Y_t = \left[ \alpha_d^{\frac{1}{\theta}} Y_{dt}^{\frac{\theta - 1}{\theta}} + (1 - \alpha_d)^{\frac{1}{\theta}} Y_{f,t-1}^{\frac{\theta - 1}{\theta}} \right]^{\frac{\theta}{\theta - 1}}, \tag{B.20}$$

(17) Domestic intermediate goods production

$$Q_{dt} = \left[\alpha_n^{\frac{1}{\sigma}} Y_{nt}^{\frac{\sigma-1}{\sigma}} + (1 - \alpha_n)^{\frac{1}{\sigma}} Y_{at}^{\frac{\sigma-1}{\sigma}}\right]^{\frac{\sigma}{\sigma-1}},\tag{B.21}$$

(18) Domestic intermediate goods feasibility constraint.

$$Q_{dt} = Y_{dt} + \tau_t X_t, \tag{B.22}$$

(19) Intermediate goods produced by workers

$$Y_{nt} = Z_t N_t, (B.23)$$

(20) Intermediate goods produced by robots

$$Y_{at} = Z_t(\zeta A_t)^{\gamma_a} \bar{s}^{1-\gamma_a}, \tag{B.24}$$

(21) Demand for domestically produced intermediate goods

$$p_{dt} = \left(\frac{\alpha_d Y_t}{Y_{dt}}\right)^{\frac{1}{\theta}},\tag{B.25}$$

(22) Demand for imported intermediate goods

$$p_{ft} = \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left( \frac{(1 - \alpha_d) Y_{t+1}}{Y_{ft}} \right)^{\frac{1}{\theta}}$$
(B.26)

(23) Relative price of worker-produced domestic intermediate goods

$$\frac{p_{nt}}{p_{dt}} = \left(\frac{\alpha_n Y_{dt}}{Y_{nt}}\right)^{\frac{1}{\sigma}},\tag{B.27}$$

(24) Relative price of robot-produced domestic intermediate goods

$$\frac{p_{at}}{p_{dt}} = \left(\frac{(1 - \alpha_n)Y_{dt}}{Y_{at}}\right)^{\frac{1}{\sigma}},\tag{B.28}$$

(25) Foreign demand for exported intermediate goods

$$X_t = \left(\frac{\tau_t p_{dt}}{\mathcal{Q}_t}\right)^{-\theta} X_t^*,\tag{B.29}$$

(26) Balance of payments condition:

$$Q_t(B_t^* - B_{t-1}^*) = \tau_t p_{dt} X_t - p_{ft} Y_{ft} + (r_t^* - 1) Q_t B_{t-1}$$
(B.30)

(27) Import price:

$$p_{ft} = \tau_t \mathcal{Q}_t, \tag{B.31}$$

(28) Resource constraint

$$C_{t} + \tau_{t} p_{dt} X_{t} - p_{ft} Y_{ft} = Y_{t} - \kappa v_{t} - \kappa_{a} \gamma_{a} p_{at} Y_{at} - (1 - q_{t-1}^{v}) v_{t-1} \int_{0}^{\nu_{t}^{*}} \nu dG(\nu) - \int_{0}^{J_{t}^{v}} e dF(e) - \frac{\psi}{2} \mathcal{Q}_{t} (B_{t}^{*} - \bar{B}^{*})^{2}$$
(B.32)

(29) Nash bargaining wage

$$\frac{b}{1-b}(J_t^e - J_t^v) = w_{nt} - \phi - \chi C_t + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} (1 - q_{t+1}^u)(1 - \delta) \frac{b}{1-b} (J_{t+1}^e - J_{t+1}^v), \quad (B.33)$$

(30) Skilled wage

$$w_{st} = (1 - \gamma_a) p_{at} Z_t \left(\frac{\zeta}{\bar{s}}\right)^{\gamma_a}. \tag{B.34}$$

## Appendix C. Imported intermediate inputs for automated production

This section considers a generalization of the baseline model to include imported intermediate goods for automating firms.

C.1. Changes relative to the baseline model. Denote by  $x_{at}$  the imported input for an automating firm. The production function for a firm that operates an automation technology is given by

$$y_{at} = Z_t \left( \zeta^{1-\gamma_f} x_{at}^{\gamma_f} \right)^{\gamma_a} s_t^{1-\gamma_a}, \tag{C.1}$$

where  $1-\gamma_a$  denotes the share of skilled labor and  $\gamma_f$  denotes the share of imported non-labor (equipment) input.

The firm takes as given the relative price of imported inputs  $p_{ft}$  and the real wage rate  $w_{st}$  of skilled workers and chooses  $x_{at}$  and  $s_t$  to maximize the profit before paying the robot operation cost  $\kappa_a$ . The value of automation is then given by

$$J_t^a = \pi_t^a (1 - \kappa_a) + (1 - \rho^o) \mathbb{E}_t D_{t,t+1} J_{t+1}^a, \tag{C.2}$$

where

$$\pi_t^a \equiv \max_{x_{at}, s_t} \quad p_{at} Z_t \left( \zeta^{1-\gamma_f} x_{at}^{\gamma_f} \right)^{\gamma_a} s_t^{1-\gamma_a} - p_{ft} x_{at} - w_{st} s_t = \gamma_a (1-\gamma_f) p_{at} \frac{Y_{at}}{A_t},$$

where we have imposed the market clearing condition that  $Y_{at} = A_t y_{at}$ .

The aggregate output of all automating firms is given by

$$Y_{at} = Z_t \left( \zeta A_t \right)^{(1-\gamma_f)\gamma_a} X_{at}^{\gamma_f \gamma_a} \bar{s}^{1-\gamma_a}, \tag{C.3}$$

where  $X_{at} = A_t x_{at}$  denotes the aggregate imports of intermediate input used by all automating firms.

The input demand functions can be written in terms of aggregate variables and they are given by

$$p_{ft} = \gamma_f \gamma_a p_{at} \frac{Y_{at}}{X_{at}}$$

$$w_{st} = (1 - \gamma_a) p_{at} \frac{Y_{at}}{\bar{s}}.$$
(C.4)

$$w_{st} = (1 - \gamma_a) p_{at} \frac{Y_{at}}{\bar{s}}. \tag{C.5}$$

The trade balance condition in the baseline model needs to be modified accordingly and it is now given by

$$\tau_t p_{dt} X_t = p_{ft} (Y_{ft} + X_{at}). \tag{C.6}$$

Compared to the baseline model, we have an extra endogenous variable  $X_{at}$  and an extra equation (C.4). There is an extra parameter  $\gamma_f$  to be calibrated. We set it to  $\gamma_f = 0.15$ , such that the home bias in the automation sector is the same as in the final goods sector.

C.2. Summary of equilibrium conditions. A search equilibrium is a system of 31 equations for 31 variables summarized in the vector

$$[r_t, C_t, Y_t, Y_{ft}, Y_{dt}, Q_{dt}, Y_{at}, Y_{nt}, X_t, A_t, p_{dt}, p_{ft}, Q_t, p_{at}, p_{nt}, m_t, u_t, v_t, q_t^u, q_t^v, q_t^a, N_t, U_t, \eta_t, I_t^e, J_t^v, J_t^a, \nu_t^*, w_{nt}, w_{st}, X_{at}].$$

We write the equations in the same order as in the dynare code.

(1) Household's bond Euler equation:

$$1 = \mathcal{E}_t \beta \frac{C_t}{C_{t+1}} r_t, \tag{C.7}$$

(2) Matching function

$$m_t = \mu u_t^{\alpha} v_t^{1-\alpha},\tag{C.8}$$

(3) Job finding rate

$$q_t^u = \frac{m_t}{u_t},\tag{C.9}$$

(4) Vacancy filling rate

$$q_t^v = \frac{m_t}{v_t},\tag{C.10}$$

(5) Employment dynamics

$$N_t = (1 - \delta)N_{t-1} + m_t, \tag{C.11}$$

(6) Number of searching workers

$$u_t = 1 - (1 - \delta)N_{t-1},$$
 (C.12)

(7) Unemployment

$$U_t = 1 - N_t, \tag{C.13}$$

(8) Vacancy dynamics

$$v_t = (1 - q_{t-1}^v)(1 - q_t^a)v_{t-1} + \delta N_{t-1} + \eta_t, \tag{C.14}$$

(9) Automation dynamics

$$A_t = (1 - \rho^o)A_{t-1} + q_t^a(1 - q_{t-1}^v)v_{t-1}, \tag{C.15}$$

(10) Employment value

$$J_t^e = p_{nt} Z_t - w_{nt} + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left[ \delta J_{t+1}^v + (1 - \delta) J_{t+1}^e \right], \tag{C.16}$$

(11) Vacancy value

$$J_t^v = -\kappa + q_t^v J_t^e + (1 - q_t^v) \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left\{ (1 - q_{t+1}^a) J_{t+1}^v + q_{t+1}^a J_{t+1}^a - \int_0^{\nu_{t+1}^*} \nu dG(\nu) \right\}. \quad (C.17)$$

(12) Automation value

$$J_t^a = \gamma_a (1 - \gamma_f) p_{at} \frac{Y_{at}}{A_t} (1 - \kappa_a) + (1 - \rho^o) \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} J_{t+1}^a$$
 (C.18)

(13) Automation threshold

$$\nu_t^* = J_t^a - J_t^v, \tag{C.19}$$

(14) Robot adoption

$$q_t^a = \left(\frac{\nu_t^*}{\bar{\nu}}\right)^{\eta_a},\tag{C.20}$$

(15) Vacancy creation

$$\eta_t = \left(\frac{J_t^v}{\bar{e}}\right)^{\eta_e},\tag{C.21}$$

(16) Final goods output

$$Y_t = \left[ \alpha_d^{\frac{1}{\theta}} Y_{dt}^{\frac{\theta - 1}{\theta}} + (1 - \alpha_d)^{\frac{1}{\theta}} Y_{f,t-1}^{\frac{\theta - 1}{\theta}} \right]^{\frac{\theta}{\theta - 1}}, \tag{C.22}$$

(17) Domestic intermediate goods production

$$Q_{dt} = \left[\alpha_n^{\frac{1}{\sigma}} Y_{nt}^{\frac{\sigma-1}{\sigma}} + (1 - \alpha_n)^{\frac{1}{\sigma}} Y_{at}^{\frac{\sigma-1}{\sigma}}\right]^{\frac{\sigma}{\sigma-1}},\tag{C.23}$$

(18) Domestic intermediate goods feasibility constraint.

$$Q_{dt} = Y_{dt} + \tau_t X_t, \tag{C.24}$$

(19) Intermediate goods produced by workers

$$Y_{nt} = Z_t N_t, (C.25)$$

(20) Intermediate goods produced by robots

$$Y_{at} = Z_t \left( \zeta A_t \right)^{(1-\gamma_f)\gamma_a} X_{at}^{\gamma_f \gamma_a} \bar{s}^{1-\gamma_a}, \tag{C.26}$$

(21) Demand for domestically produced intermediate goods

$$p_{dt} = \left(\frac{\alpha_d Y_t}{Y_{dt}}\right)^{\frac{1}{\theta}},\tag{C.27}$$

(22) Demand for imported intermediate goods

$$p_{ft} = \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \left( \frac{(1 - \alpha_d) Y_{t+1}}{Y_{ft}} \right)^{\frac{1}{\theta}} \tag{C.28}$$

(23) Relative price of worker-produced domestic intermediate goods

$$\frac{p_{nt}}{p_{dt}} = \left(\frac{\alpha_n Y_{dt}}{Y_{nt}}\right)^{\frac{1}{\sigma}},\tag{C.29}$$

(24) Relative price of robot-produced domestic intermediate goods

$$\frac{p_{at}}{p_{dt}} = \left(\frac{(1 - \alpha_n)Y_{dt}}{Y_{at}}\right)^{\frac{1}{\sigma}},\tag{C.30}$$

(25) Foreign demand for exported intermediate goods

$$X_t = \left(\frac{\tau_t p_{dt}}{\mathcal{Q}_t}\right)^{-\theta} X_t^*,\tag{C.31}$$

(26) Balanced trade condition:

$$\tau_t p_{dt} X_t = p_{ft} (Y_{ft} + X_{at}). \tag{C.32}$$

(27) Import price:

$$p_{ft} = \tau_t \mathcal{Q}_t, \tag{C.33}$$

(28) Resource constraint

$$C_t + \kappa v_t + \kappa_a \gamma_a p_{at} Y_{at} + (1 - q_{t-1}^v) v_{t-1} \int_0^{\nu_t^*} \nu dG(\nu) + \int_0^{J_t^v} e dF(e) = Y_t.$$
 (C.34)

(29) Nash bargaining wage

$$\frac{b}{1-b}(J_t^e - J_t^v) = w_{nt} - \phi - \chi C_t + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} (1 - q_{t+1}^u)(1 - \delta) \frac{b}{1-b} (J_{t+1}^e - J_{t+1}^v), \quad (C.35)$$

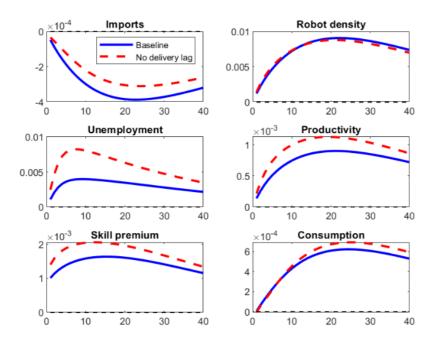
(30) Skilled wage

$$w_{st} = (1 - \gamma_a) p_{at} \frac{Y_{at}}{\bar{s}} \tag{C.36}$$

(31) Demand for imported input by automating firms

$$p_{ft} = \gamma_f \gamma_a p_{at} \frac{Y_{at}}{X_{at}} \tag{C.37}$$

FIGURE D.1. Impulse responses to a trade uncertainty shock: No delivery lags.



APPENDIX D. ADDITIONAL MODEL RESULTS

D.1. No delivery lags. In the baseline model, we assume that importing intermediate inputs for final goods production requires a delivery lag. To show that our main results do not depend on this assumption, we consider a version of the model without delivery lags. The final goods production function (15) is replaced by

$$Y_t = \left[ \alpha_d^{\frac{1}{\theta}} Y_{dt}^{\frac{\theta - 1}{\theta}} + (1 - \alpha_d)^{\frac{1}{\theta}} Y_{ft}^{\frac{\theta - 1}{\theta}} \right]^{\frac{\theta}{\theta - 1}}.$$
 (D.1)

The demand for imported intermediate goods in Eq. (22) is replaced by

$$p_{ft} = \left(\frac{(1 - \alpha_d)Y_t}{Y_{ft}}\right)^{\frac{1}{\theta}}.$$
 (D.2)

The rest of the equilibrium conditions remain the same.

We use the same calibrated parameters to simulate the impulse responses to a trade uncertainty shock. Figure D.1 shows that the impulse response are qualitatively similar to those in the baseline model shown in Figure 1., although the magnitude of the responses are slightly different. For example, compared to the baseline model, trade uncertainty in the model without delivery lags leads to a smaller expenditure-switching effect. Thus, imports decline less, unemployment rises more, and robot density increases less.

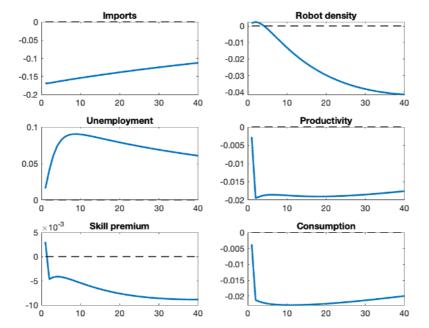


FIGURE D.2. Impulse responses to a first-moment trade cost shock.

D.2. Other shocks. The effects of trade uncertainty are different from those of a first-moment shock to trade costs. Figure D.2 shows the impulse responses to a first-moment trade cost shock. When the trade cost rises, imports fall persistently. The increase in trade costs worsens the terms of trade, raising the cost of final goods production and resulting in lower automation and higher unemployment. The decline in automation reduces labor productivity, further exacerbating the recessionary effects of the shock, leading to persistent drops in consumption. The decline in automation also reduces the demand for skilled workers, resulting in a fall in the skill premium.

Figure D.3 shows that, unlike trade uncertainty, TFP uncertainty encourages offshoring, resulting in an increase in imports. TFP uncertainty has a recessionary effect, raising unemployment and reducing consumption. Unlike trade uncertainty that boosts automation, TFP uncertainty lowers to persistent declines in robot density after the initial increases. Accordingly, labor productivity declines persistently following initial increases.

Figure D.4 shows the impulse responses to a first-moment shock to TFP. An increase in TFP lowers unemployment and stimulates automation investment, leading to persistent increases in productivity and aggregate consumption. The rise in automation also leads to a higher skill premium. The increase in productivity leads to real exchange rate depreciation (not shown in the figure), resulting in lower imports.

FIGURE D.3. Impulse responses to a TFP uncertainty shock.

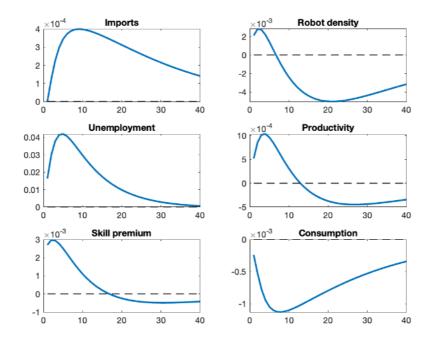
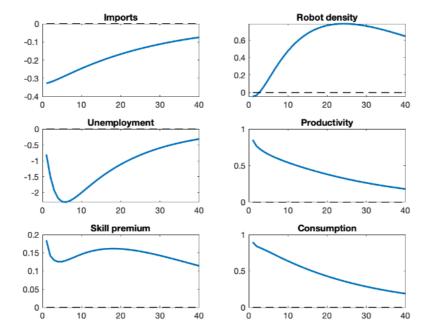


FIGURE D.4. Impulse responses to a first-moment TFP shock.



## APPENDIX E. ADDITIONAL EMPIRICAL RESULTS

Table E.1 shows that TPU has a greater negative effects on the import shares of industries that are more exposed to offshoring in the three largest trading partners of the United States: Mexico, Canada, and China. The effects for China are statistically significant at the 99 percent level, possibly reflecting the sharp increases in bilateral trade tensions between the United States and China since 2016.

Table E.1. Trade policy uncertainty and import shares from different origins

	(1)	(2)	(3)	(4)
	log(Mexico)	log(Canada)	log(China)	log(Vietnam)
Initial Import Share $\times \log(\text{TPU})$	-1.494	-0.0613	-1.583***	-1.069
	(1.128)	(0.247)	(0.301)	(2.116)
log(1+Tariff)	4.889	-13.90	-2.597	42.88
	(5.709)	(8.236)	(38.50)	(66.50)
Industry fixed effect	✓	✓	✓	✓
Time fixed effect	✓	✓	✓	✓
Observations	308	308	308	299
$\mathbb{R}^2$	0.973	0.975	0.887	0.835
Years	1997:2018	1997:2018	1997:2018	1997:2018
No. of industries	14	14	14	14

Note: Each column reports the results of regressing the import share from a particular origin on the interaction between TPU and initial exposure to offshoring. China import share, for example, measures U.S. intermediate imports from China in a particular industry divided by gross output in that industry. All regressions control for industry and time fixed effects as well as industry-time-specific tariffs that the U.S. imposes on its imports. Standard errors clustered at the industry level are shown in parentheses. The levels of statistical significance are denoted by asterisks: \*\*\* for p < 0.01, \*\* for p < 0.05, and \* for p < 0.1.

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