

$$f \sim \alpha xy \left(\frac{s_b}{s_f}\right)^a \rightarrow A = xy \Phi\left(\frac{s_b}{s_f}\right)$$

$$A \sim \alpha_1 xy \left(\frac{s_b}{s_f}\right)^{a_1} + \alpha_2 xy \left(\frac{s_b}{s_f}\right)^{a_2} + \dots \rightarrow \frac{A}{xy} \sim \left(\frac{s_b}{s_f}\right)^a$$

$$A \sim \alpha_1 xy (\pi_1)^{a_1} (\pi_2)^{b_1} + \alpha_2 xy (\pi_1)^{a_2} (\pi_2)^{b_2} + \dots$$

$$A = xy \Phi(\pi_1, \pi_2)$$

\downarrow
f(u,v)

$$v: LT^{-1} \quad g: LT^{-2} \quad \frac{s_b}{s_f}: \text{unitless}$$

$$R: L \quad v: L^2 T^{-1}$$

$$LT^{-1} = L^a (LT^{-1})^b (L^2 T^{-1})^c$$

$$a+b+2c=1$$

$$-2b-c=-1$$

$$a = \frac{1-3c}{2}$$

$$b = \frac{1-c}{2}$$

$$v \sim R^{k-\frac{3}{2}c} g^{k-\frac{1}{2}c} v^c \Phi\left(\frac{s_b}{s_f}\right)$$

$$\sim \sqrt{Rg} \left(\frac{v}{Rg}\right)^c \Phi\left(\frac{s_b}{s_f}\right)$$

$$\Phi_2 \uparrow$$

$$2gR^2(s_b - s_f) / 4v s_f = \frac{gR^2}{v} \left(\frac{2}{4}\right) \left(\frac{s_b - s_f}{s_f}\right) \rightarrow \left(\frac{s_b}{s_f} - 1\right)$$