

# Hemispherical Lens Based Imaging Receiver for MIMO Optical Wireless Communications

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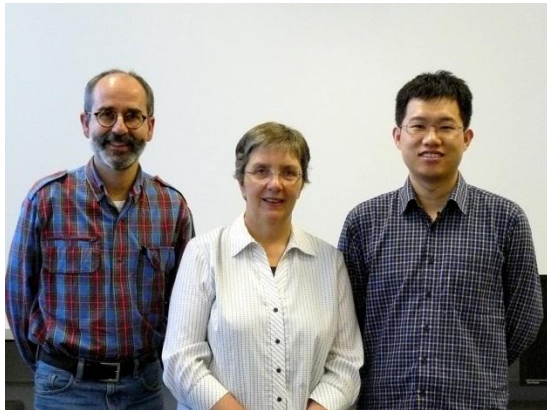
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# Outline

Introduction

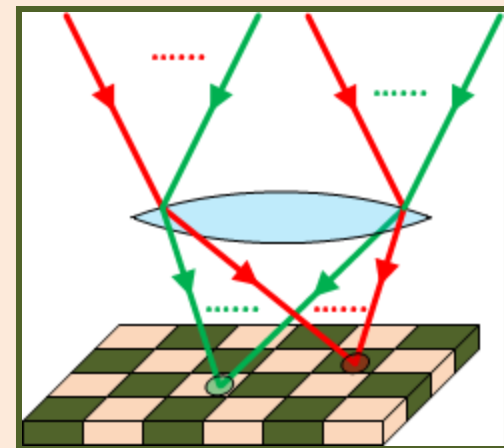
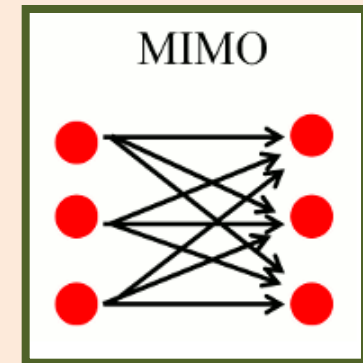
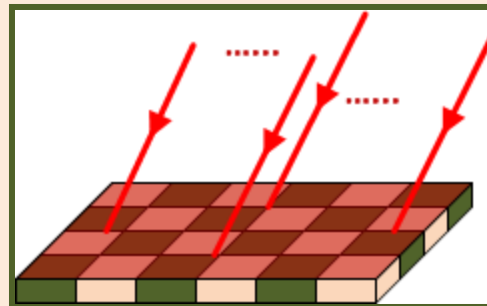
System description and analysis

Simulation results

Summary

# MIMO Optical Wireless System with Imaging Receiver

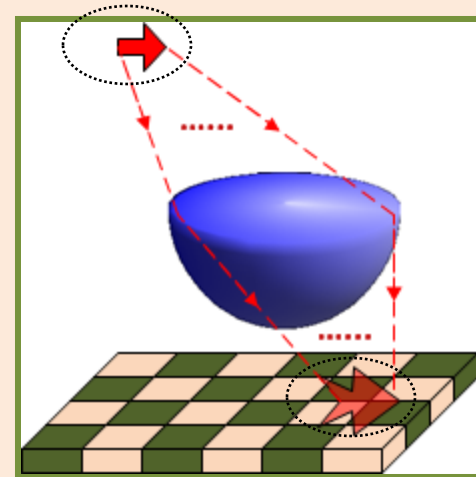
- ✓ MIMO has potential to increase the data rate and the robustness of optical wireless systems
- ✓ Non imaging receiver
  - evenly distributed power
  - very little diversity
- ✓ Imaging receiver using conventional lens
  - significant spatial diversity
  - small field of view (FoV)



- ✓ **Can we increase the FoV with a different lens?**
- ✓ **Given a different lens, can we still have spatial diversity?**

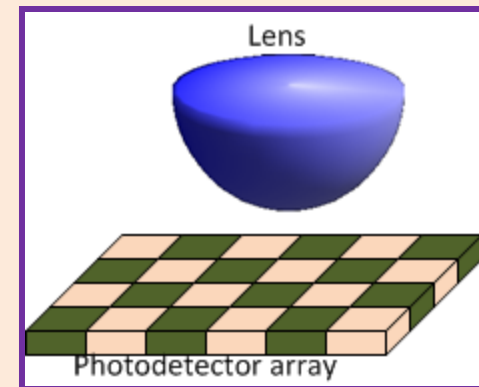
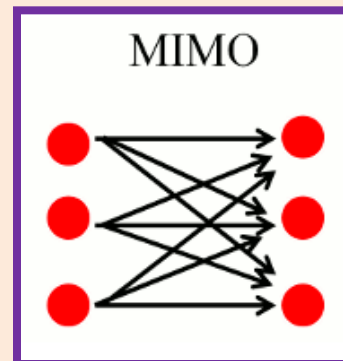
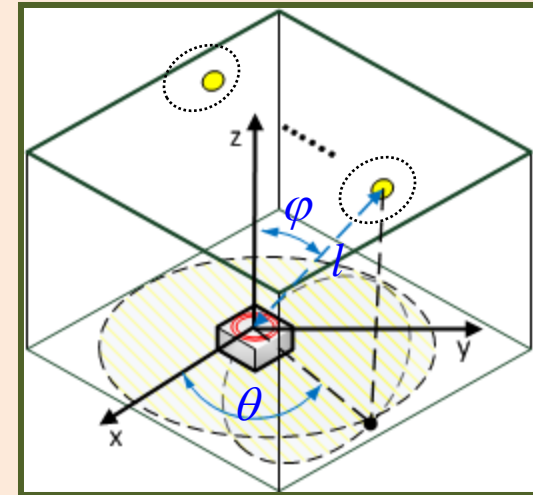
# Imaging Receiver Using Hemispherical Lens

- ✓ Hemispherical lens
  - gives wide field of view, used for cloud recording as early as 1920s
  - forms distorted images
  - not a problem for IM/DD
- ✓ Contribution of this work
  - Study the MIMO channel gain with hemispherical lens based receiver
  - Calculate total received power as a function of angle of incidence and show the wide FoV of the receiver
  - Demonstrate spatial diversity by observing the images of the LEDs and calculating the channel matrix.



## System Description

- ✓  $N_t$  Generalized Lambertian LEDs installed on the ceiling, pointing down
  - LED is placed at  $S:(l \sin \varphi \cos \theta, l \sin \varphi \sin \theta, l \cos \varphi)$
  - Therefore  $\varphi$  is the angle of incidence
  - emitting un-polarized light
  - Radiation pattern:  $R_o(\phi) = \frac{(m+1)}{2\pi} \cos^m \phi$
  - where  $m = -\ln 2 / \ln(\cos \Phi_{1/2})$
- ✓ The receiver put on the floor, pointing up
  - Lens is of radius  $R$  and refraction index  $n$
  - $N_r$  photodetectors
  - A  $N_r \times N_t$  Channel Matrix



## Analysis

### ✓ Ray tracing

- reflection and refraction on the surface of the lens
- two refractions: change the direction the ray travels and are governed by Snell's Law

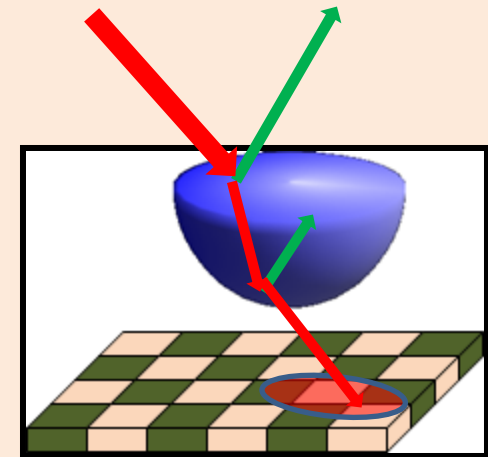
$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

$n_1$   $n_2$ : refractive index of media 1 and media 2, respectively.  $\alpha_1$ : angle of incidence  $\alpha_2$ : angle of refraction

- two reflections: results in the loss of optical power governed by Fresnel equations

$$R_p(\alpha_1, \alpha_2) = \frac{n_1 \cos \alpha_2 - n_2 \cos \alpha_1}{n_1 \cos \alpha_2 + n_2 \cos \alpha_1} \quad R_s(\alpha_1, \alpha_2) = \frac{n_1 \cos \alpha_1 - n_2 \cos \alpha_2}{n_1 \cos \alpha_1 + n_2 \cos \alpha_2}$$

--For un-polarized light, the power transmission coefficient is  $T = 1 - \frac{1}{2}(R_s^2 + R_p^2)$



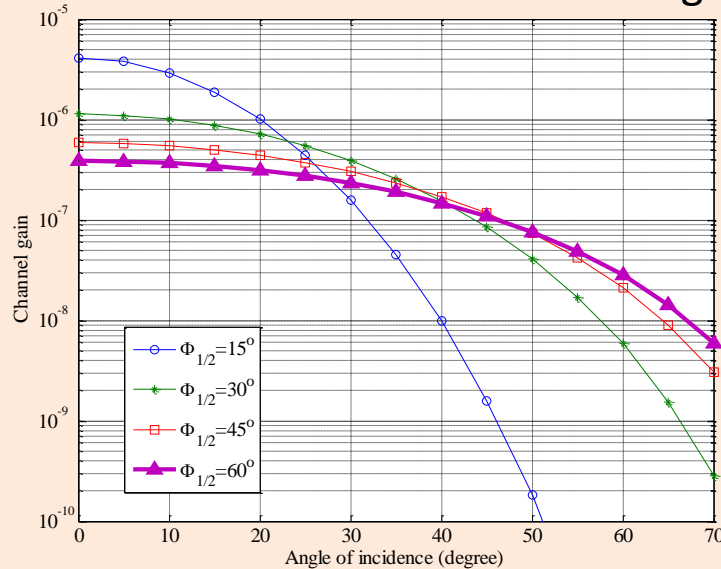
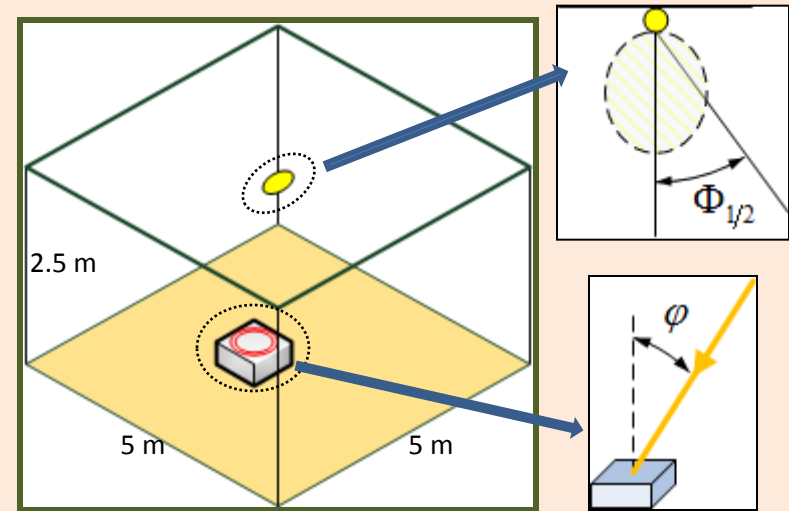
receiver

### ✓ Channel gain

$$\frac{P_o}{P_i} = \frac{(m+1) \cos^m \phi \cos \varphi T_{\text{air-lens}}(\alpha_1)}{2\pi l^2} \iint_{\alpha_3 < \arcsin(n_1/n_2)} T_{\text{lens-air}}(\alpha_3, \alpha_4) r dr d\beta$$

## Calculated total received power as a function of angle of incidence

- ✓ Settings
  - 5 m x 5 m x 2.5 m room
  - One LED on the ceiling pointing down with semi-angle  $\Phi_{1/2}$
  - Receiver put on the floor pointing up with 5 mm lens and a photodetector.
  - Therefore the maximum angle of incidence available is 70.5 degrees



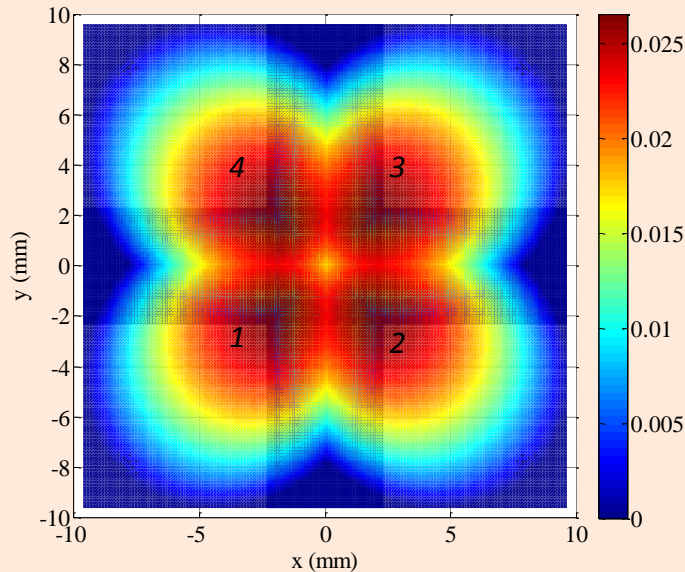
Channel gains versus the angle of incidence for Lambertian emitters with varying half power semi-angles

- ✓ Channel gain drops at different rates
- ✓ Adequate gain provided by some of LEDs at large angle of incidence
- ✓ Field of view depends on half power semi angles of transmitters:
  - Large half power semi-angle = Greater field of view
- ✓ Large half power semi-angle
  - Adequate gain out to 70 degrees angle of incidence

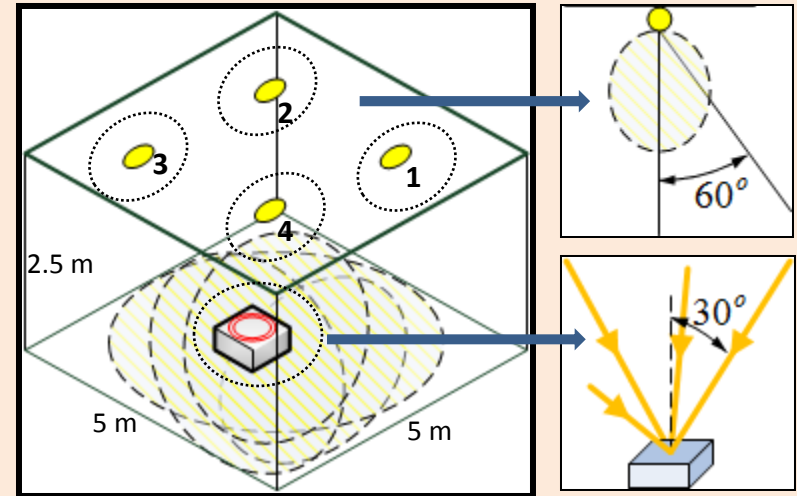
## Power Density on Imaging Plane

### ✓ Settings

- 5 m x 5 m x 2.5 m room
- four Lambertian LEDs, with semi-angles 60 degrees, on the ceiling making 30 degrees of angle with the receiver
- Receiver put at the center of the floor pointing up with 5 mm lens and four photodetectors. Each covers one quadrant.



Four LEDs with 30 degrees of angle of incidence



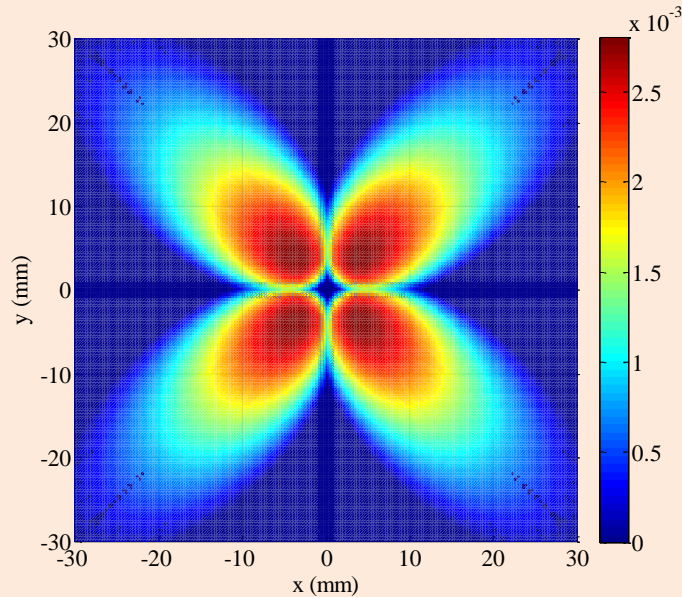
- ✓ Images of four LEDs are clearly separated
- System with four photodiode receivers would have significant diversity

$$\mathbf{H} = \begin{bmatrix} 0.009 & 0.151 & 1.124 & 0.151 \\ 0.152 & 0.01 & 0.157 & 1.13 \\ 1.136 & 0.158 & 0.011 & 0.158 \\ 0.152 & 1.13 & 0.157 & 0.01 \end{bmatrix} \times 10^{-6}$$

- ✓ Little correlation between rows or columns
- Good diversity

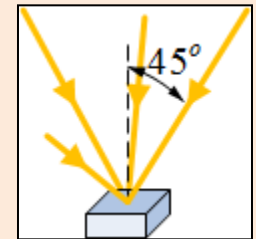
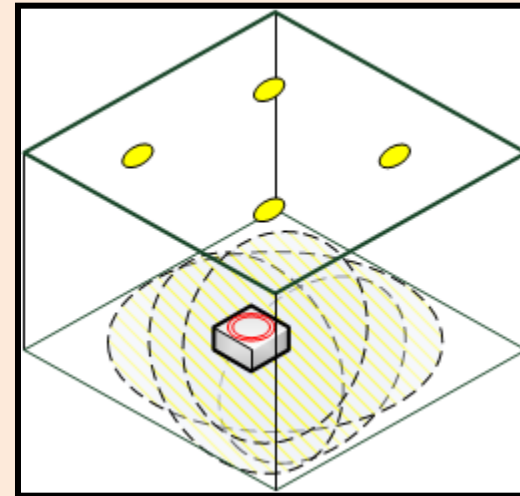


## Effect of more widely spaced transmitters



Four LEDs with 45 degrees of angle of incidence

- ✓ With more widely spaced transmitters
  - Angle of incidence increases
  - Overall received power decreases
  - Completely separated images

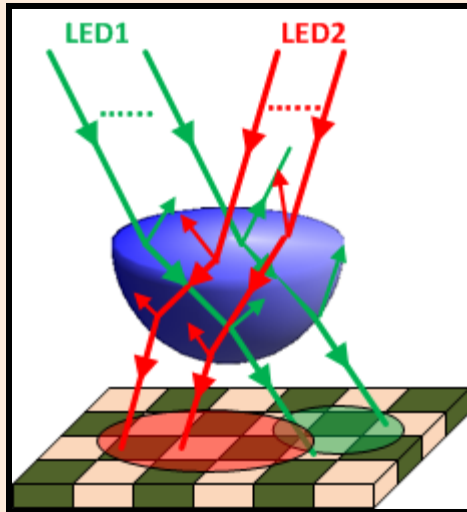


$$\mathbf{H} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

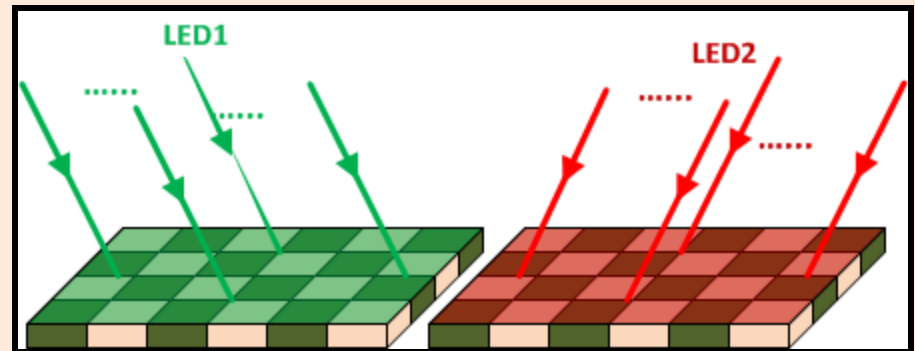
- ✓ No correlation between rows and columns
  - Full diversity

## Imaging with Hemispherical lens vs Non Imaging

Imaging



Non-imaging



- ✓ Optical power distributes unevenly in each image
- ✓ Various LEDs form separated images

$$\mathbf{H} = \begin{bmatrix} h_{1,1} & h_{1,2} & \cdots & h_{1,N_t} \\ h_{2,1} & h_{2,2} & \cdots & h_{2,N_t} \\ \vdots & \vdots & \cdots & \vdots \\ h_{N_r,1} & h_{N_r,2} & \cdots & h_{N_r,N_t} \end{bmatrix}$$

- ✓ The channel matrix is of full rank
- ✓ Therefore provides full diversity order

- ✓ The optical power distributes evenly among the photodetectors

$$\mathbf{H} = \underbrace{\begin{bmatrix} h_1 & h_2 & \cdots & h_{N_t} \\ h_1 & h_2 & \cdots & h_{N_t} \\ \vdots & \vdots & \cdots & \vdots \\ h_1 & h_2 & \cdots & h_{N_t} \end{bmatrix}}_{\text{Unit-ranked}}$$

- ✓ Therefore no diversity provided

# Summary

In this work, we have answered the following questions:

Can we increase the FoV with a different lens?



The imaging receiver has large field of view with a hemispherical lens— as large as 70 degrees for a Lambertian LED

Given a different lens, can we still have spatial diversity?



Spatial diversity is also provided by the lens— full ranked channel matrix

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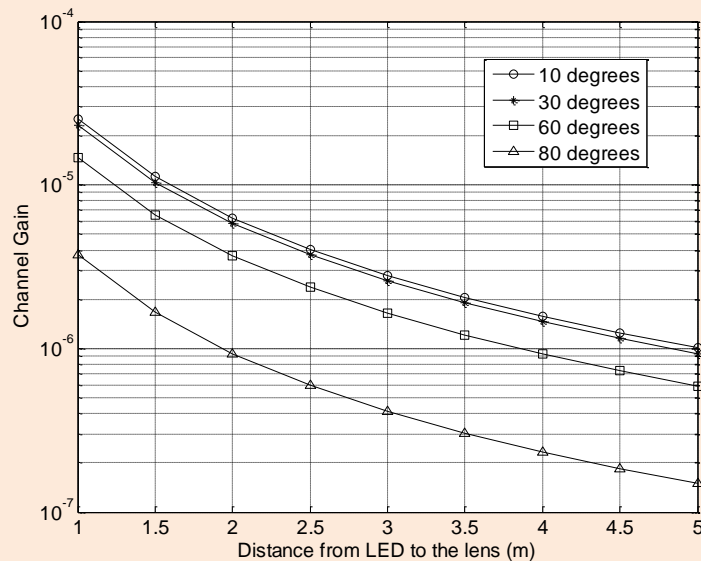
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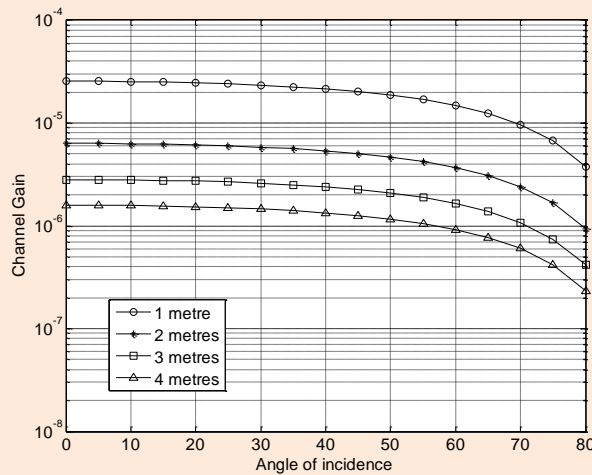
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Thank you!

# Additional Graphs



- ‘Total’ channel gain versus distance
  - Total received power on photodetector/power transmitted by LED
- LED semi-angle 15 degrees
- **LED pointing directly at receiver**



- ‘Total’ channel gain versus angle of incidence
  - Total received power on photodetector/power transmitted by LED
- LED semi-angle 15 degrees
- **LED pointing directly at receiver**