### Wesley J. Wildman — Boston University — 2012-2013 — STH TT871

### **Description**

This course is an introduction to historic and recent scientific theories to the depth needed for reading with understanding most literature in the philosophy and history of science, in religion and science, and in some basic science journals. Another aim of this class is to identify "boundary questions" in the science discussed and to point out how these questions have inspired and influence work in philosophy and religion.

This is not a "popular science" or "science for humanities" course. Literacy in certain disciplines is the goal and, to attain it, the competency required far exceeds that of popular science. For example, a significant amount of mathematics is needed to grasp a large swathe of literature in the philosophy of physics, and most philosophy of biology presumes a detailed knowledge of evolutionary theory.

The pedagogical challenge of this course is to provide this competence in one year available. More familiar methods of science instruction do not work, as they require time-consuming practices such as lab work, memorization, and gaining familiarity with mathematical notation and ideas through repeated calculation. Other methods are adopted in this course and will be discussed, as well as used, in class.

The course is a requirement in the Religion & Science doctoral program. It is the only official course at a Boston Theological Institute (BTI) school that satisfies the science literacy requirement of the BTI's Science and Religion Certificate program. In fact, one semester of the class will satisfy the BTI certificate requirement, but do consult with the instructor well in advance to make sure that you have the necessary background if you plan to take the physics (second) semester of the course.

### **Description**

This course is an introduction to historic and recent scientific theories to the depth needed for reading with understanding most literature in the philosophy and history of science, in religion and science, and in some basic science journals. The class also identifies "boundary questions" in the science discussed and to point out how these questions have inspired and influence work in philosophy and religion.

### Learning Goals

By the end of this course, students should:

- be able to access most literature in the philosophy and history of science, most literature in religion and science, and some literature in basic science journals; and
- possess a solid understanding of how boundary questions—the questions that arise within scientific work that cannot be answered within the sciences themselves—influence philosophical, theological, and ethical reflection.

### **Requirements**

Attendance at both the science lectures (Wednesdays 8-11, STH 115) and the math lectures (Thursday 7:15-9:25, STH 115) is required for students taking the full year, such as those in the SPR program. Other students may take just the biology section in the Fall. Students wanting to take just the physics section in the Spring must attend the math section in the Fall as well, unless attendance is waived by the instructor. In addition:

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- You do not need to purchase texts for this course. The instructors will provide texts where necessary, as well as extensive lecture notes. Reading consists in carefully studying these texts and lecture notes. Aritcles or short books may be assigned to prepare for a segment.
- Each student must have email and web access. This is provided free of charge for registered Boston University students. Documents are shared over email and there is a web site in support of the course under <a href="http://blackboard.bu.edu/">http://blackboard.bu.edu/</a>.
- CD-ROM-based science learning programs may also be required and are available for students to use as needed. Each student should have access to a CD-ROM drive and a computer capable of running these programs. Detailed requirements will be discussed in class.

A grade for the course is assigned on the basis of:

- passing end-of-segment oral examinations with the instructors (see below for details);
- attendance at lectures and tutorials; and
- successful completion of periodic homework assignments.

# **Policies**

Incompletes are not allowed—as a matter of fairness—except in cases of serious emergencies. Don't leave your emergency to the last minute. Paperwork is necessary.

Students with Disabilities—Any students in this course who have a disability that might prevent them from fully demonstrating their abilities should meet with the instructor as soon as possible to initiate disability verification and discuss accommodations that may be necessary to ensure your full participation in the successful completion of course requirements.

Students taking the course for doctoral credit are required to do all work at a doctoral level. In addition, students should submit one 1000-word review of a recent book related to the course content for publication in an appropriate journal. This review is in addition to regular coursework.

The STH Academic Code of Conduct may be found on the STH website at: <u>www.bu.edu/sth/academic/academic-conduct</u>. All students are required to familiarize themselves with this code, its definitions of misconduct, and its sanctions. Students should especially familiarize themselves with the section on plagiarism.

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# Course Schedule for Biology Semester (Fall (2012)

The course is divided into 4 sections. Please see below for what we'll be delving into each week:

| Week/Date        | Topics of Interest   | Assigned Readings  | Homework or<br>Presentation                               |
|------------------|--|--|---|
| Section 1: Basic | Physics, Chemistry and Biology   |  |   |
| Week 1           | <ul> <li>-Introduction to course</li> <li>Setting up goals for the class/semester</li> <li>-Introduction to quantum chemistry, periodic table;<br/>housekeeping discussions of pedagogical philosophy<br/>for the biology section</li> </ul>   | None   |   |
| Week 2           | -General Chemistry (atoms, bonds, molecules)<br>-Introduction to Chemical Transmission –<br>Neurotransmitters (NTM)  | <ol> <li>Freeman Chp.</li> <li>The atoms and<br/>molecules of the<br/>Ancient world</li> </ol>   |   |
| Week 3           | <ul> <li>Origin of organic molecules and life on Earth</li> <li>From biochemistry to cell biology (lipids, proteins)</li> <li>Processes of cell division (mitosis and meiosis);</li> <li>Introduction to energy and metabolism</li> <li>Introduction to Behavioral Neuroscience (BN) research methods</li> </ul> | <ol> <li>Freeman Chp.</li> <li>Macromolecules<br/>and the RNA<br/>World</li> <li>Freeman Chp.</li> <li>Members and<br/>the first cells</li> <li>Freeman Chp.</li> <li>Cell structure<br/>and function</li> <li>Freeman Chp.</li> <li>Cell division</li> <li>Freeman Chp.</li> <li>Cell division</li> <li>Freeman Chp.</li> <li>Cell division</li> <li>Freeman Chp.</li> <li>Meiosis</li> </ol> | Sign up for<br>presentation of<br>organelle<br>structures |
| Section 2: Intro | duction to the Brain   |  |   |
| Week 4           | Neural Transmission – Part I   | <ol> <li>Freeman Chp.</li> <li>Electrical signals in animals</li> </ol>  | Sign up for<br>Journal<br>Presentation                    |
| Week 5           | Neural Transmission – Part II  |  |   |
| Week 6           | Neuroanatomy – Part I  | 1) Freeman Chp.<br>18: Introduction to   |   |

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|               |   | Development   |  |
|---------------|---|---|--|
|               |   | 2) Freeman Chp.<br>19: Early<br>Development                           |  |
| Week 7        | Neuroanatomy – Part II  |   |  |
| Section 3: A  | Case Study on Parkinson's Disease and Associated Neu  | ropsychological Deficit   | 8  |
| Week 8        | Introduction to Parkinson's disease   | See assigned readings   | Sign up for<br>Neurological<br>Disease<br>Presentation     |
| Week 9        | Executive Cognitive Deficits in Parkinson's disease   | See assigned readings   | Sign up for<br>presentation<br>about Frontal<br>Lobe Tests |
| Week 10       | Personality in Parkinson's disease  | See assigned readings   | Sign up for<br>Personality in<br>PD<br>presentation        |
| Section 4: Ex | volutionary Approaches and Neurocognitive Theories of   | Religion  |  |
| Week 11       | Introduction to Evolutionary Theory – Part I  | 1) Freeman Chp. 21:<br>Darwinism and the<br>Evidence for<br>Evolution |  |
|               |   | 2) Freeman Chp. 22:<br>Evolutionary<br>Processes                      |  |
|               |   | 3) Freeman Chp. 23:<br>Speciation                                     |  |
|               |   | 4) Freeman Chp. 24:<br>The History of Life                            |  |
| Week 12       | No Class – Fall Recess – Thanksgiving   |   |  |
| Week 13       | Introduction to Evolutionary Theory – Part II:<br>Evolutionary Theories of Religion from the<br>Perspective of Cognitive Neuroscience | See assigned readings   | Sign up for<br>Action Script<br>Generation<br>Presentation |
| Week 14       | Neurologic Constraints on Evolutionary Theories of  |   |  |

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| Religion |  |
|----------|--|

#### **Reading List for Biology Semester**

#### Week 8: Introduction to Parkinson's disease

- Chaudhuri, K. R., Healy, D. G., & Schapira, A. H. V. (2005). Non-motor symptoms of Parkinson's disease: Diagnosis and management. *The Lancet Neurology*, *5*(3), 235-245.
- Jankovic, J. (2008). Parkinson's disease: Clinical features and diagnosis. *Journal of Neurology, Neurosurgery and Psychiatry,* 79, 368-376.
- Langston, J. W., Ballard, P., Tetrud, J. W., & Irwin, I. (1983). Chronic Parkinsonism in humans due to a product of Meperidine-analog synthesis. *Science*, *219*(4587), 979-980.
- Parkinson, J. (2002). An essay on the shaking palsy. *Journal of Neuropsychiatry and Clinical Neuroscience*, 14(2), 223-236.

#### **Additional Readings of Interest**

- Gerstenbrand, F., & Karamat, E. (1999). Adolf Hitler's Parkinson's disease and an attempt to analyze his personality structure. *European Journal of Neurology*, 6(2), 121-127.
- Jones, J. (2004). Great shakes: Famous people with Parkinson's disease. *Southern Medical Journal*, 97(12), 1186-1189.

#### Week 9: Executive Cognitive Deficits in Parkinson's disease

- Barkeley, R. A. (2001). The executive functions and self-regulation: An evolutionary neuropsychological perspective. *Neuropsychology Review*, 11(1), 1-29.
- Ettlin, T., & Kischka, U. (1999). Beside frontal lobe testing: "The frontal lobe score." In B. L. Miller & J. L. Cummings (Eds.), *The human frontal lobes: Functions and disorders* (pp. 233-246). New York: The Guilford Press.

#### Week 10: Personality in Parkinson's disease

- McNamara, P., Durso, R., & Harris, E. (2007). "Machiavellianism" and frontal dysfunction: Evidence from Parkinson's disease.' *Cognitive Neuropsychiatry*, *12*(4), 285-300.
- Stuss, D. T., Glow, C. A., & Hetherington, C. R. (1992). "No longer Gage": Frontal lobe dysfunction and emotional changes. *Journal of Consulting and Clinical Psychology*, *60*(3), 349-359.

You will be assigned additional readings in class.

# Week 13: Introduction to Evolutionary Theory – Part II: Evolutionary Theories of Religion from the Perspective of Cognitive Neuroscience

Banyas, C. A. (1999). Evolution and phylogenetic history of the frontal lobes. "In B. L. Miller & J. L. Cummings (Eds.), *The human frontal lobes: Functions and disorders* (pp. 83-106). New York: The Guilford Press.

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# Course Schedule for Physics Semester (Spring 2013)

### Segment P1: Electromagnetism [Prof. Wildman]

| Week 1 | Basic laws of electrostatics (Coulomb, Ampere, and Faraday)  |
|--------|--|
| Week 2 | Maxwell's equations (including theorems of Gauss and Stokes) |

#### **Oral Examination of Material in Segment P1**

#### Segment P2: Special Theory of Relativity [Prof. Wildman]

| Week 3 | Conceptual Basics (classical mechanics; Galilean transformation; inertial frames of reference; motivation for a new mechanics; Lorentz transformation)                 |
|--------|--|
| Week 4 | Relativistic Mechanics (postulates of STR; relativity of simultaneity; length contraction; time dilation; addition of velocities; twin paradox; experimental evidence) |
| Week 5 | Relativistic Dynamics (mass-energy equivalence), Electrodynamics and relativity (Maxwell's equations in tensor notation)   |

#### **Oral Examination of Material in Segment P2**

### Segment P3: General Theory of Relativity [Prof. Wildman]

| Week 6 | Conceptual Basics (theory of gravity or general theory of relativity?), Space-Time Tells<br>Matter-Energy how to Move (geometric point of view; the equation of geodesic deviation;<br>Riemann tensor; analogy with electromagnetism and Newtonian physics; calculating<br>Riemann components) |
|--------|--|
| Week 7 | Matter-Energy Tells Space-Time how to Curve (calculating with equation of geodesic deviation; Einstein tensor; stress-energy tensor)   |
| Week 8 | Einstein's Field Equations (approximation methods for solving Einstein's field equations for entire universe; the closed universe; cosmological constant; other applications of GTR)   |
|        | No Class: Spring Recess  |

#### Segment P4: Cosmology [Prof. Wildman]

| Week 9  | Early Cosmology (ancient and medieval concepts, planetary system debates, Galileo, Kepler)                                  |
|---------|---|
| Week 10 | Big Bang cosmology (basic observations and theoretical model), Quantum cosmologies (competing models of the early universe) |

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### Oral Examination of Material in Segments P3, P4

### Segment P5: Quantum Mechanics [Prof. Wildman]

| Week 12 | Basic Experiments and Theoretical Moves (Plank's postulate; photoelectric effect; Compton effect; atomic spectra; DeBroglie's postulate; scattering experiments; low-intensity polarization; double-slit experiment; uncertainty principle) |
|---------|---|
| Week 13 | Formalism (Stern-Gerlach experiment; prediction versus explanation; wave functions; states, properties, and measurements; quantum electrodynamics)  |
|         | No Class: Substitute Monday Schedule  |
| Week 14 | Non-Locality (Bohr versus Einstein; Einstein-Podolsky-Rosen thought experiment; Bell's inequalities)  |
| Week 15 | Interpretations of Formalism (basic problems from the measurement problem to quantum chaos; Copenhagen "interpretation"; theories of measurement from DeBroglie, Bohm, and Popper to von Neumann, Wigner, and Everett)                      |

**Oral Examination of Material in Segment P5** 

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# Fall 2012 Mathematics Schedule

### Segment M1: One-Dimensional Calculus [Prof. Wildman]

| Week 1 | Introduction (mathematical notation; number system; functions; continuity)  |
|--------|---|
| Week 2 | Differentiation I (from first principles; geometrical interpretation of the derivative; circles, sine and cosine functions) |
| Week 3 | Differentiation II (basic derivatives; basic rules of differentiation; differential equations)                              |
| Week 4 | Integration I (from first principles; geometric interpretation of integral; sine and cosine functions revisited)            |
| Week 5 | Integration II (definite versus indefinite integrals; basic integration rules and techniques)                               |
| Week 6 | Fundamental Theorem of Calculus (relation between areas under curves and anti-derivatives)                                  |

#### **Oral Examination of Material in Segment M1**

#### Segment M2: Vector Spaces and Basic Linear Algebra [Prof. Wildman]

| Week 7 | Vectors (geometrical interpretation; basic operations; length; angle), Bases (linear combinations; linear independence; dimensionality) |
|--------|---|
| Week 8 | Vector Spaces (definition; functions)   |

### Segment M3: Vector Calculus (for Physics Segment P1) [Prof. Wildman]

| Week 9  | Generalizing the Derivative (directional derivative; gradient; divergence; curl; notation) |
|---------|--|
| Week 10 | Generalizing the Integral (path integral; surface integral; volume integral)               |
| Week 11 | Amazing Theorems (divergence theorem; Stoke's theorem)                                     |
|         | No Class: Thanksgiving Recess  |
| Week 12 | Vector Calculus Applications (electrostatics)  |
| Week 13 | Review and practice  |

#### **Oral Examination of Material in Segments M2, M3**

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### Spring 2013 Mathematics Schedule

### Segment M3 (continued): Vector Calculus (for Physics Segment P1) [Prof. Wildman]

| Week 1 | Vector Calculus Applications, continued (electrostatics) |
|--------|--|
|--------|--|

#### Segment M4: More Linear Algebra (for Physics Segment P2) [Prof. Wildman]

| Week 2 | Basis Change (coordinate systems; bases; basis change functions)  |
|--------|---|
| Week 3 | Matrices (definition; matrix algebra; solving simple simultaneous equations; basis change functions represented as matrices; Galilean transformation; Lorentz transformation) |

#### Segment M5: Tensor Calculus (for Physics Segments P3, P4) [Prof. Wildman]

| Week 4 | Understanding the Metric Tensor and the Polarization Tensor (building physical intuition for tensors; creating mathematical notation for describing the physics) |
|--------|--|
| Week 5 | Tensors in General Form (multi-linear functions; linear functionals; contravariant and covariant indices; partial derivatives)                                   |
| Week 6 | Examples (electromagnetic tensor; Riemann curvature tensor; stress-energy tensor)  |
| Week 7 | Breaking Down the Einstein Field Equations (Riemann curvature tensor; Ricci tensor; connections; Christoffel symbols; Einstein tensor)                           |

#### Segment M6: Hilbert Spaces (for Physics Segment P5) [Prof. Wildman]

| Week 8 | Hilbert Spaces (definition; bases; orthonormal bases; basis change)  |
|--------|--|
|        | No Class: Spring Recess  |
| Week 9 | Functions on Hilbert Spaces (functions; operators), Application to Quantum Mechanics (wave functions, observables, and measurements) |

#### Segment M7: Complex Analysis (for Physics Segment P5) [Prof. Wildman]

| Week 10 | Complex Number System (numbers, operations, converting between polar and Cartesian coordinates)                               |
|---------|---|
| Week 11 | Complex Functions (examples of complex functions, complex exponential function, application to wave functions, wave equation) |

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## Segment M8: Chaos Theory [Prof. Wildman]

| Week 12 | The Logistic Mapping (understanding iteration; exploring bifurcation diagram using computer software; identifying regimes) |
|---------|--|
|         | No Class: Substitute Monday Schedule   |
| Week 13 | Chaos (definitions; controversies; philosophical issues from modeling to meaning)  |
| Week 14 | Review and practice  |

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### Examination Content, Described by means of Sample Questions

These questions merely indicate the content of oral examinations. Exams are not limited to these questions. In general, and throughout the exams where appropriate, be prepared to speak about the relevance of the scientific material to philosophical, ethics, metaphysical, and theological questions (we call these "boundary issues").

#### Examination of Biology Segments B1, B2, B3: Chemistry and Biochemsitry

What are fermions (leptons and quarks), bosons? What do they do, what do they make, how do they interact?

Explain why the periodic table arranged the way it is.

What is electron configuration for a given element? valence number? group? Calculate chemical formula for simple ionically bonded compounds based on valence numbers. "Read" a symbolic chemical structure of an organic molecule.

Desribe the various types of chemical bonds and their relative strengths (ionic bonds, covalent bonds, hydrogen bonds, Van der Waal's forces)

How does a chemical reaction work? What role does a catalyst play in a chemical reaction? What is a favorable reaction? How do you run reactions in unfavorable directions? Draw reaction energy diagrams.

Describe the four main macromolecules, their monomers, differences in their structure.

Lipids: triglycerides, phospholipids, cholesterol. What is hydrophobicity? Lipid bilayer? Carbohydrates: 6-member glucose ring, polysaccharides Proteins: amino acid structure, types of amino acid side chains, peptide bond formation Nucleic acids: nucleotide structure, four nucleotides, purines vs. pyrimidines

Describe the role of hydrogen bonding in formation of protein secondary structure (alpha helix, beta sheet), DNA double helix, DNA:RNA complexes during transcription and RNA-RNA complexes during translation.

How did the Miller-Urey experiments try to recreate the origin of biological molecules on young Earth?

Describe the role of protein enzymes as biological catalysts. Give an example of a chemical reaction facilitated by enzymatic activity.

Describe the structure and function of following cellular components: plasma membrane, cell wall, cytoplasm, cytoskeleton, nucleus, rough endoplasmic reticulum, smooth endoplasmic reticulum, Golgi, mitochondria, chloroplast. What mitochondrial processes lead to ATP production?

What are exocytosis, endocytosis and phagocytosis? What is the connection between these processes and movement of membrane vesicles within a cell? What is endosymbiotic hypothesis?

Draw a schematic and name the phases of the cell cycle. Where does DNA replication occur? What important checkpoint control must happen during the G1 and G2 gap phases to ensure smooth

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progression towards mitosis? Describe the processes that occur during mitosis (chromosomal condensation, disassembly of nuclear envelope, chromosomal alignment, chromosomal separation and physical separation of the daughter cells). What cytoskeletal structures pull chromosomes apart?

What experiments demonstrated the role of DNA as hereditary material? How is DNA organized in chromosomes? Why DNA replication is called "semiconservative"? Definition of a gene and the concept of gene expression. What is genetic code? Transcription; mRNA processing; introns and exons. tRNA, rRNA, ribosome and the "decoding" process; catalytic activity of RNA.

#### Examination of Biology Segments B4, B5: Cell Biology and Evolutionary Biology

Describe the types of cell. Describe the structure and function of following cellular components: plasma membrane, cell wall, cytoplasm, cytoskeleton, nucleus, rough endoplasmic reticulum, smooth endoplasmic reticulum, Golgi, mitochondria, chloroplast.

Give a brief overview of mitochondrial processes that lead to ATP production.

Give a brief overview of exocytosis, endocytosis and phagocytosis. What is the connection between these processes and movement of membrane vesicles within a cell?

Draw a schematic and name the phases of the cell cycle. Where does DNA replication occur? What important checkpoint control must happen during the G1 and G2 gap phases to ensure smooth progression towards mitosis?

Describe the processes that occur during mitosis. You do not have to memorize specific names of the phases (although you may find it helpful). However, you need to describe the steps of chromosomal condensation, disassembly of nuclear envelope, chromosomal alignment, chromosomal separation and physical separation of the daughter cells. What cytoskeletal structures pull chromosomes apart?

Give a brief overview of gamete production during meiosis. What is diploid, haploid, polyploid number of chromosomes?

Describe cells in a functional context (either the immune system of the nervous system, depending on what was covered in class).

Summarize the work of Gregor Mendel. What two main principles of genetics were derived from his work (Independent Assortment and Segregation)? What is the molecular biological basis for these principles?

Write out a Punnett square for a single gene cross between a) two heterozygote parents and b) heterozygote parent and homozygote parent. Examples: 1) Hb<sup>wt</sup>hb<sup>mut</sup> x Hb<sup>wt</sup>hb<sup>mut</sup>; 2) Hb<sup>wt</sup>hb<sup>mut</sup> x Hb<sup>wt</sup>Hb<sup>wt</sup>; 3) CF<sup>wt</sup>cf<sup>mut</sup> x CF<sup>wt</sup>cf<sup>mut</sup>; 4) CF<sup>wt</sup>cf<sup>mut</sup> x CF<sup>wt</sup>CF<sup>wt</sup>.

Write out a Punnett square for a cross involving a gene on an X chromosome. Examples:  $X^{wt}X^{mut} \times X^{wt}Y$ ;  $X^{wt}X^{mut} \times X^{mut}Y$ .

In mice there are two separate alleles for coat color and hair length. The dominant alleles are gray coat with short hair and the recessive alleles are tan coat with long hair. Work out a cross between a

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homozygous dominant mouse with a homozygous recessive mouse in the P generation and predict the allelic distribution in the F1 and F2 generations.

Describe Hardy-Weinberg law and the assumptions that underlie this law. What factors can affect the stability of gene frequencies?

Describe (as a narrative) relationship between genotype and phenotype (from gene to function with steps in between).

What are alleles of a gene? What are protein domains? How mutation and domain shuffling can lead to diversification within a genome?

Present major postulates of Darwin's theory of natural selection, and describe how Darwin's idea of "descent with modification" has been explained in light of the modern chromosomal theory of inheritance. What evidence did Darwin adduce in support of his theory? What were its major flaws? What is the Modern Synthesis?

What is natural selection? What are examples of selective pressures that operate on individuals within a population?

How does speciation occur? What are the factors relevant to population and evolutionary change?

Developmental biology: define and briefly discuss the following concepts: zygote, cell cleavage, blastula, gastrulation, inner cell mass of a human embryo, cell fate and cell "potency", connection between cellular differentiation and gene expression, conservation of genetic networks in development of different species, maternal influence on embryonic development, somatic cell nuclear transfer, adult stem cells.

#### **Examination of Mathematics Segments M1: One-Dimensional Calculus**

What is a function? Continuous function? Graph of a function? Tangent to a graph? Slope of a tangent?

How do the sine and cosine functions relate to the geometry of a circle?

Define the derivative (from first principles). Describe the geometric meaning of a derivative.

What are basic rules of differentiation? Basic derivatives? Differential equations?

Define the integral (from first principles). Describe the geometric meaning of an integral. Distinguish definite from indefinite integrals.

What are basic rules of integration? Basic integrals? Basic integration techniques?

What is an anti-derivative? State the fundamental theorem of calculus? Describe the relation between anti-derivatives and areas under curves.

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#### Examination of Mathematics Segments M2, M3: Vector Calculus

What is a vector space? linear combination? linear dependence and independence? basis?

How do we define a metric on a vector space? Explain "a metric is a bi-linear, positive-definite quadratic form." Examples of metrics on  $R^2$ , including graphs of length-1 vectors in Euclidean and Lorentzian metrics.

How do we use a metric to speak of length of vectors and angle between vectors? What is orthonormal basis? coordinate system? How do we represent the same vectors in more than one coordinate system?

What is scalar (dot) product? vector (cross) product? linearity of an operation? test for orthogonality? right-hand rule? geometric and coordinate representation of dot product and cross product?

What are examples of functions with a variety of vector-space domains and ranges? vector fields and scalar fields? component scalar fields of a vector field?

What is directional derivative? partial derivative relative to a basis?

What is gradient? del? divergence? curl?

What is integral over a curve? a surface? a volume?

What is flux? circulation?

What is Gauss's theorem (divergence theorem)? Stokes' Theorem?

#### **Examination of Physics Segments P1: Electromagnetism**

State Maxwell's equations in differential and integral form. Show how to derive the integral from the differential form, and *vice versa*.

Explain the connection between Maxwell's equations and the basic results of electrostatics. Derive Coulomb's law from Maxwell I and Ampere's Law from Maxwell II.

Write down the field equation for Electromagnetic radiation. (Bonus: derive it from Maxwell's equations!) Explain the velocity of electromagnetic radiation from the field equation.

How do Maxwell's equations establish the unification of light and electromagnetism? What is the significance of this result?

#### **Examination of Physics Segments P2: Special Theory of Relativity**

What is an inertial frame of reference? Principle of relativity? Galilean transformation?

State the postulates of STR. Describe the Lorentz transformation and its significance.

State the mechanical consequences of STR: relativity of simultaneity (via thought experiment), length contraction and time dilation (write up formulas), addition of velocities (write up formula).

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State the dynamical consequences of STR: mass-energy equivalence (explain the energy triangle).

Describe experiments confirming STR.

What is a space-time diagram? Use one to explain the Lorentz Metric versus the Euclidean metric. Use one to explain the twin paradox.

What is the philosophical significance of STR for understanding space and time?

### Examination of Physics Segments P3, P4: General Theory of Relativity and Cosmology

Tensors
 Tensor in general form
 Coordinate language verus "object" language
 Einstein summation convention
 Examples of tensors (metric tensor, Riemann)
 Differentiation of tensors
 Parallel transport, geodesics, and curvature
 Parallel transport, geodesics,

2. General Theory of Relativity
Why the name GTR rather than "theory of gravity"?
Geometric point of view (unconstained motion defines a geodesic in a curved space)
Global versus local point of view
Equation of geodesic deviation for a sphere (derive and interpret)
Equation of geodesic deviation generally (state and interpret)
Riemann curvature tensor (calculate Reimann components near the earth and inside the earth)
Definition of Einstein Tensor and its constitutive tensors
Einstein's field equations (state and interpret)

3. Big-Bang Cosmology

Basic assumptions: homogeneity and isotropy meaning of t,t component of field equations when density is constant [ $(a'')^2=(8\pi\rho a^2)/3 - 1$ ] interpretation as dynamic universe; Einstein's reaction (introduced cosmological constant) Big-Bang Cosmology Evidence (Hubble, CBR, nuclear abundance, dark night sky,...) Narrative of early universe, including connections between high-energy particle physics and cosmology Inflation used to explain problems (such as flatness of universe and variations in CBR)

4. Quantum Cosmologies
The overriding purpose of quantum cosmologies
The connection between high-energy particle physics and quantum cosmologies
Various quantum cosmologies—qualitatively describe and compare
The metaphysical significance of quantum cosmologies

### **Examination of Physics Segments P5: Quantum Machanics**

1. Early discoveries

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1.1 Energy quantization of radiation
Plank (1901) Black Body
Einstein (1905) Photoelectric Effect
Bohr (1913) Atomic Spectra
Compton (1923) Scattering Xrays from foil
1.2 Interference effects of particles
DeBroglie's (1924) postulate of wavelength tied to momentum
Davisson-Germer (1927) and Thompson (1928) crystal scattering and transmission of electrons
1.3 Double-slit experiment (illustrates Heisenberg Uncertainty Principle)
1.4 Stern-Gerlach experiment (illustrates probabilities nature of measurement outcomes)

2. Formalism

2.1 Mathematical interpretation of systems, states, observables, measurement

2.2 von Neumann's Hilbert Space approach

2.3 Born's Projection Postulate

2.4 Schrödinger's Equation

3. Non-locality

3.1 Einstein-Podolsky-Rosen thought experiment (1935): locality entails violation of uncertainty principle, which implies incompleteness of quantum mechanics

3.2 Bell's inequalities: locality entails that statistics from experiments on correlated particles pairs should conform to specific inequalities (but Aspect's experiments show they do not, thus demonstrating non-locality)

3.3 Non-locality and faster-than-light information transfer

4. Philosophical Interpretation

4.1 Three levels of interpretation

Correspondence rules and associated principles connecting formalism to observable phenomena

Creating conceptually unifying, semi-pictorial models

Adjustments to theory on the basis of appealing models

4.2 Major interpretations

Standard (Copenhagen) interpretation (distinguish from Bohr)

Many Worlds and Many Minds interpretations

Hidden Variables interpretations (esp. Bohm)

Continuous Spontaneous Localization theories

4.3 Significance for theology (optional)

Freedom versus determinism

Locus for natural-law-conforming action of divine being

Entanglement and unity of divine creation