## MA 581 Qualifier Problems: Spring 2007

- 1. A fair coin is tossed until the first heads appears. Then, a fair, six-sided die is rolled as many times as the coin was tossed.
  - a. Find the probability that the experimenter requires between 5 and 20 tosses (inclusive) to get her first heads on the coin.
  - b. Find the probability that the die *never* rolls a "5."
  - c. Suppose this experiment is conducted, and the experimenter's die tosses *never* rolled a "5." Find the probability that she had needed to toss the coin exactly 7 times.
- 2. The r.v. X has pdf  $f(x)=cx^2$ , for 0 < x < 3, and f(x)=0 for other values of x.
  - a. Find the value of c.
  - b. Find the standard deviation of X.
  - c. Find  $E(e^{X}/X^{2})$ .
  - d. Define the *tierce* of a r.v. to be a number t satisfying P(X>t)=1/3. Find the *tierce* of X.
  - e. Suppose X and Y are iid, each having pdf  $f(x)=cx^2$ , for 0 < x < 3, and f(x)=0 for other values of x. Find the covariance of X+Y and X, that is, cov(X+Y, X).